

# VIS EXAMPLES

## FOR MULTIVARIATE NETWORKS

---

CMPT 733

STEVEN BERGNER

SURVEY PAPER AND TUTORIAL BY  
CAROLINA NOBRE, MARC STREIT, ALEXANDER LEX



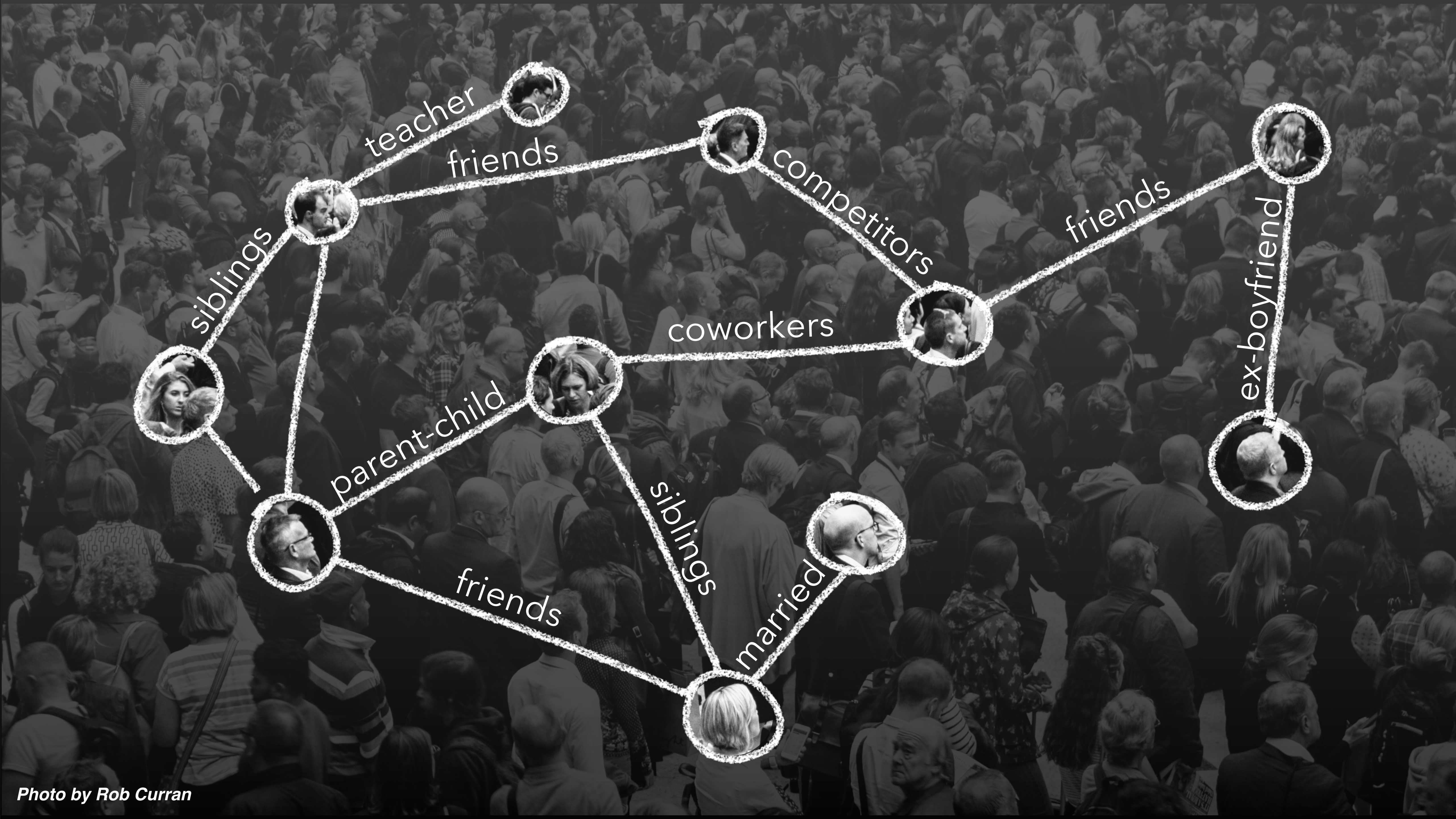


Photo by Rob Curran



Name: Samuel  
Age: 41  
Job: Nurse

Name: Julia  
Age: 34  
Job: Vet

Name: Ellen  
Age: 31  
Job: Actress

Name: Gordon  
Age: 54  
Job: Chef

Name: Roger  
Age: 51  
Job: Doctor

Name: Camille  
Age: 42  
Job: Teacher

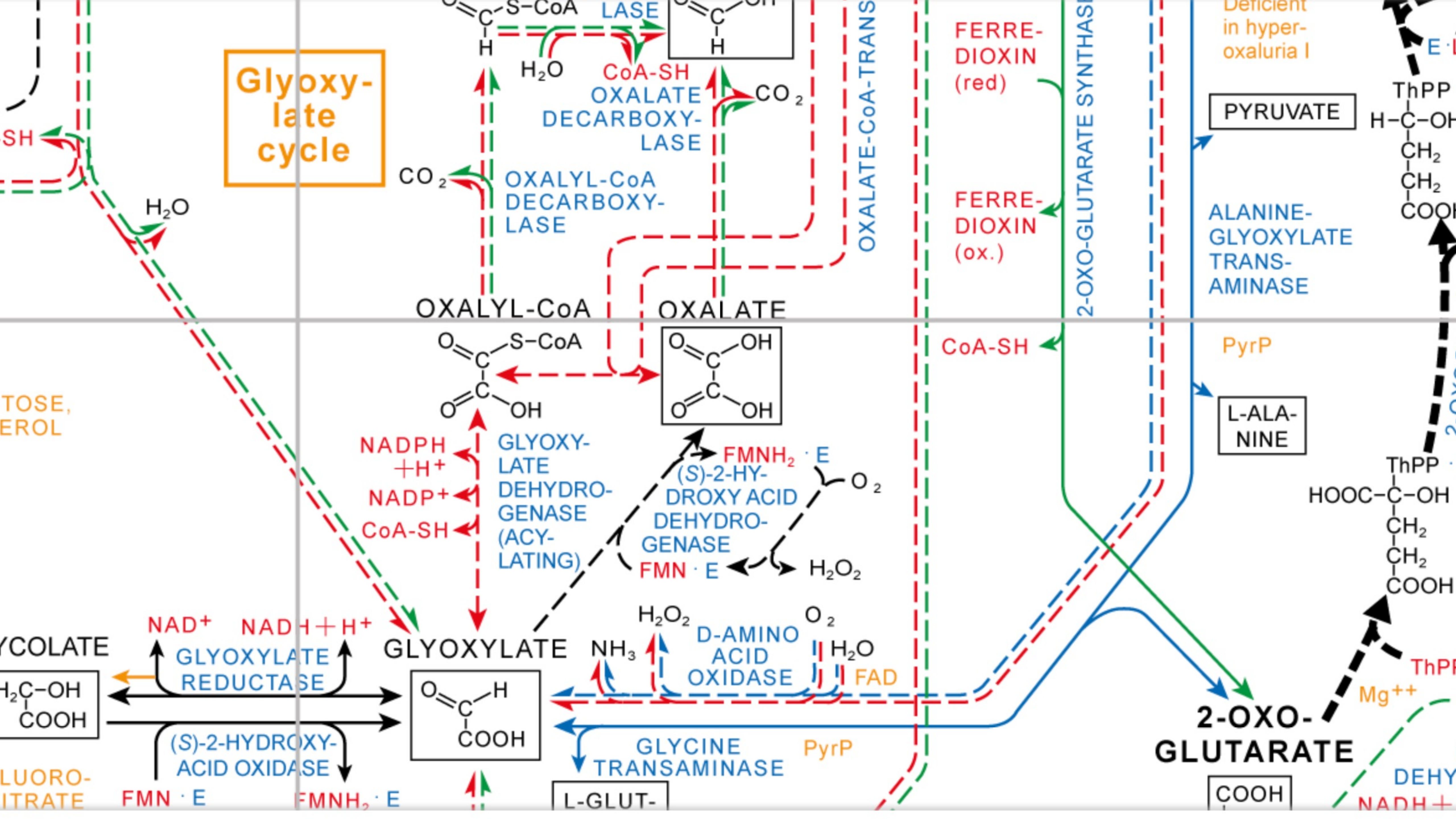


**A MULTIVARIATE NETWORK IS**  
**NETWORK TOPOLOGY +**  
**NODE AND EDGE ATTRIBUTES**

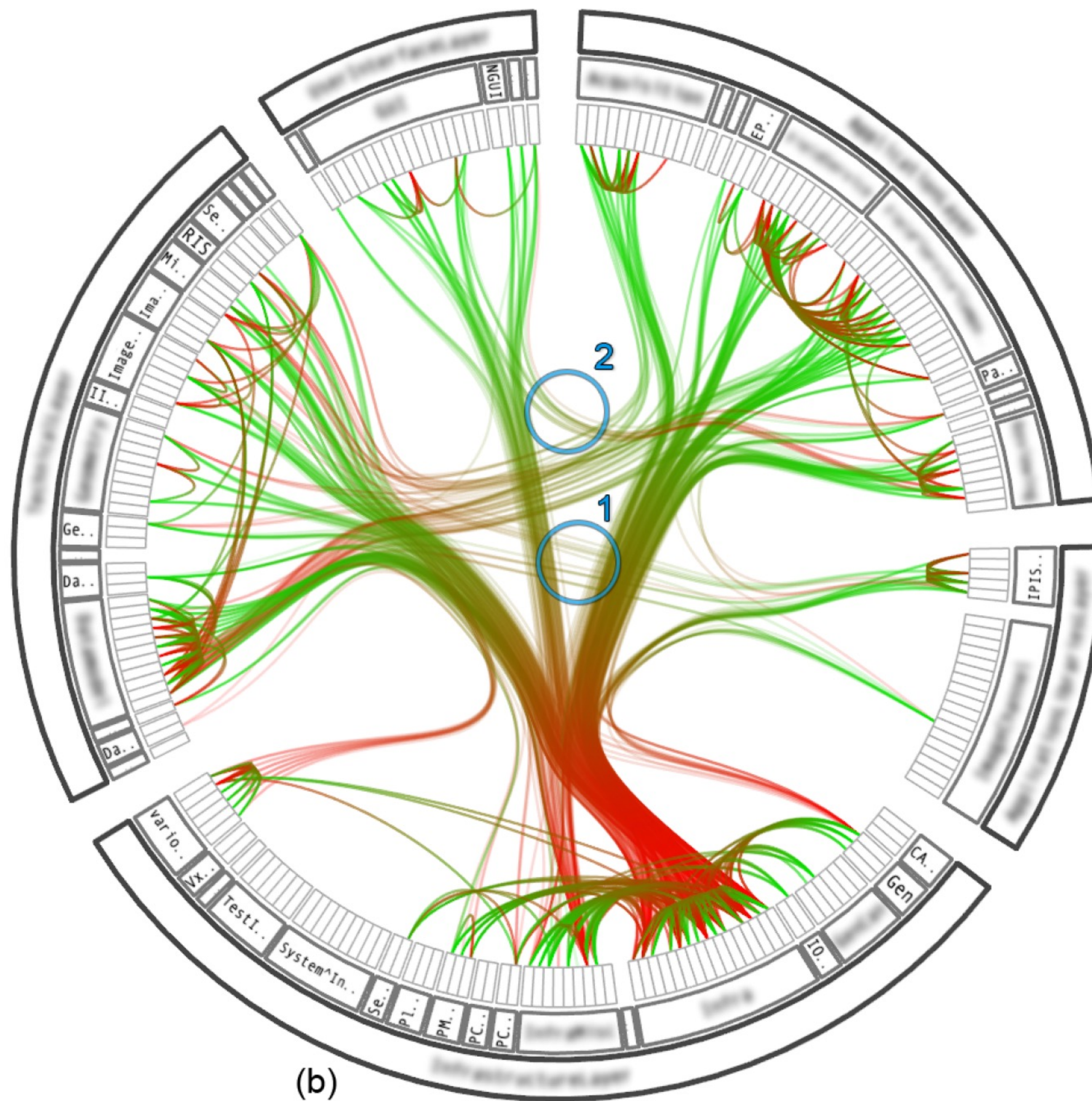












Holten and Wijk, 2009

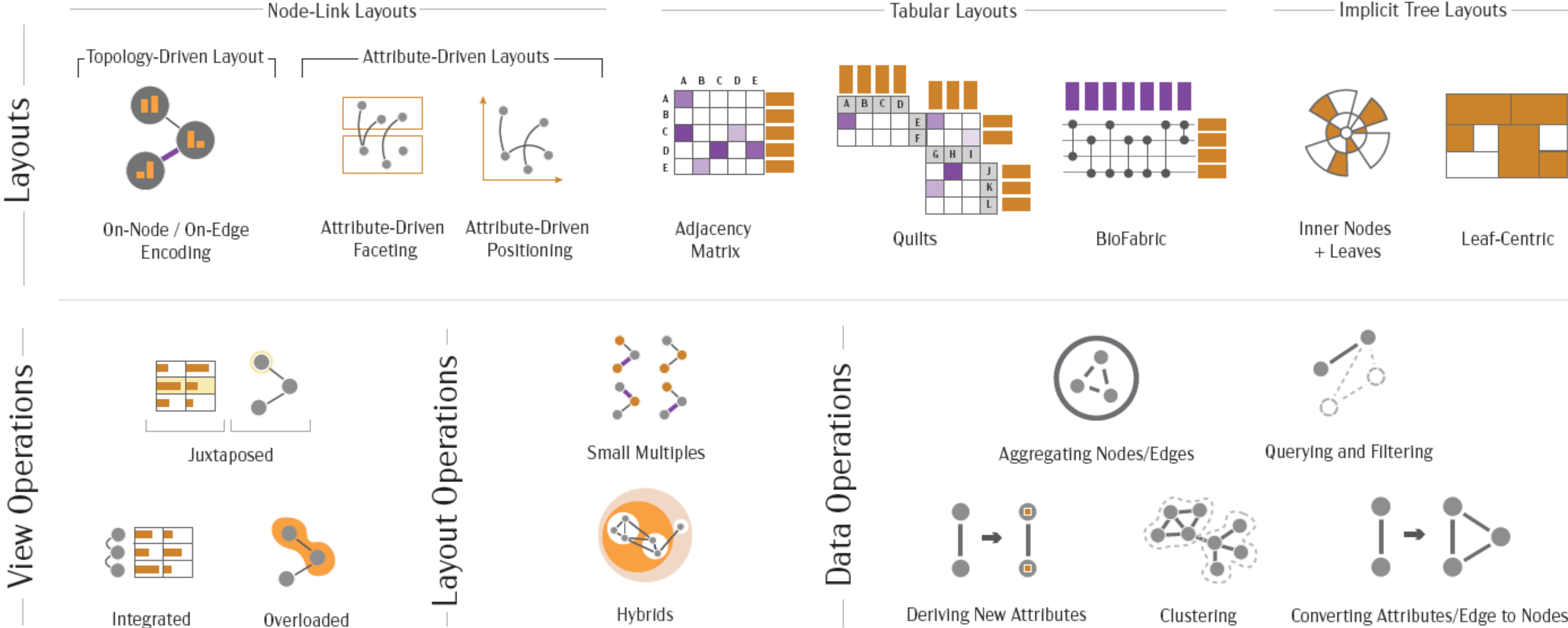


# The State of the Art in Visualizing Multivariate Networks

C. Nobre<sup>1</sup>, M. Meyer<sup>1</sup>, M. Streit<sup>2</sup>, and A. Lex<sup>1</sup>

<sup>1</sup>University of Utah, Utah, USA

<sup>2</sup>Johannes Kepler University Linz, Austria

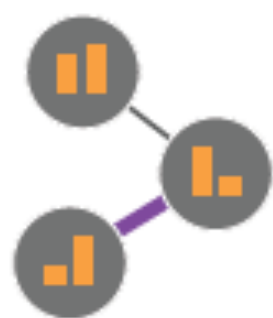




# Layouts

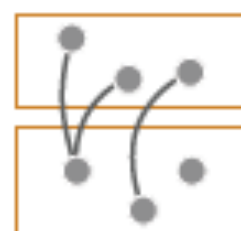
## Node-Link Layouts

### Topology-Driven Layout

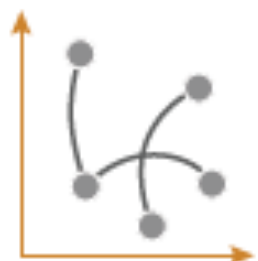


On-Node / On-Edge  
Encoding

### Attribute-Driven Layouts



Attribute-Driven  
Faceting

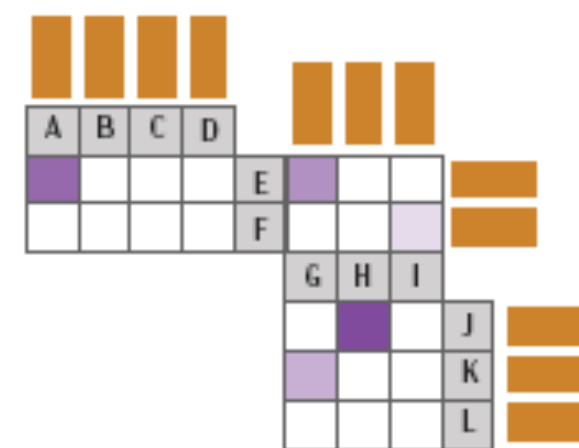


Attribute-Driven  
Positioning

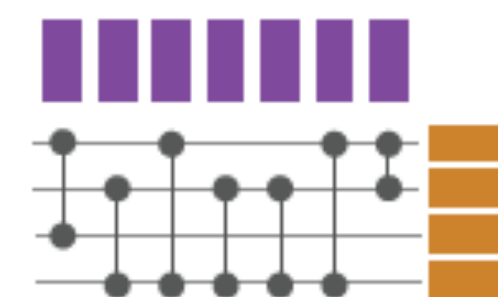
## Tabular Layouts



Adjacency  
Matrix



Quilts

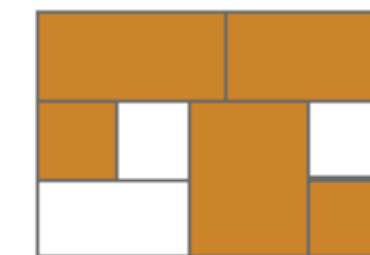


BioFabric

## Implicit Tree Layouts



Inner Nodes  
+ Leaves



Leaf-Centric

# View Operations



Juxtaposed

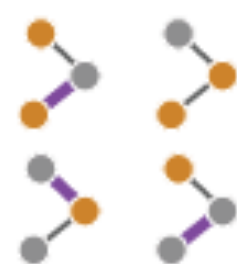


Integrated



Overloaded

# Layout Operations



Small Multiples



Hybrids

# Data Operations



Aggregating Nodes/Edges



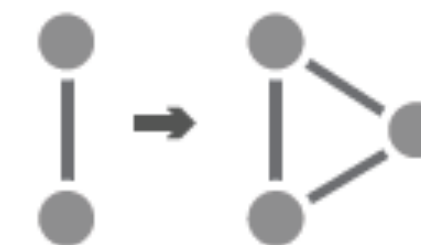
Deriving New Attributes



Clustering



Querying and Filtering



Converting Attributes/Edge to Nodes



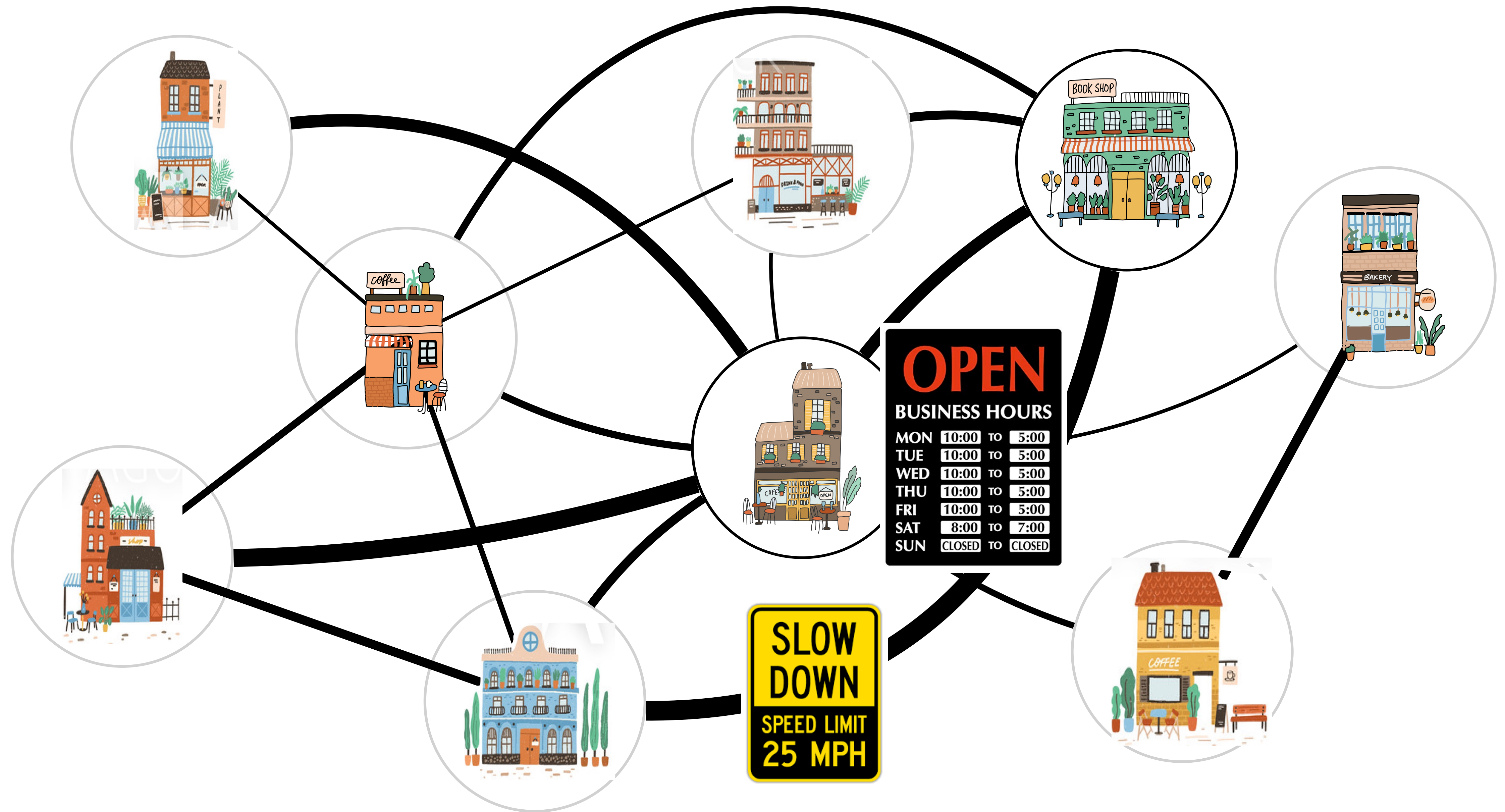
# MVNV Tasks



# How is an MVN task different than a regular graph task?

MVN Tasks rely on both the **topology** of the network and the **attributes** of the nodes and edges





What is an efficient way I can complete all my errands?



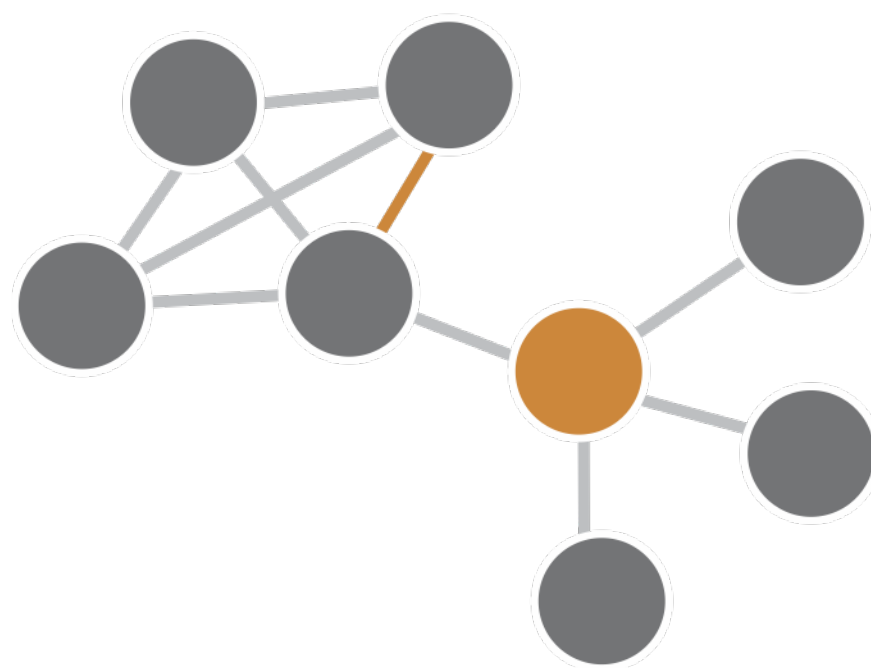
- 
- ▶ What is the **fastest route** to get all my errands done?

Tasks that rely on the **topology** of the network  
and the **attributes** of the nodes and edges

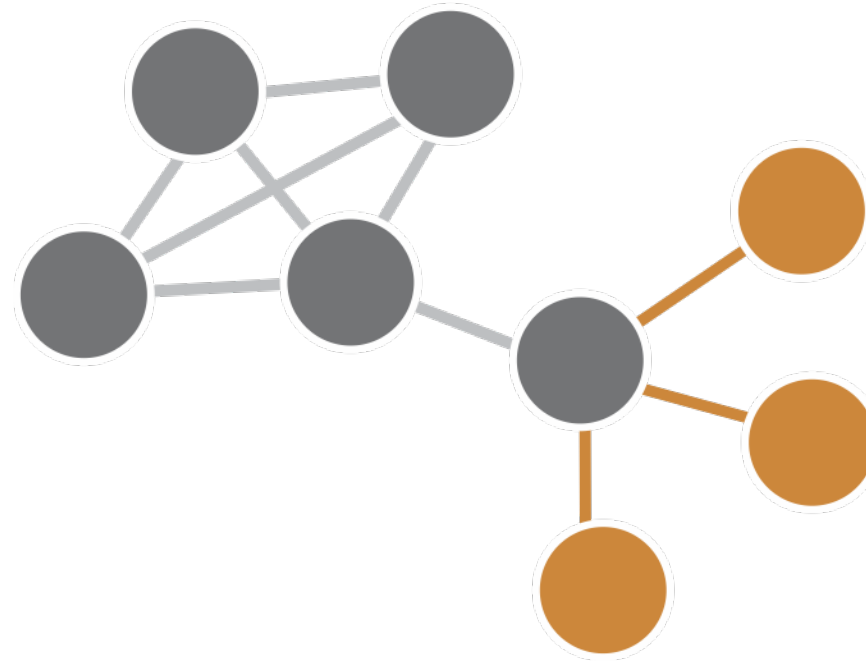


# MVNV tasks are applied to topological structures

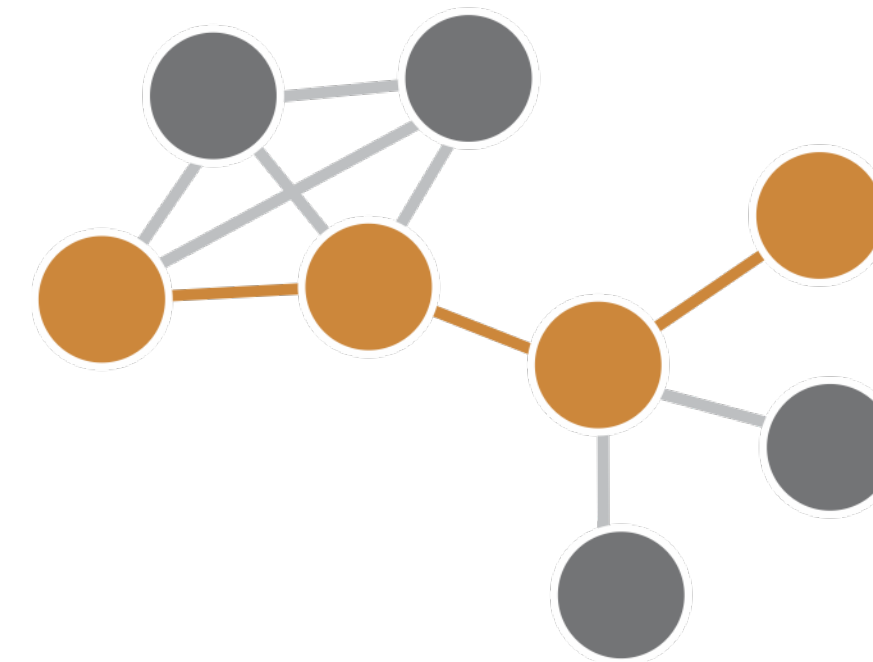
Single Node/Edge



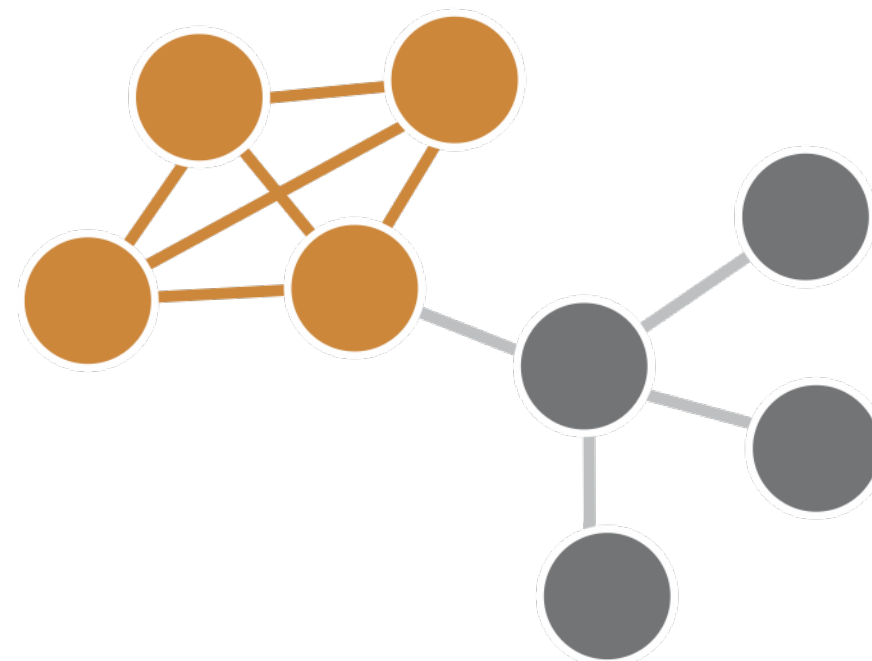
Node Neighbors



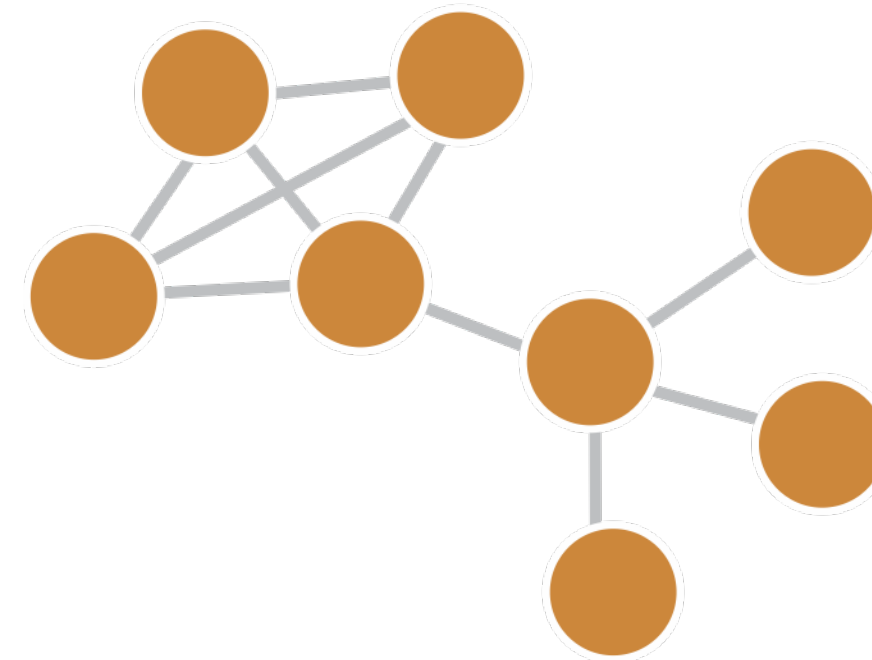
Path



Cluster



Network/Subnetwork

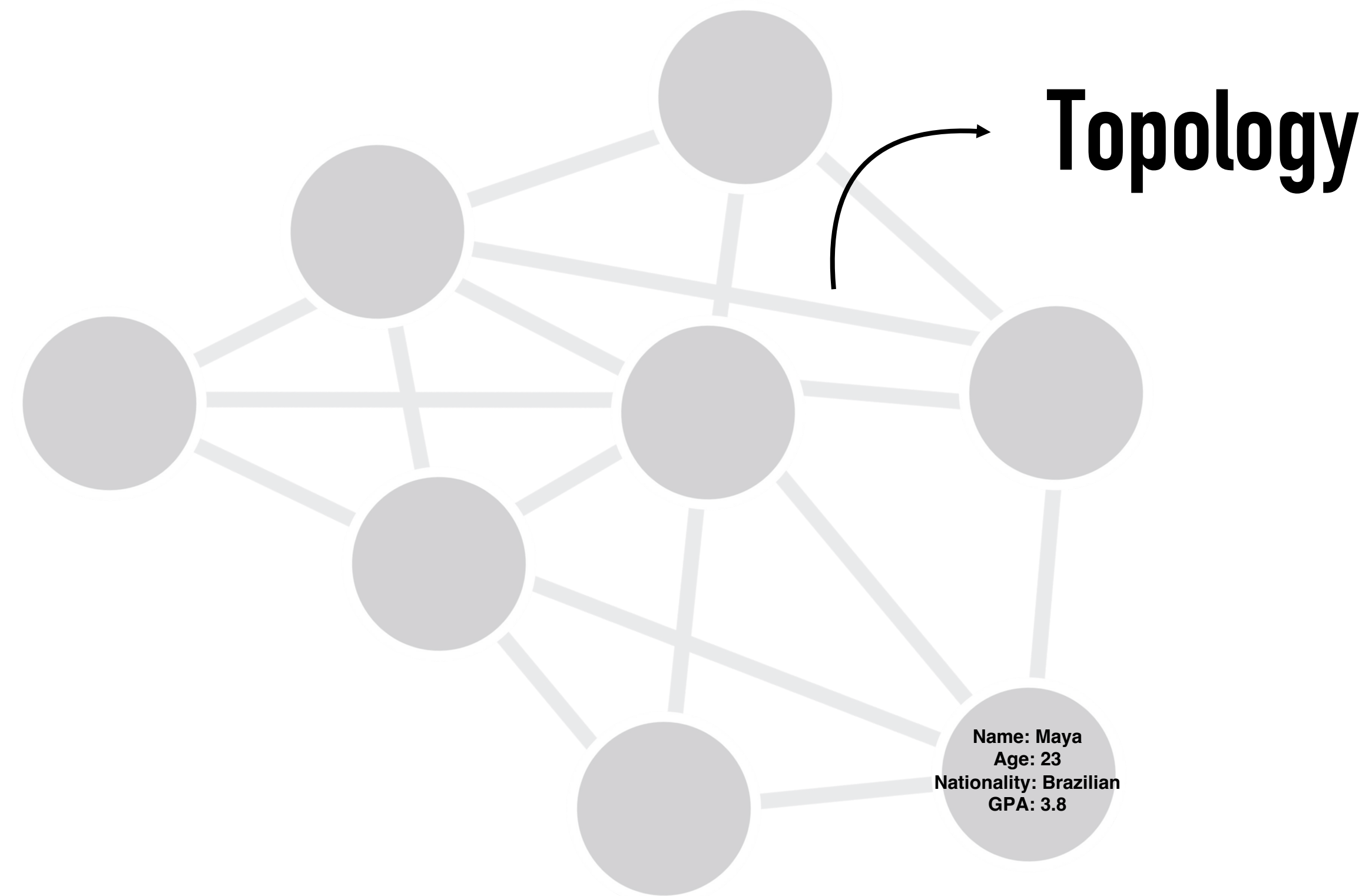




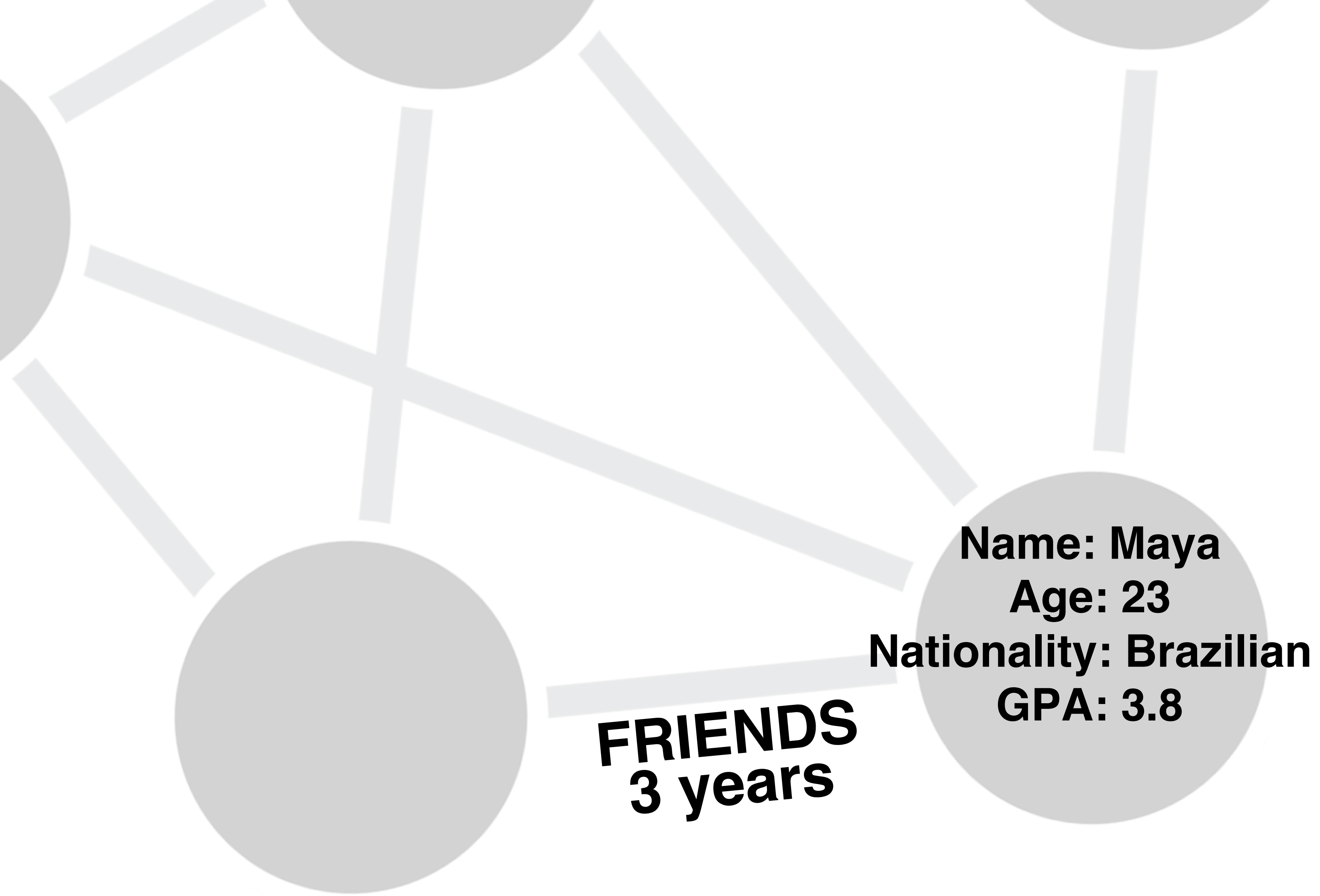


# Network and Attribute Characteristics

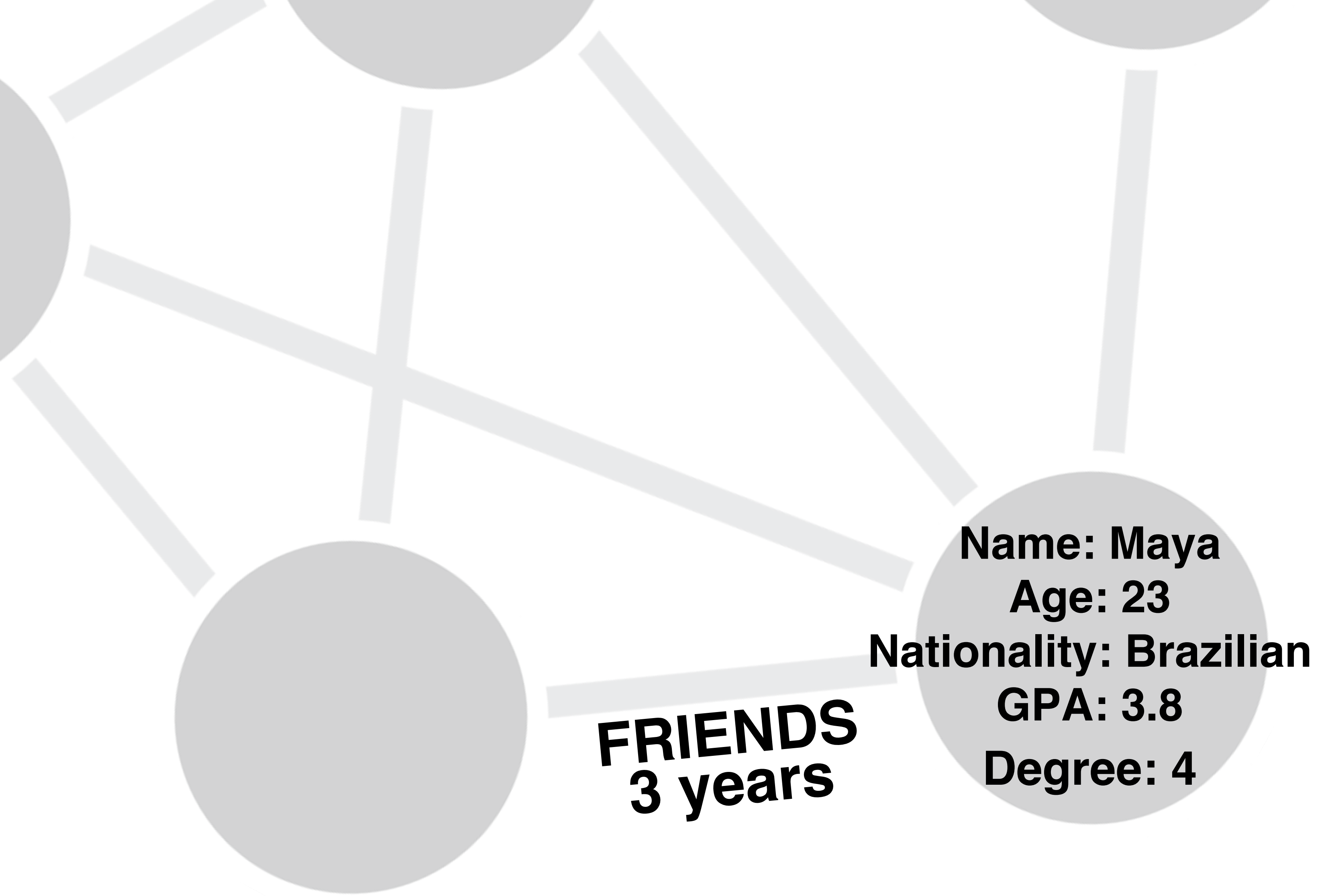




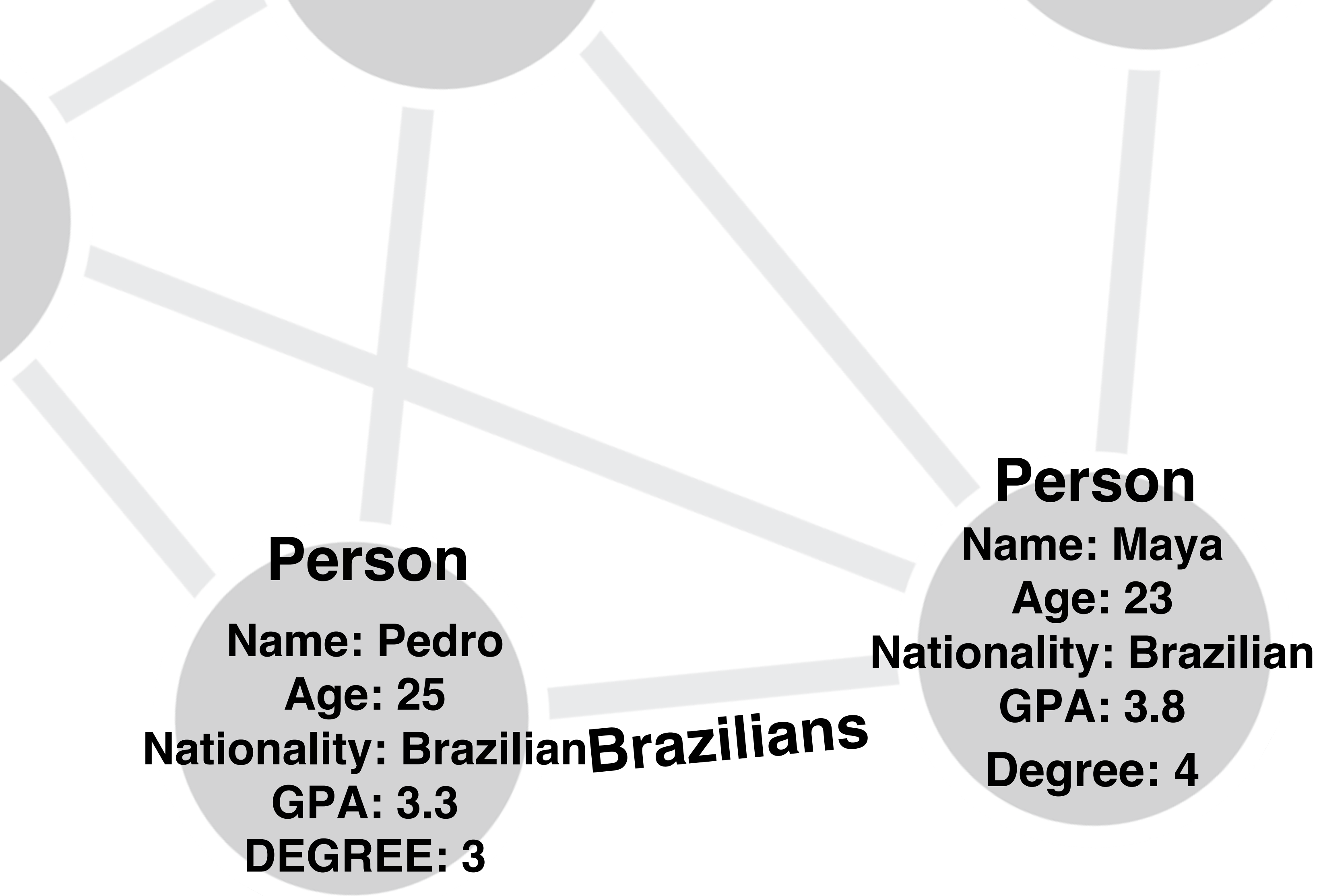






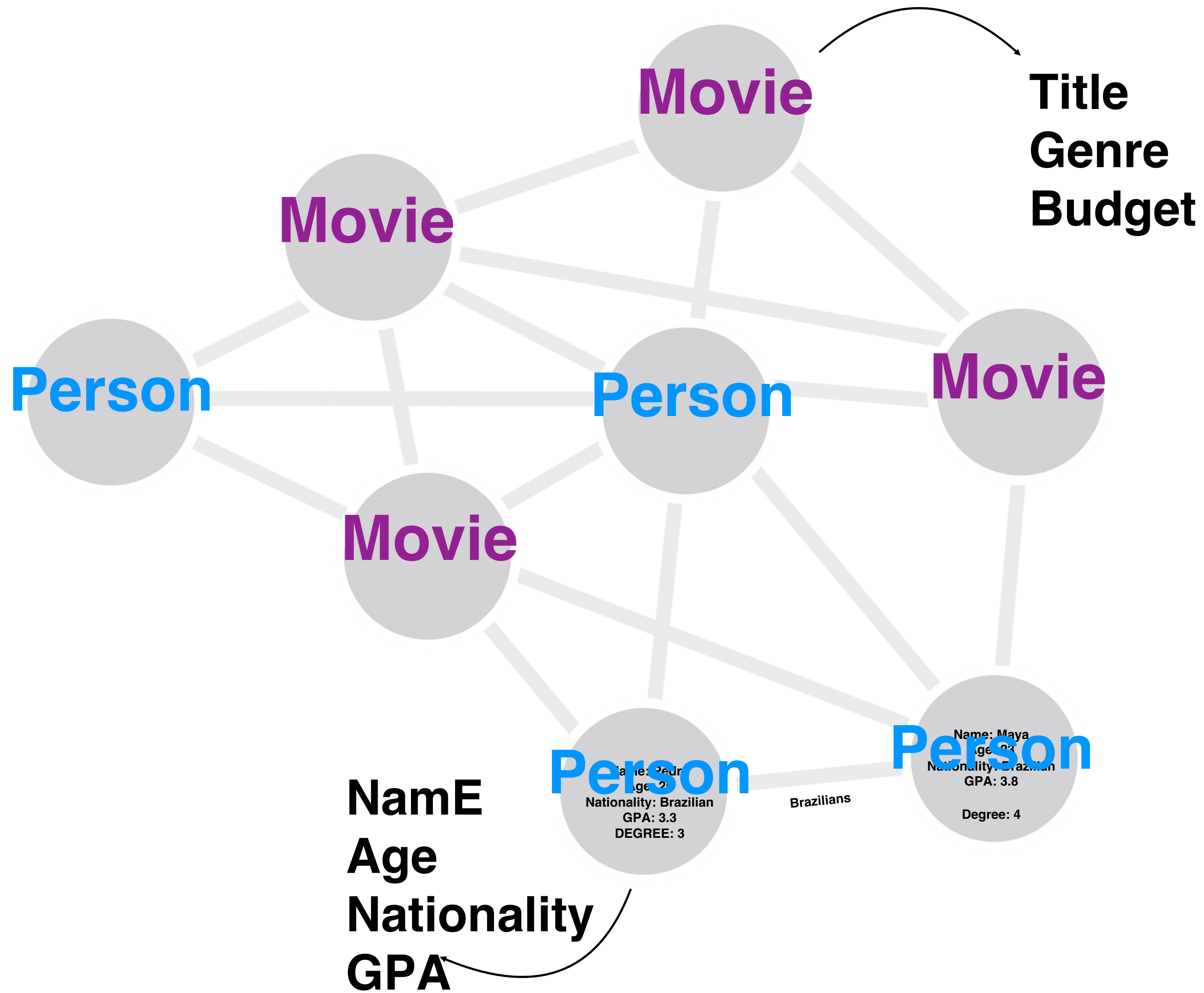




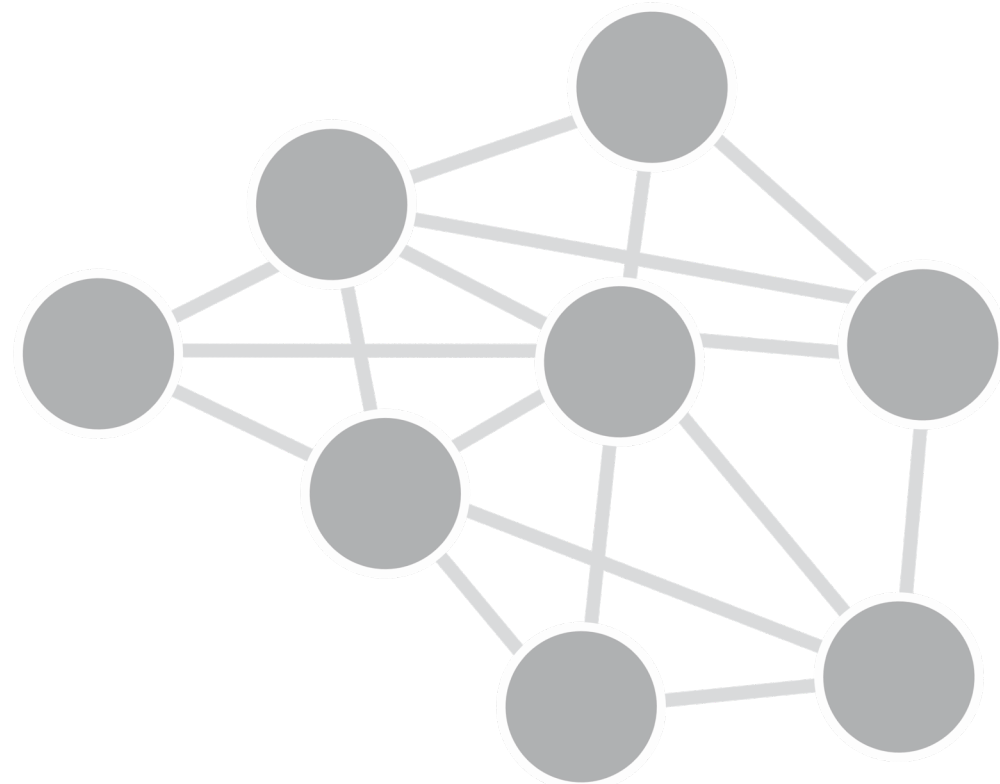


ity

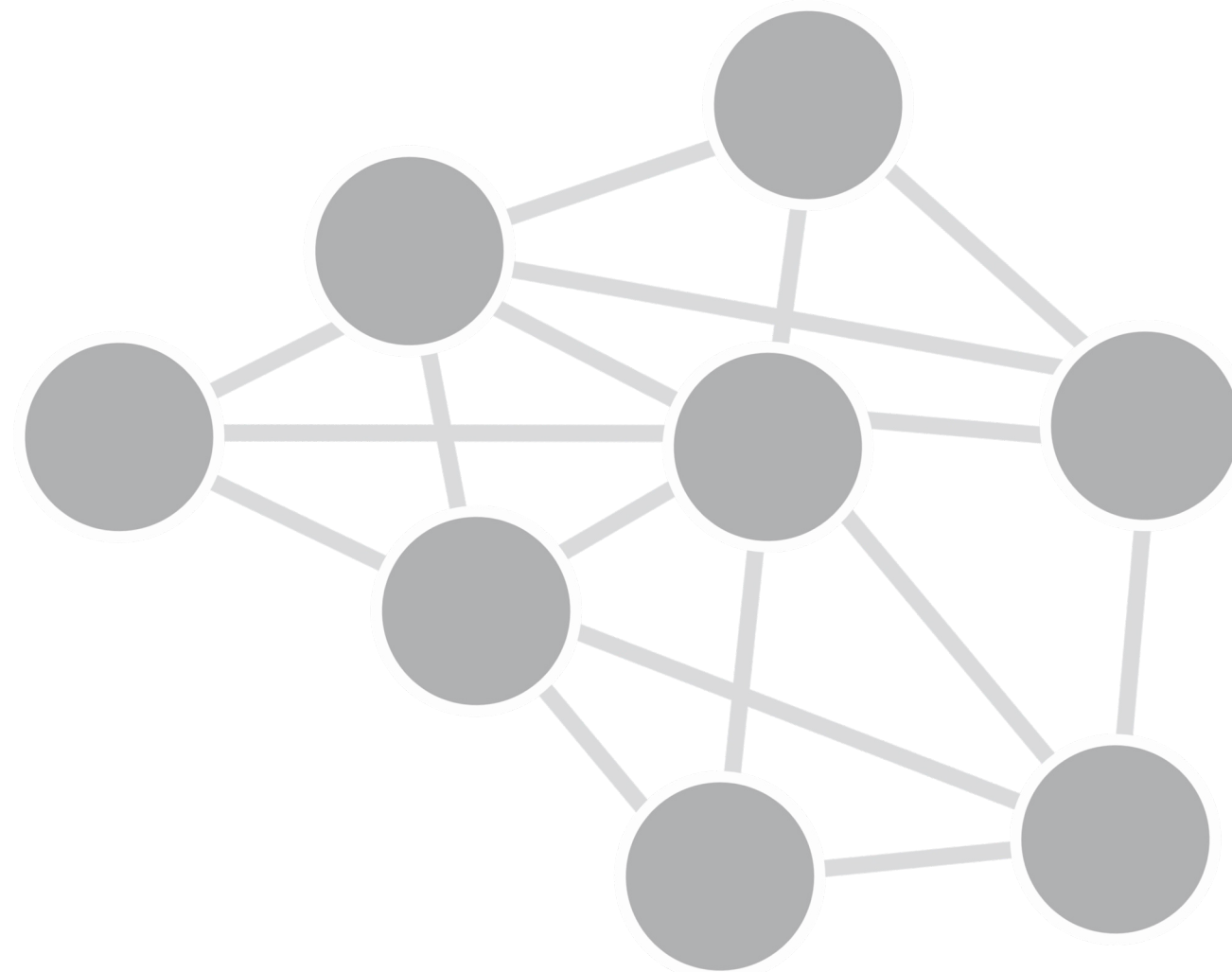




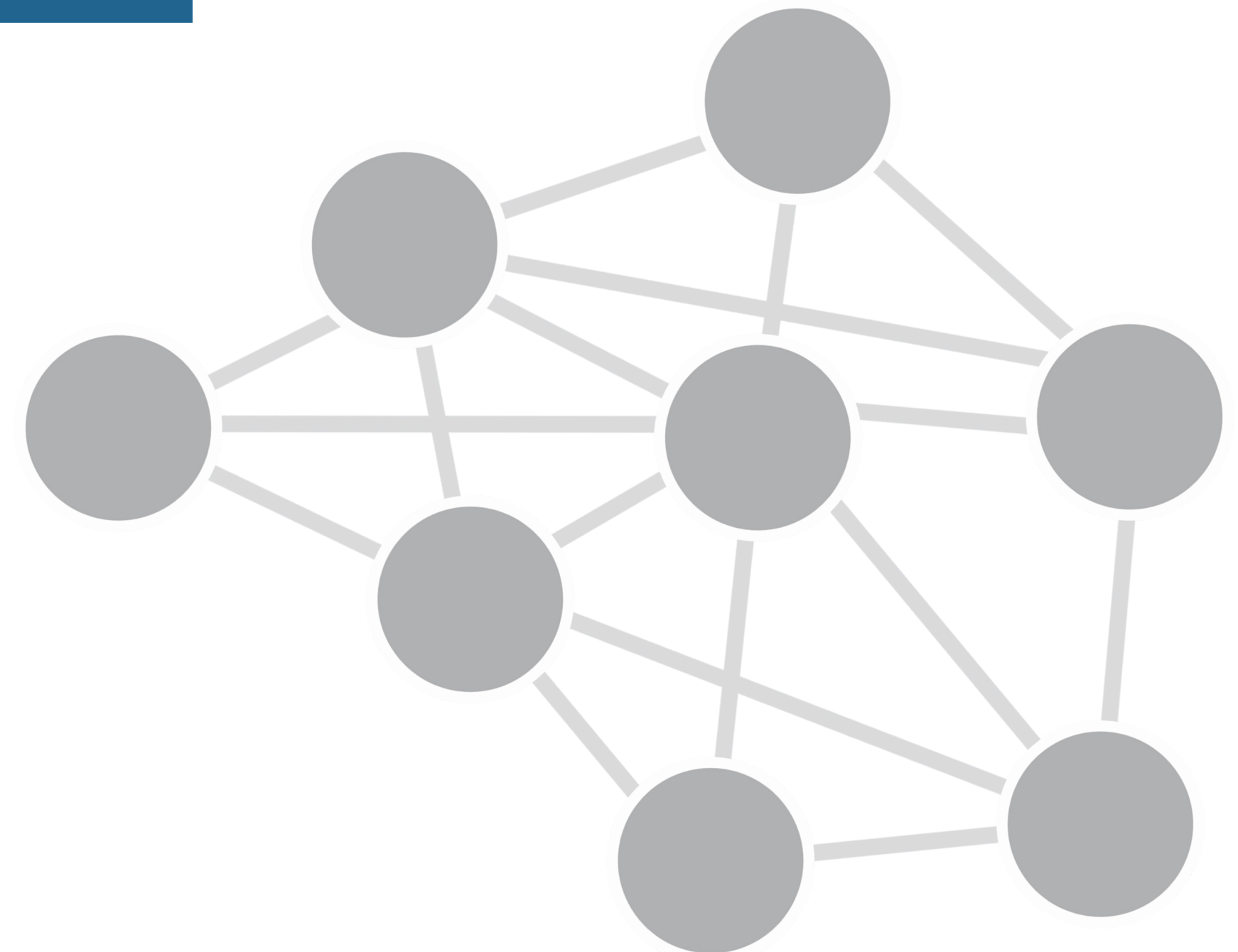
# Network Size



**Small**  
**<100**



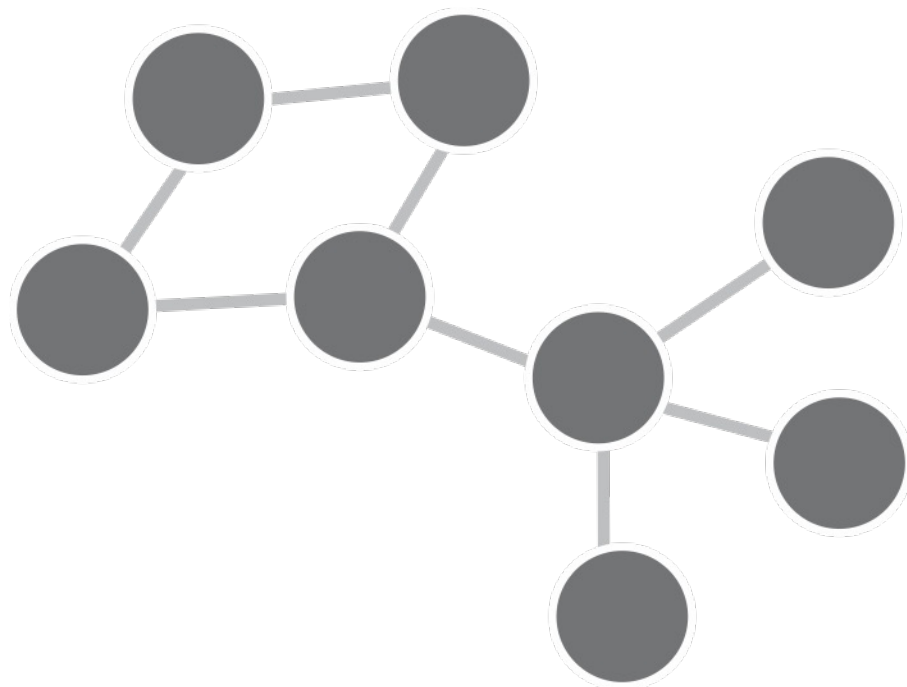
**Medium**  
**100–1000**



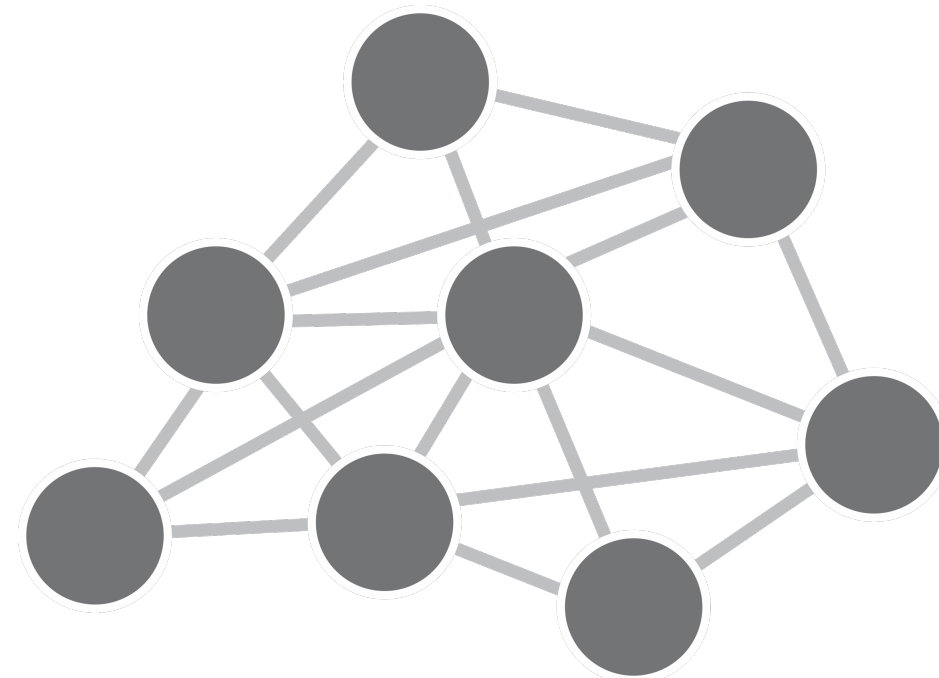
**Large**  
**>1000**



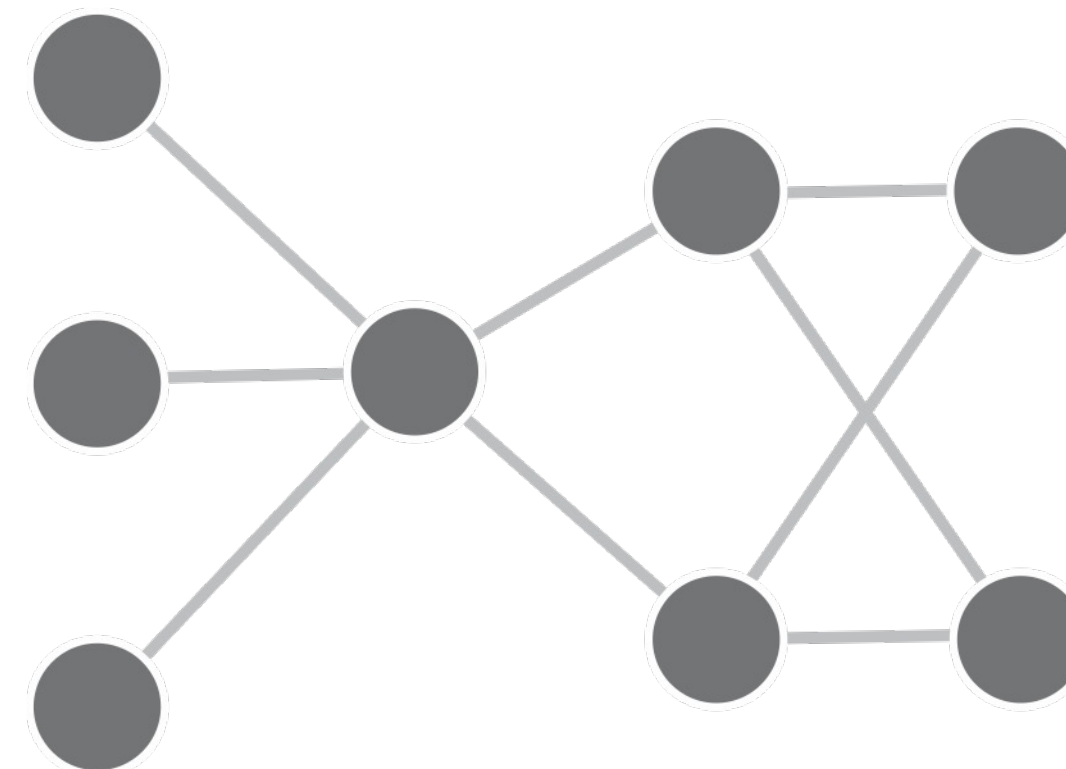
# Network Types



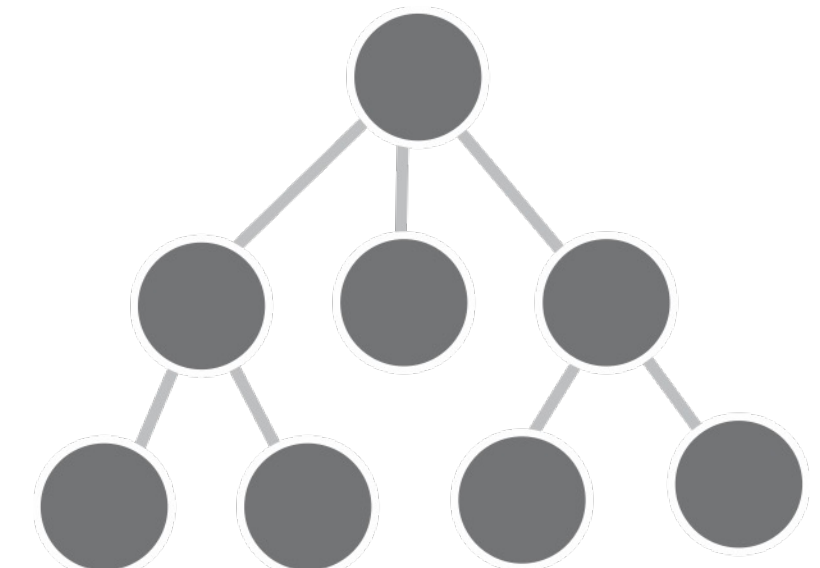
**Sparse**



**Dense**



**Layered**



**Trees**

## Node-Link Layouts

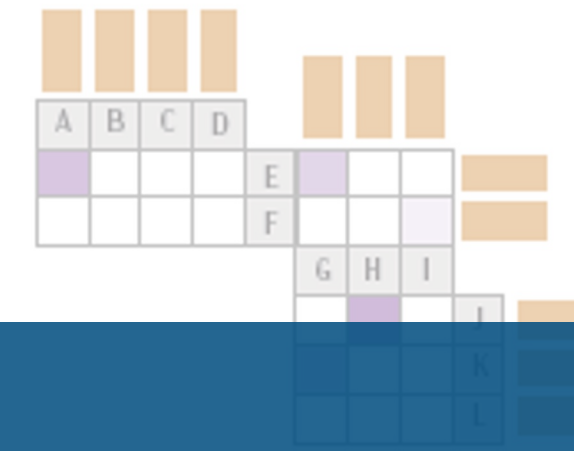
## Topology-Driven Layout

On-Node / On-Edge  
Encoding

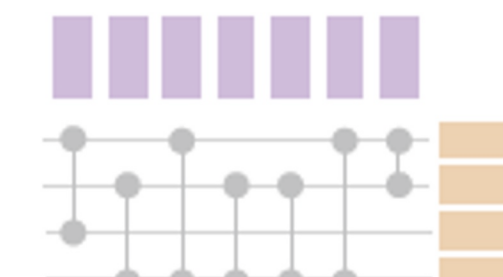
## Attribute-Driven Layouts

Attribute-Driven  
FacetingAttribute-Driven  
Positioning

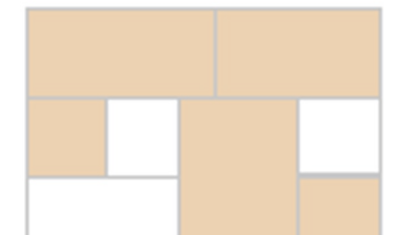
## Tabular Layouts

Adjacency  
Matrix

Quilts



BioFabric

Inner Nodes  
+ Leaves

Leaf-Centric

# Taxonomy of Layouts and Operations

## Juxtaposed



Integrated



Overloaded

## Small Multiples



Hybrids

## Aggregating Nodes/Edges

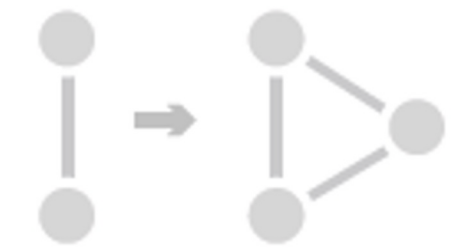


Deriving New Attributes



Clustering

## Querying and Filtering



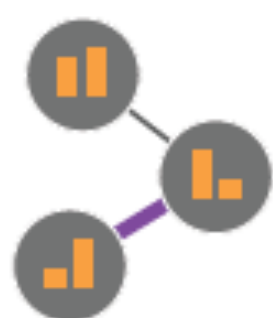
Converting Attributes/Edge to Nodes



# Layouts

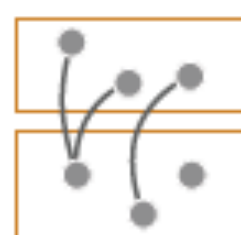
## Node-Link Layouts

### Topology-Driven Layout

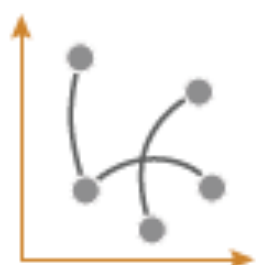


On-Node / On-Edge  
Encoding

### Attribute-Driven Layouts



Attribute-Driven  
Faceting

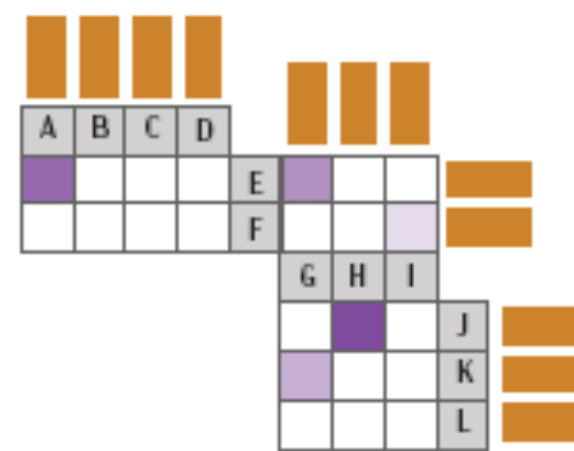


Attribute-Driven  
Positioning

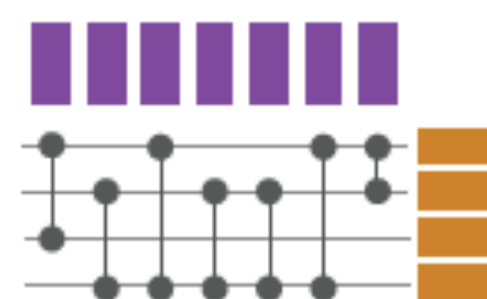
## Tabular Layouts



Adjacency  
Matrix



Quilts

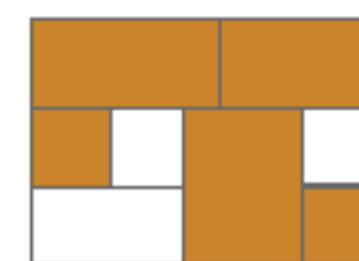


BioFabric

## Implicit Tree Layouts



Inner Nodes  
+ Leaves



Leaf-Centric

# View Operations



Juxtaposed

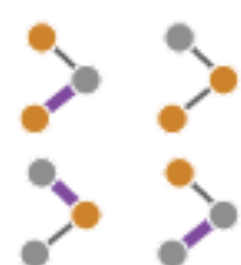


Integrated



Overloaded

# Layout Operations



Small Multiples



Hybrids

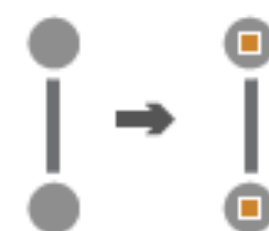
# Data Operations



Aggregating Nodes/Edges



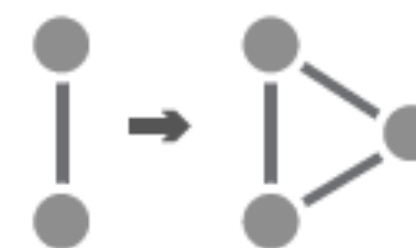
Querying and Filtering



Deriving New Attributes



Clustering

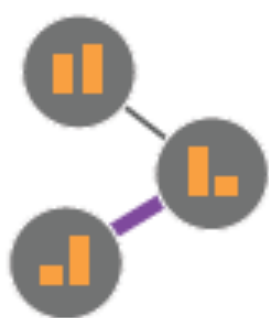


Converting Attributes/Edge to Nodes

# Layouts

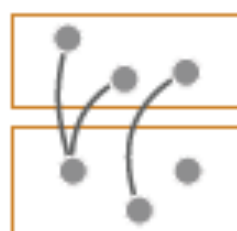
## Node-Link Layouts

### Topology-Driven Layout

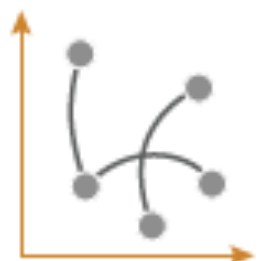


On-Node / On-Edge  
Encoding

### Attribute-Driven Layouts



Attribute-Driven  
Faceting

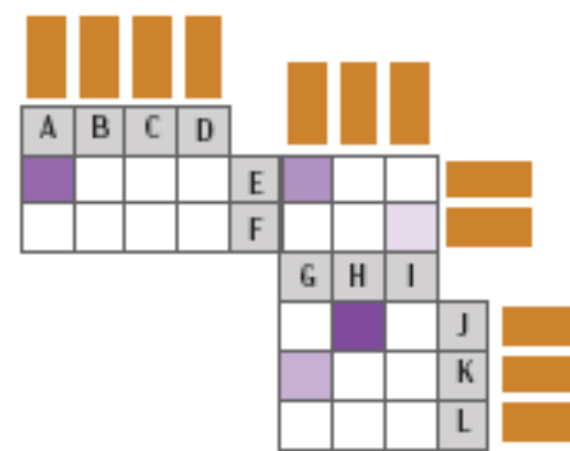


Attribute-Driven  
Positioning

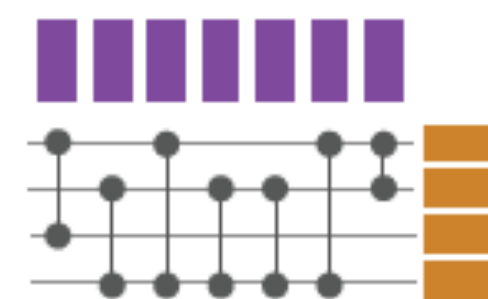
## Tabular Layouts



Adjacency  
Matrix



Quilts

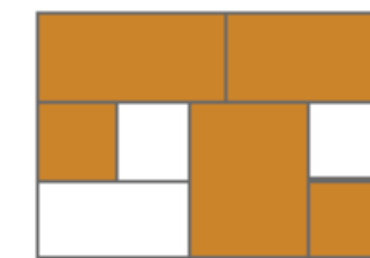


BioFabric

## Implicit Tree Layouts

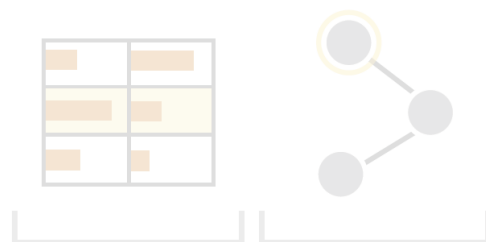


Inner Nodes  
+ Leaves

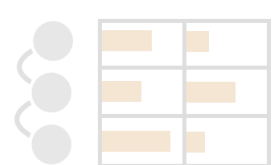


Leaf-Centric

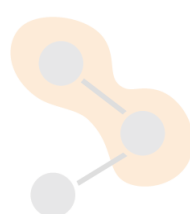
# View Operations



Juxtaposed

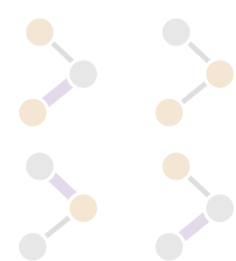


Integrated

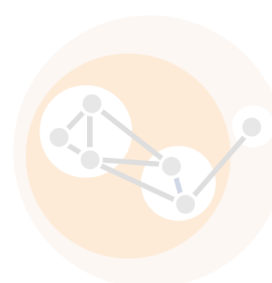


Overloaded

# Layout Operations



Small Multiples



Hybrids

# Data Operations



Aggregating Nodes/Edges



Deriving New Attributes



Clustering



Querying and Filtering



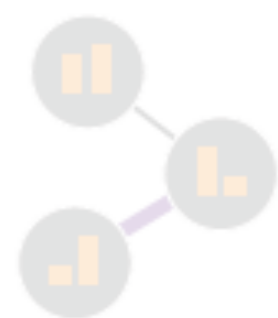
Converting Attributes/Edge to Nodes



# Layouts

## Node-Link Layouts

### Topology-Driven Layout



On-Node / On-Edge  
Encoding

### Attribute-Driven Layouts



Attribute-Driven  
Faceting

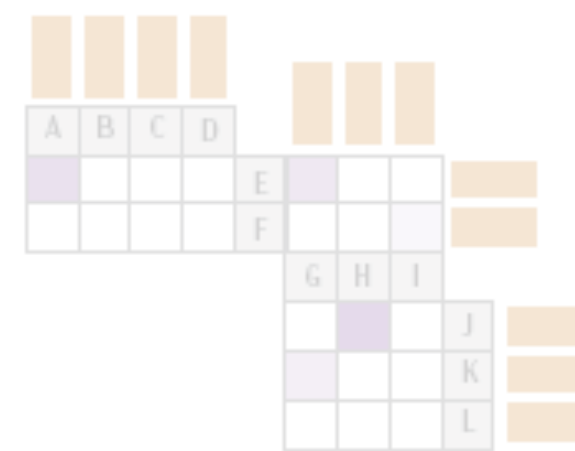


Attribute-Driven  
Positioning

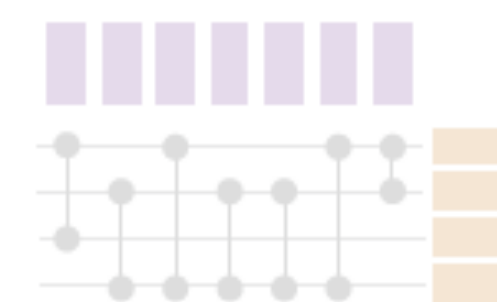
## Tabular Layouts



Adjacency  
Matrix



Quilts

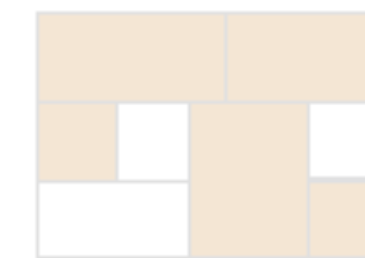


BioFabric

## Implicit Tree Layouts

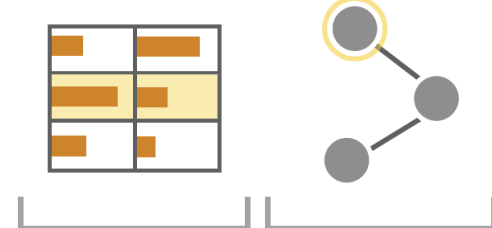


Inner Nodes  
+ Leaves



Leaf-Centric

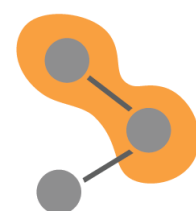
# View Operations



Juxtaposed

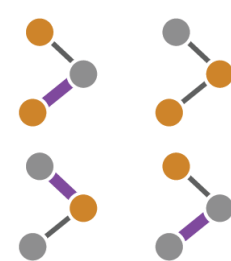


Integrated



Overloaded

# Layout Operations



Small Multiples



Hybrids

# Data Operations



Aggregating Nodes/Edges



Querying and Filtering



Deriving New Attributes

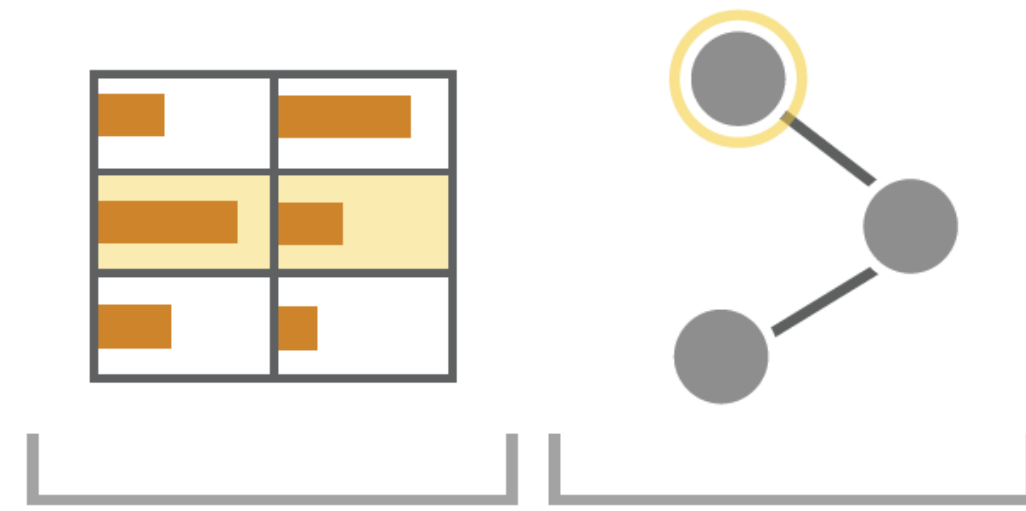


Clustering

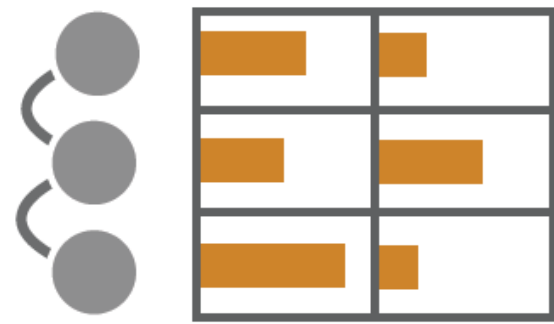


Converting Attributes/Edge to Nodes

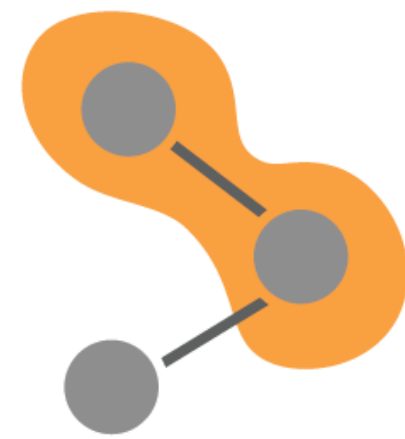
# View Operations



Juxtaposed



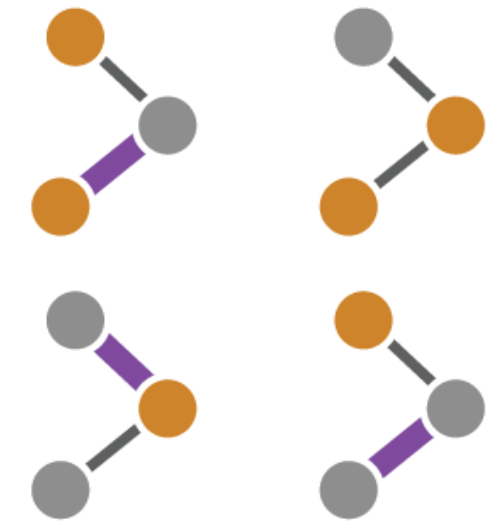
Integrated



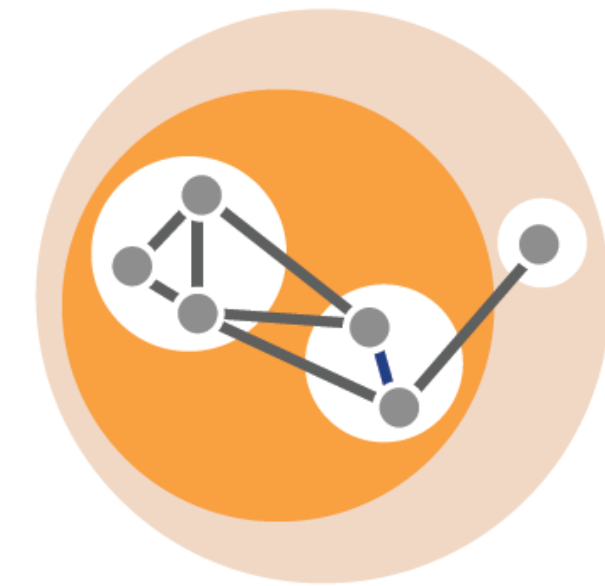
Overloaded

**Separate views for  
Topology and Attributes**

# Layout Operations



Small Multiples



Hybrids

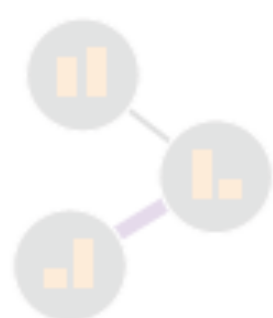
**Multiple layouts for  
Topology or Attributes**



# Layouts

## Node-Link Layouts

### Topology-Driven Layout



On-Node / On-Edge  
Encoding

### Attribute-Driven Layouts



Attribute-Driven  
Faceting

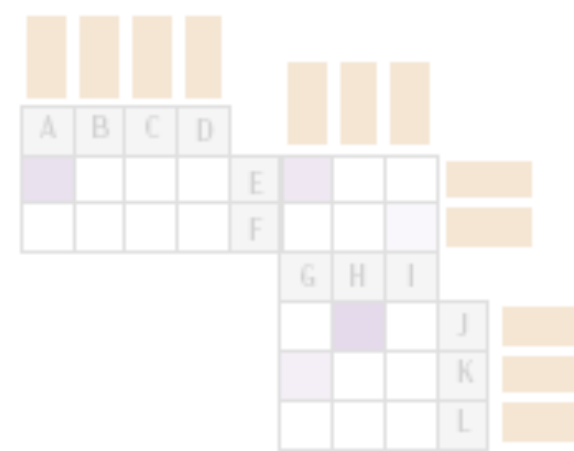


Attribute-Driven  
Positioning

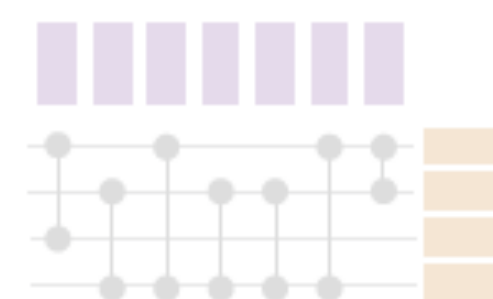
## Tabular Layouts



Adjacency  
Matrix



Quilts

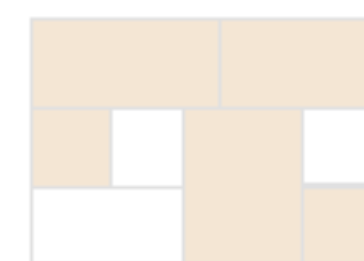


BioFabric

## Implicit Tree Layouts



Inner Nodes  
+ Leaves



Leaf-Centric

# View Operations



Juxtaposed



Integrated



Overloaded

## Layout Operations



Small Multiples



Hybrids

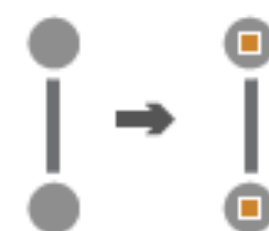
# Data Operations



Aggregating Nodes/Edges



Querying and Filtering



Deriving New Attributes



Clustering



Converting Attributes/Edge to Nodes

		Size			Type				Node Attributes				Edge Attributes				Topolog. Structures					
			Small (<100 nodes)	Medium (<1,000)	Large (>1,000 nodes)	Complex (sparse)	Complex (dense)	Layered/K-Partite	Trees	Few (<5)	Several (≥5)	Homog. (1 type)	Hetero. (>1 type)	Few (<3)	Several (≥3)	Homog. (1 type)	Hetero. (>1 type)	Single node/edge	Neighbors	Paths	Clusters	Entire/sub network
Node-Link Layouts	On-node/edge encoding		3	2	1	3	1	3	3	2	1	3	2	2	1	3	1	3	3	2	2	2
	Attr.-driven faceting		3	1	1	3	1	3	1	3	1	3	3	2	1	2	1	3	2	1	1	1
	Attr.-driven positioning		3	1	1	3	1	1	1	3	1	3	1	2	1	2	1	3	2	1	1	2
Tabular Layouts	Adjacency matrix		3	1	1	2	3	2	1	2	3	3	2	3	2	3	2	3	3	1	3	2
	Quilts		3	1	1	3	1	3	3	3	3	3	3	3	3	3	2	3	3	2	2	2
	BioFabric		3	1	1	3	3	2	1	3	3	3	3	3	3	3	3	3	1	1	1	2
Implicit	Inner nodes & leaves		3	2	1	0	0	0	3	3	1	3	1	0	0	0	0	3	3	3	0	3
	Leaves		3	2	2	0	0	0	3	3	1	3	1	0	0	0	0	3	2	1	0	3
View Operations	Juxtaposed		3	2	1	3	1	3	3	3	3	3	3	3	3	3	3	2	1	1	2	2
	Integrated		3	2	1	3	1	3	3	3	3	3	3	2	2	3	3	3	3	3	1	2
	Overloaded		3	2	1	3	1	3	3	3	1	3	1	1	1	1	1	3	3	2	3	2

0

Does \*not\* support

1

Supports poorly

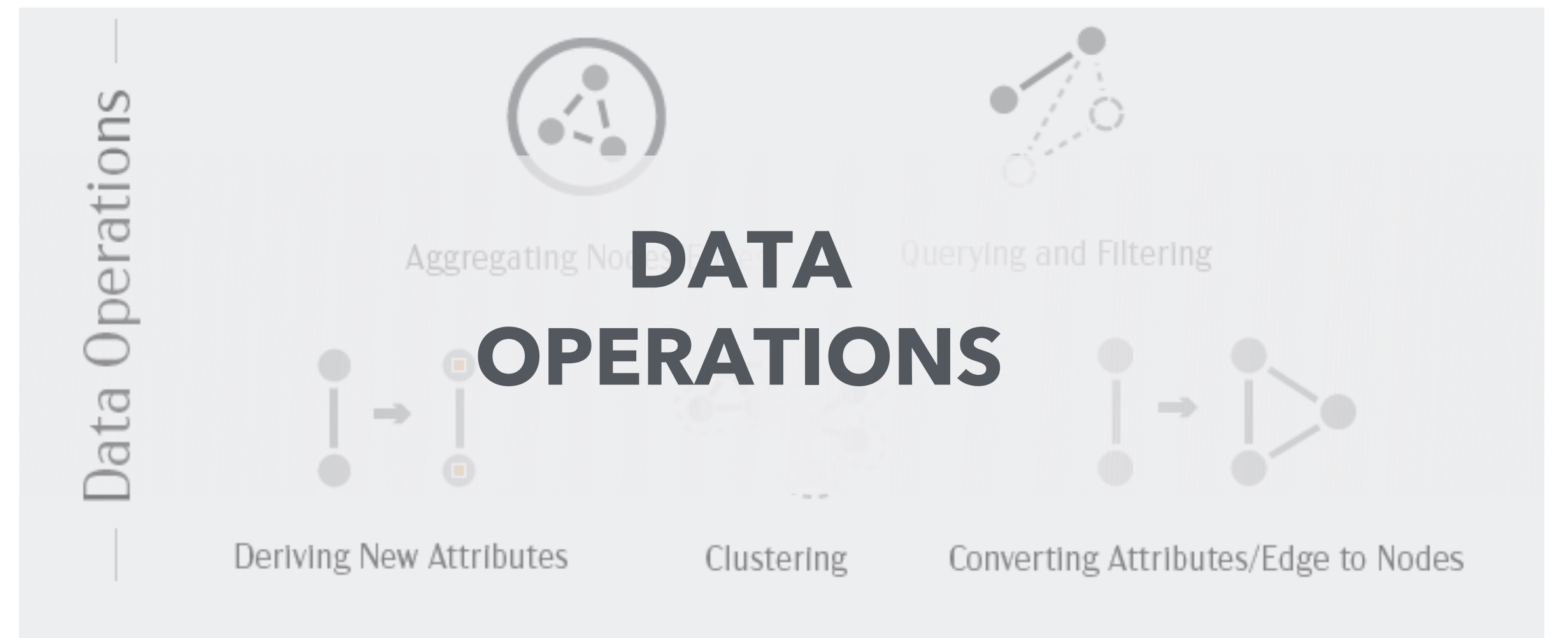
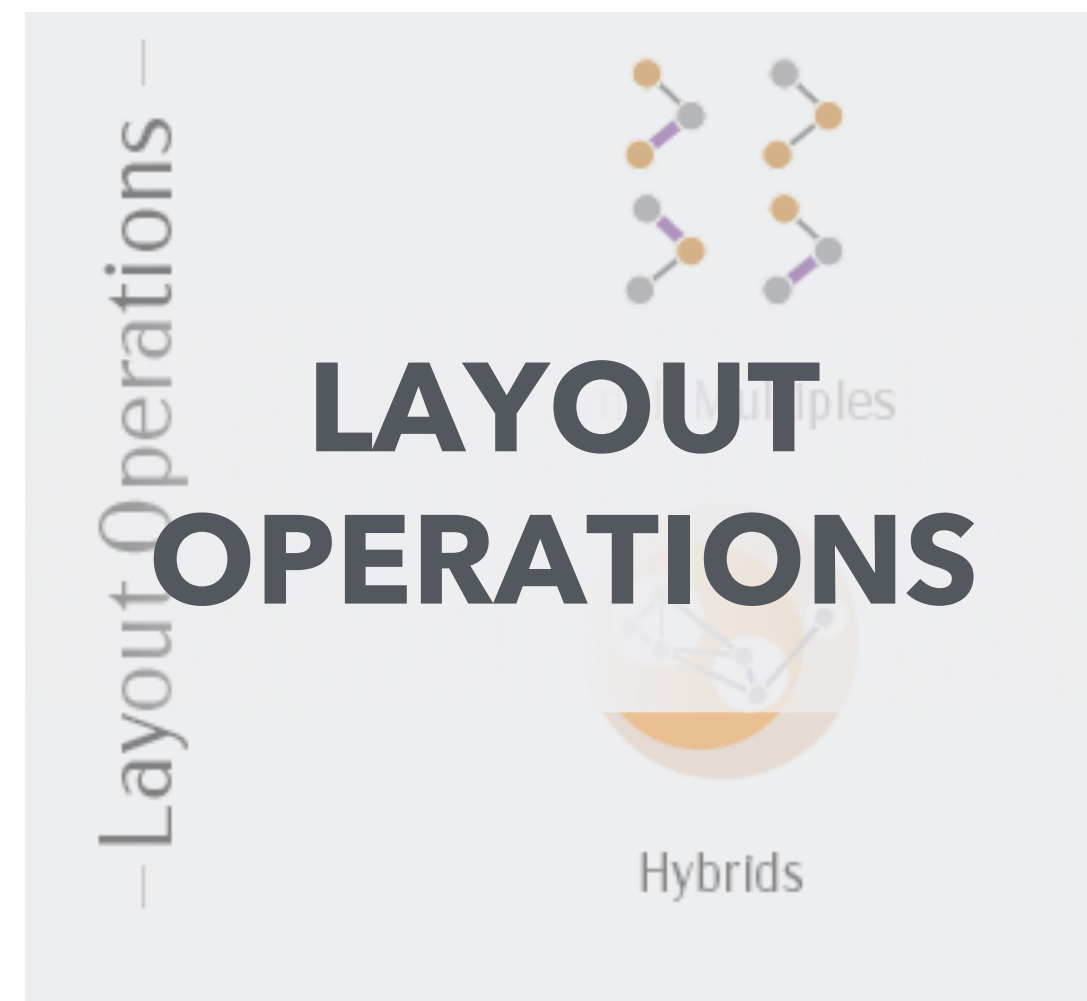
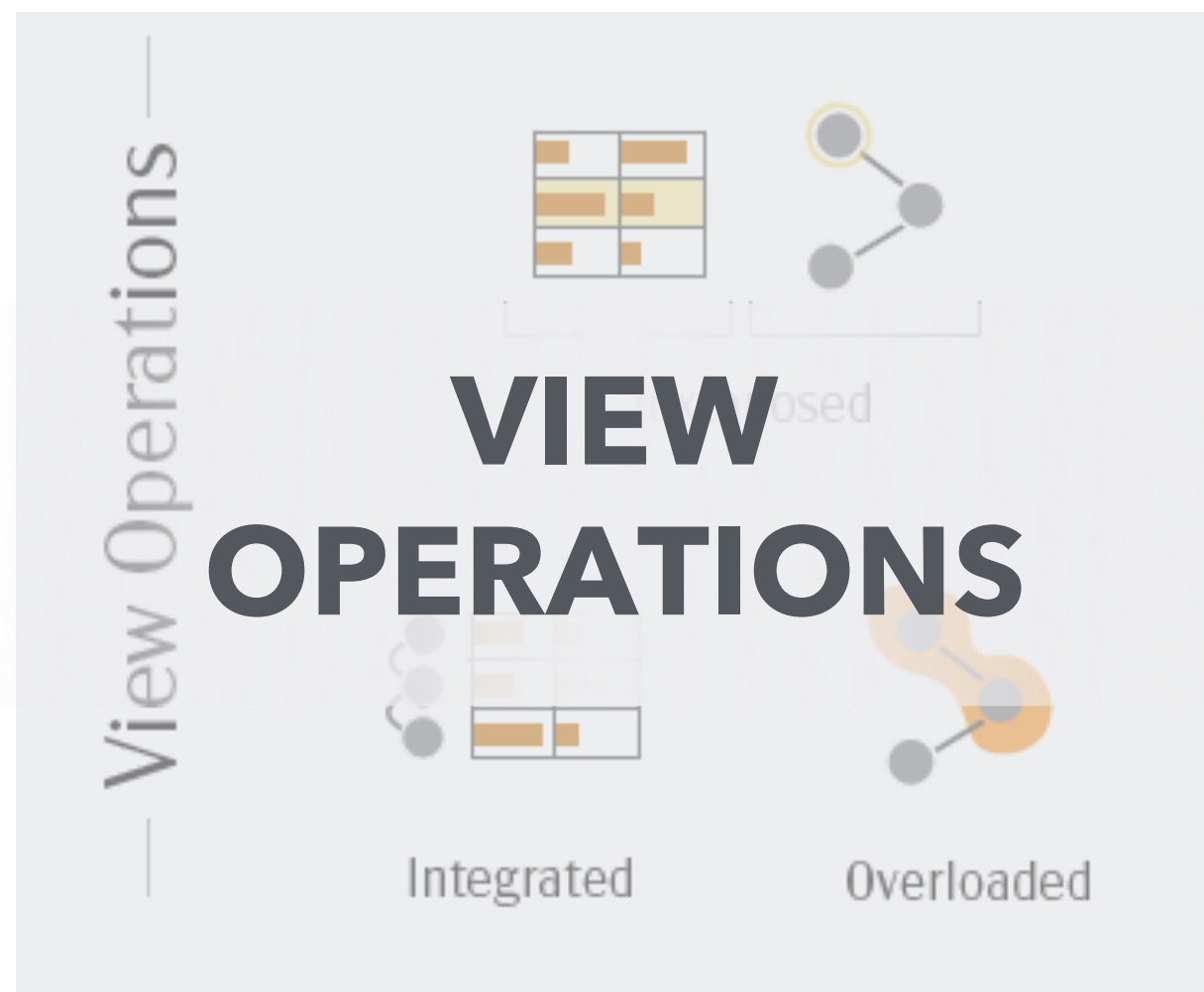
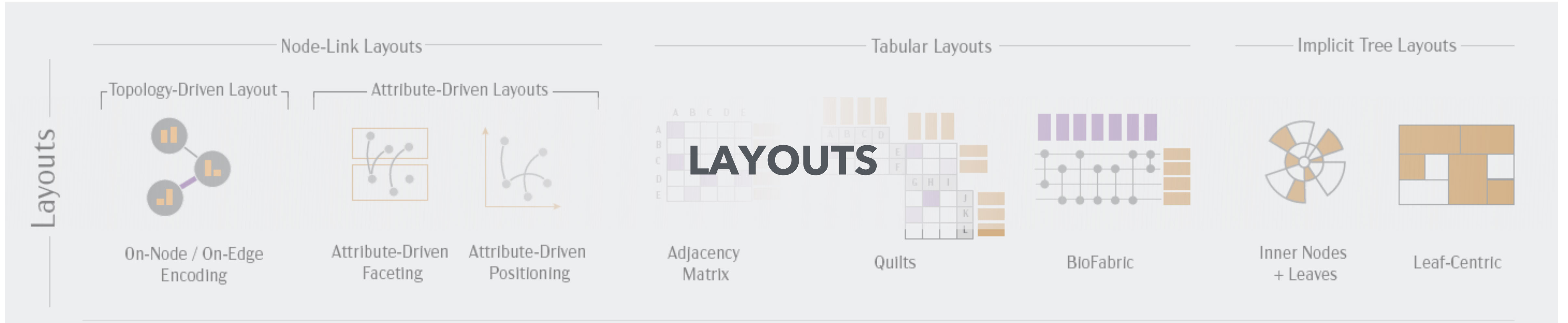
2

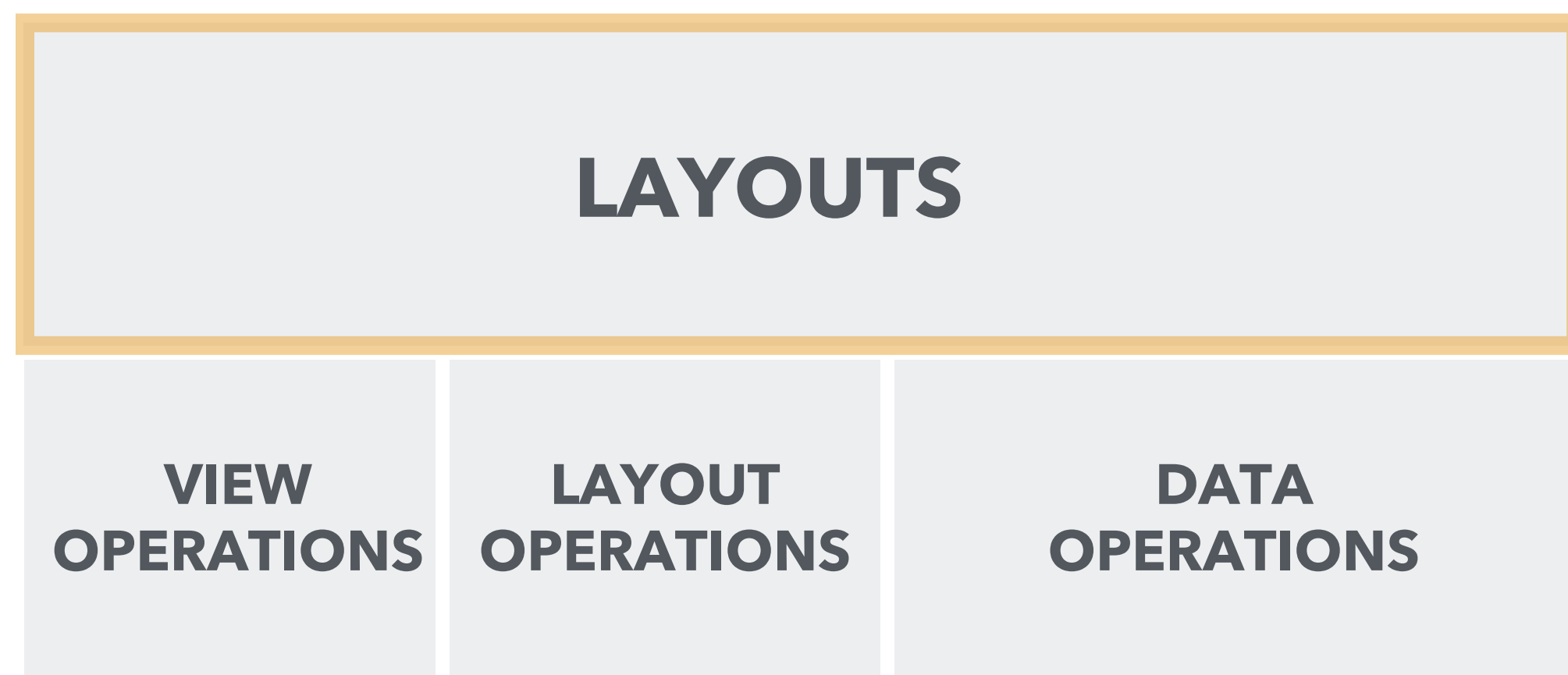
Supports

3

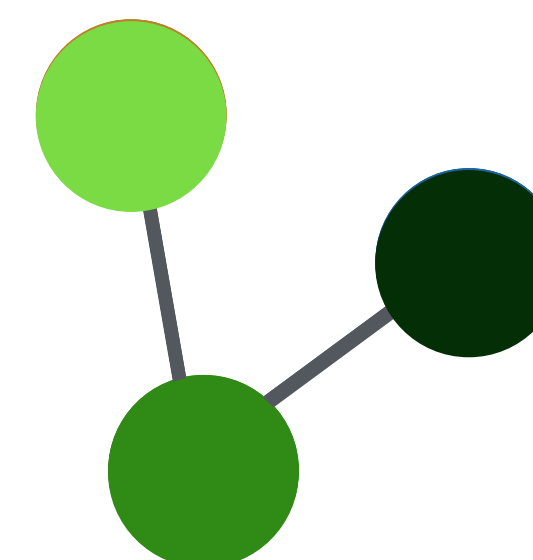
Optimized for



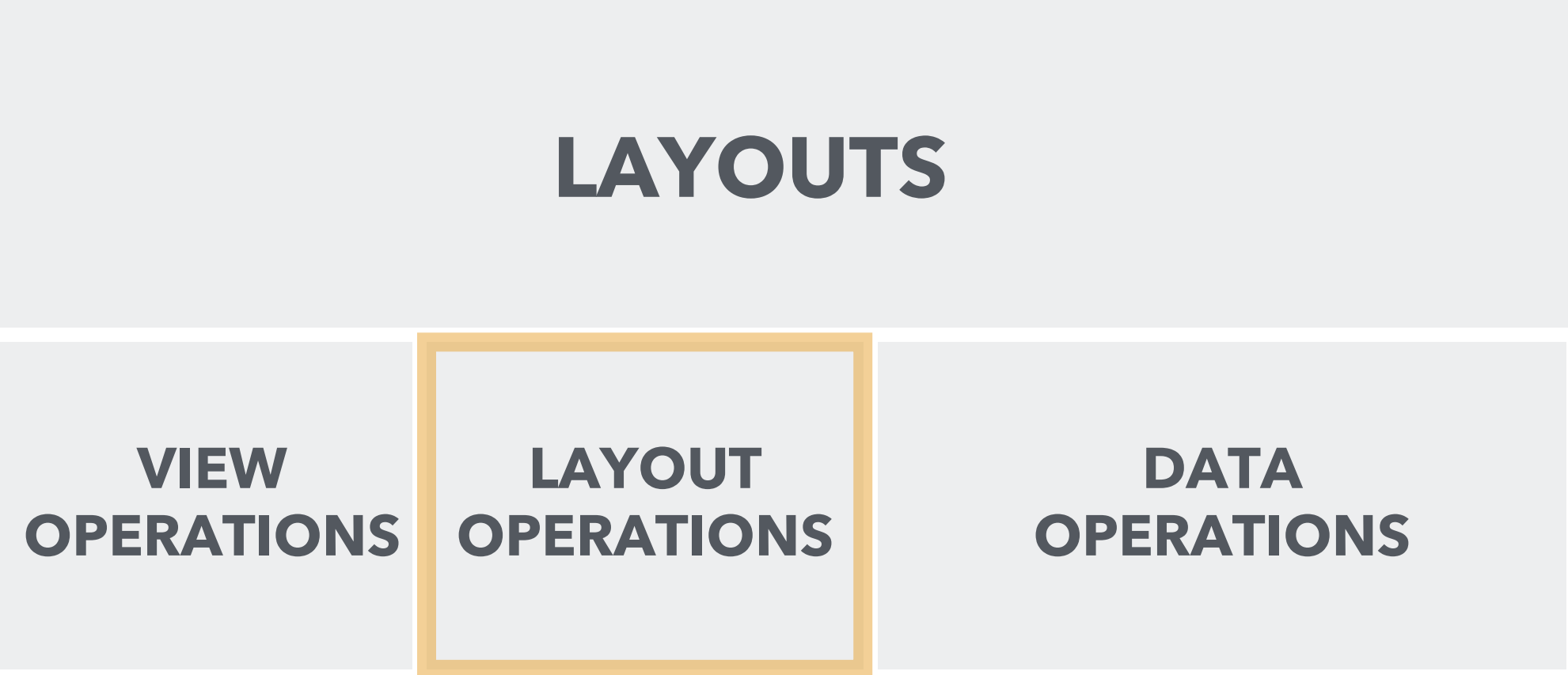




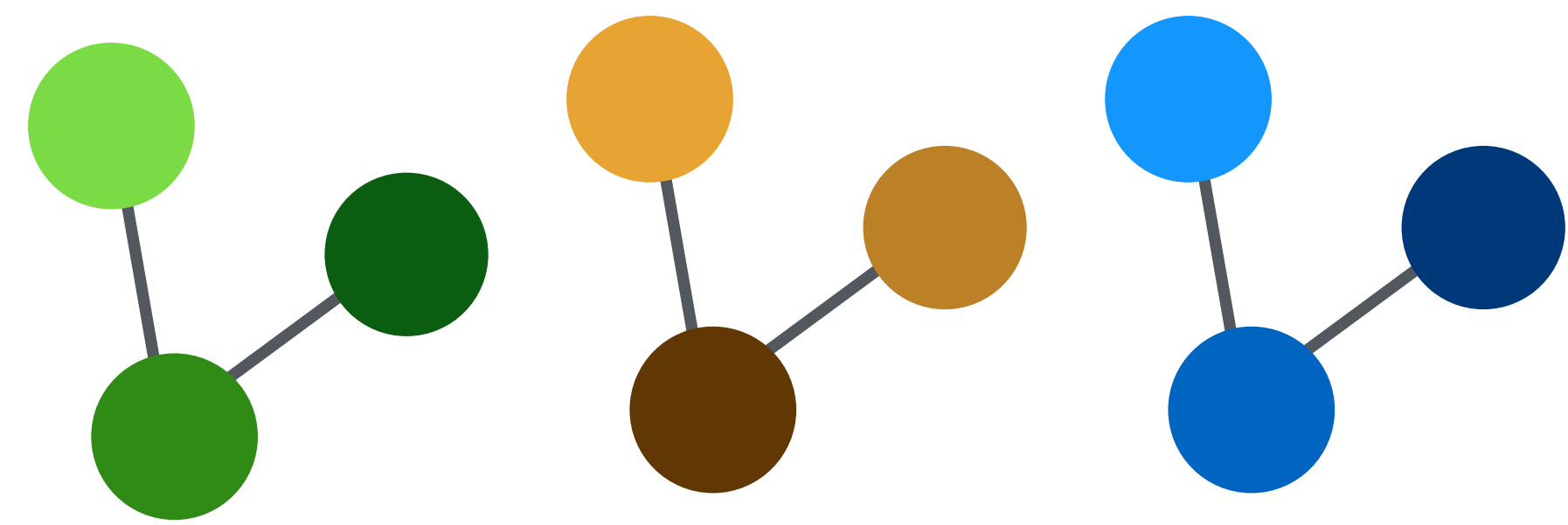
Node-Link Diagram with on-node encoding

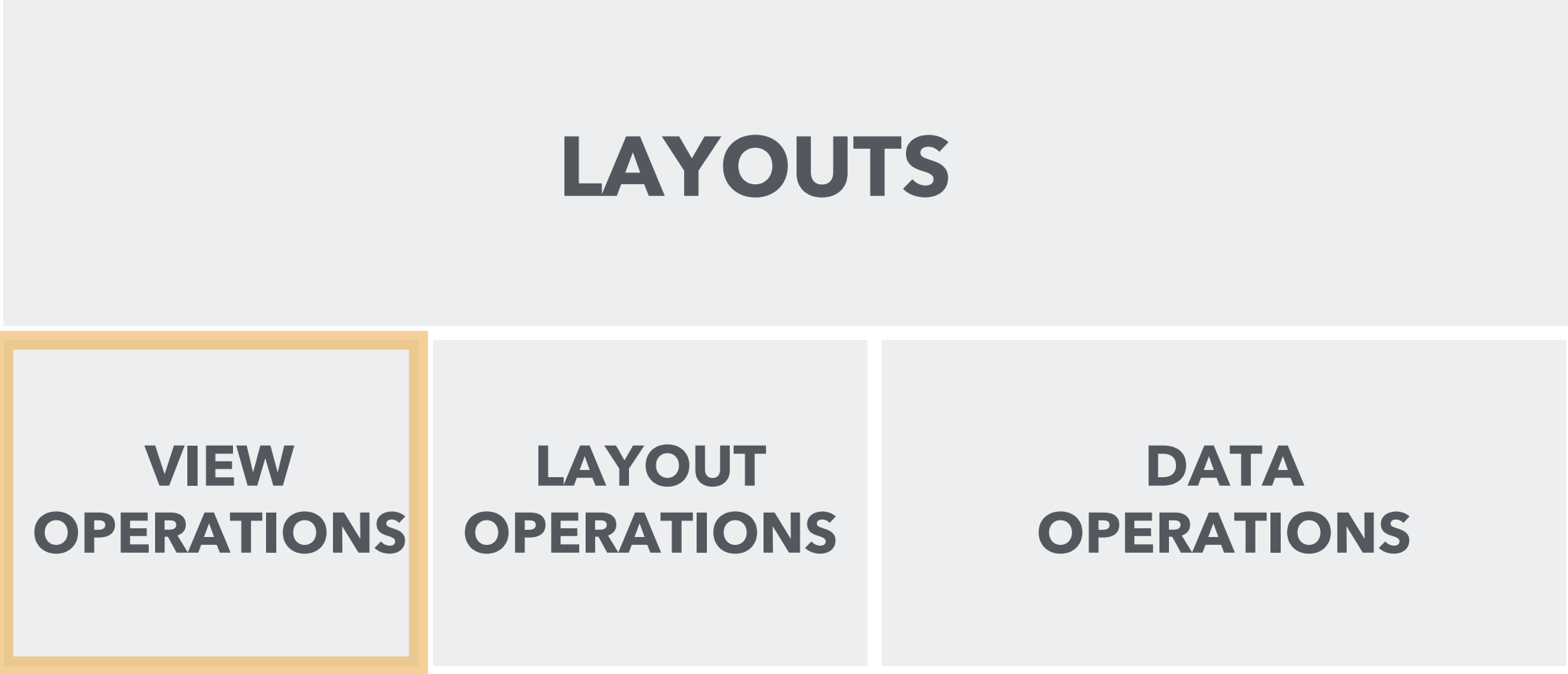




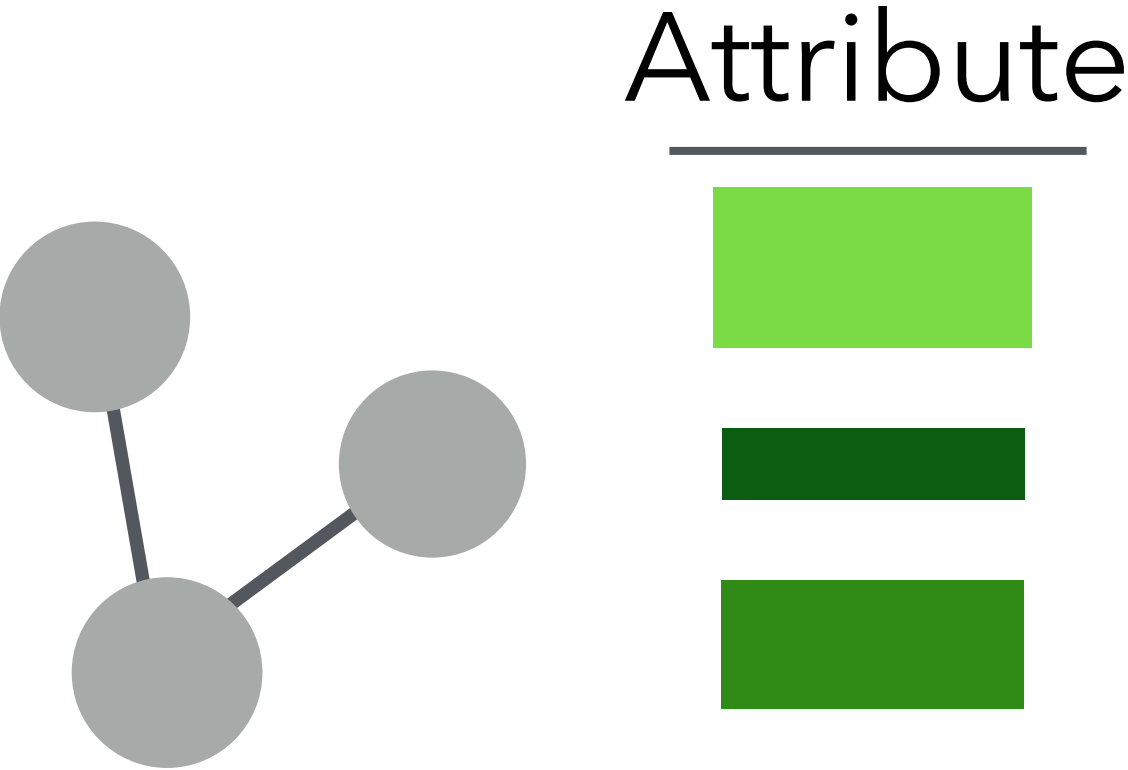


Small Multiples

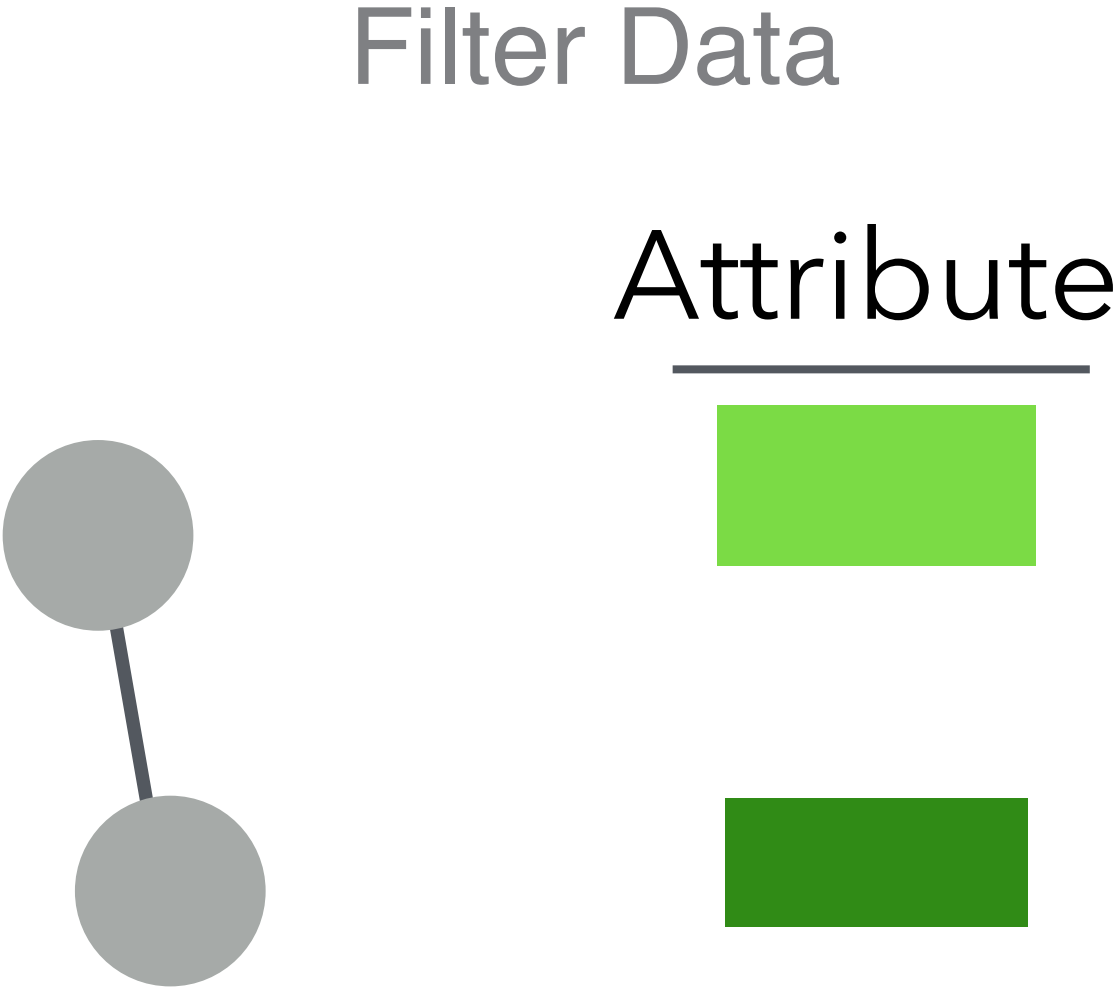
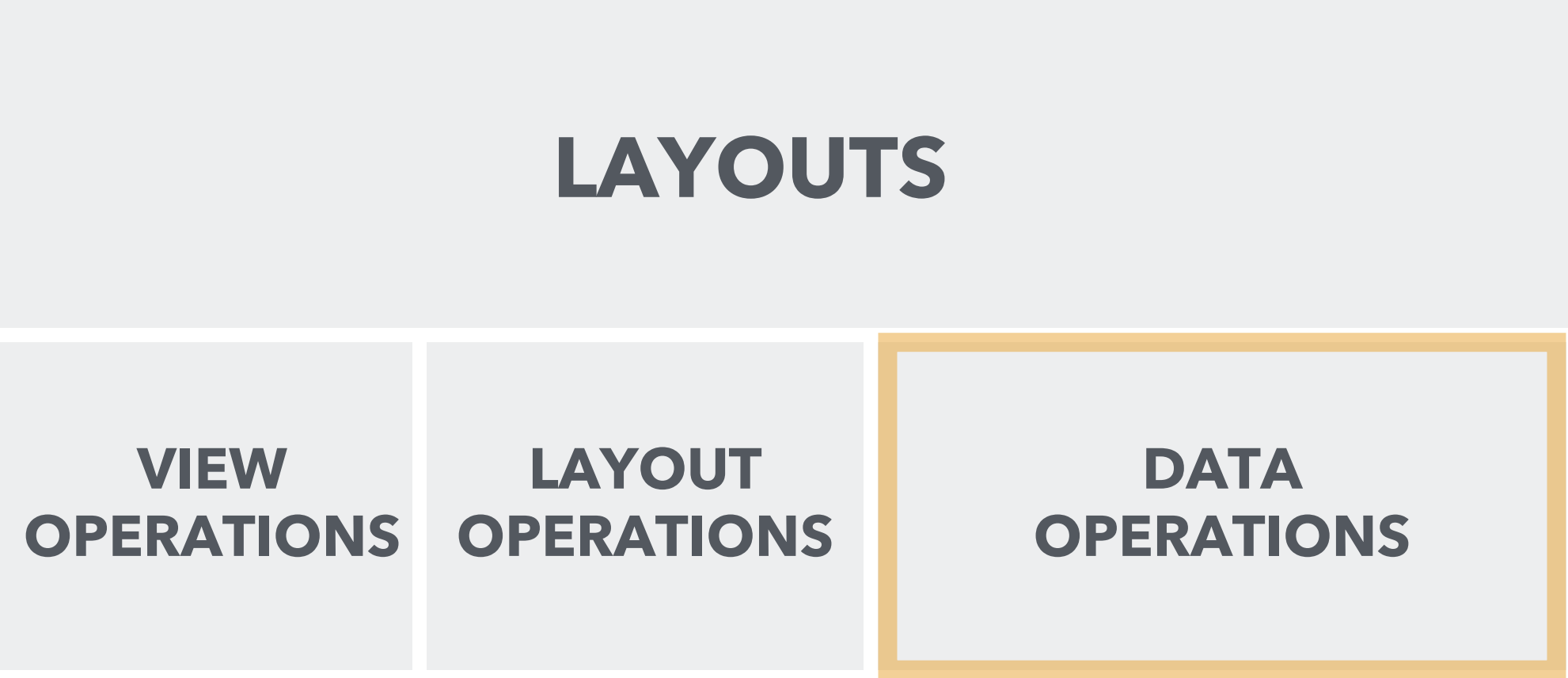


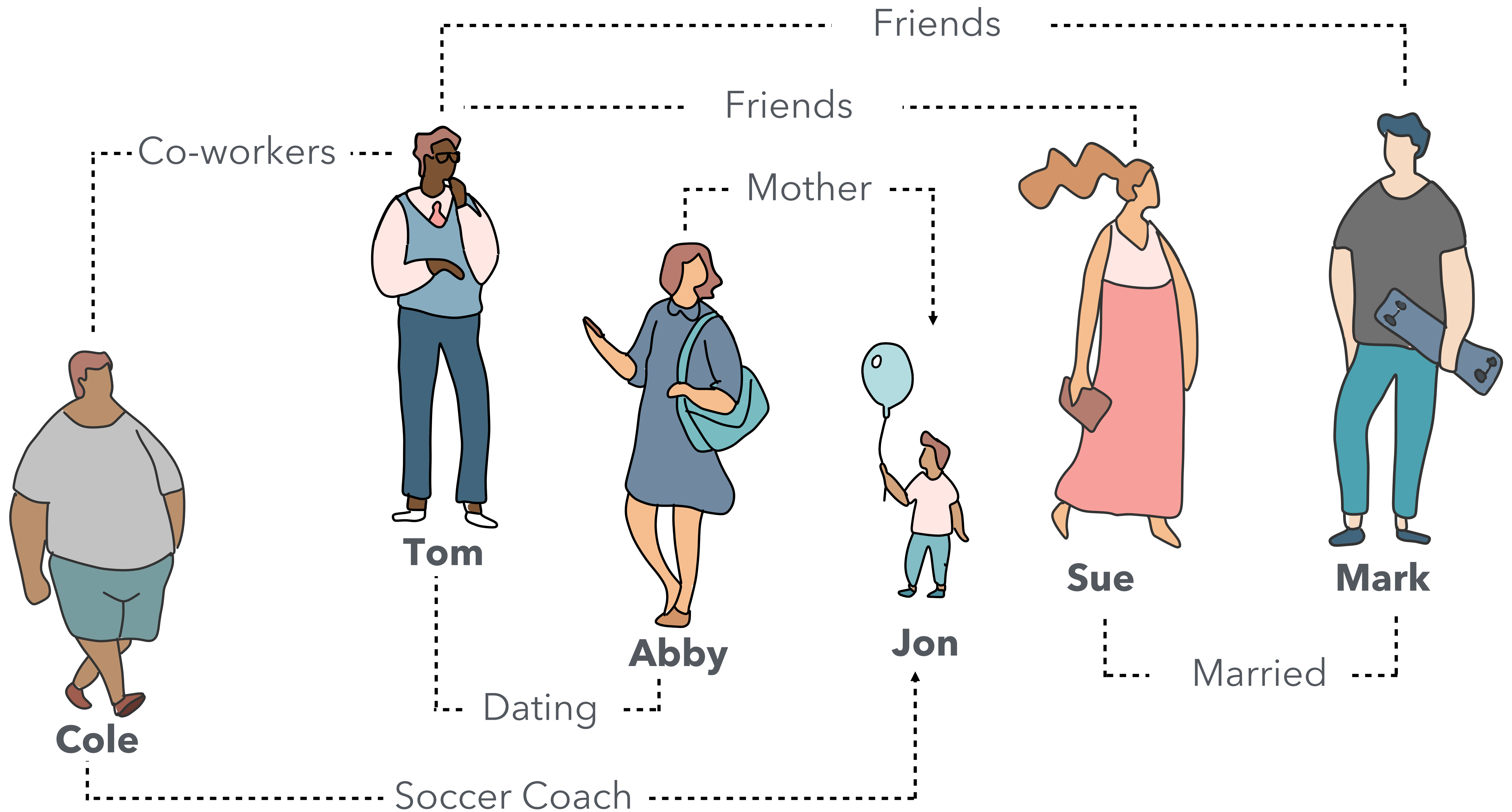


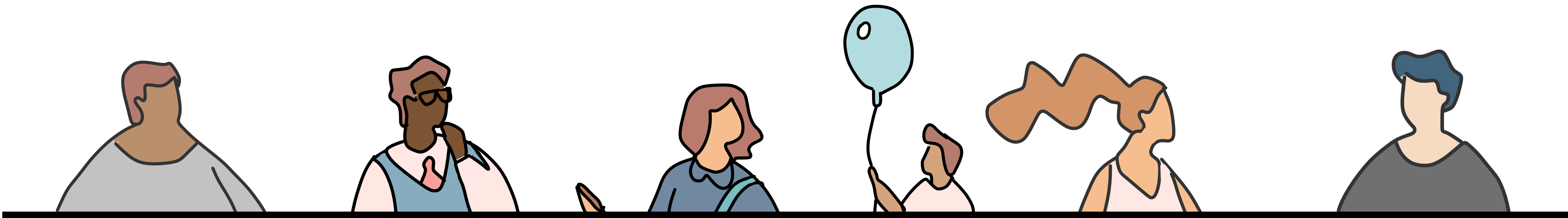
Juxtaposed Views





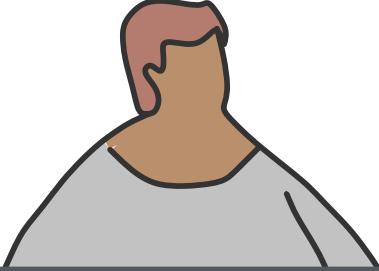

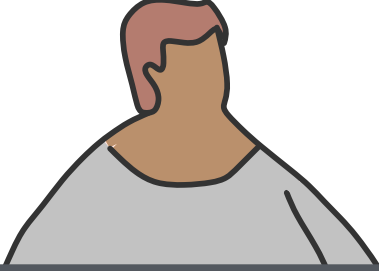
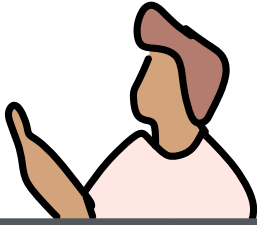



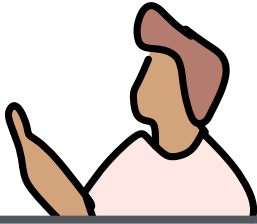



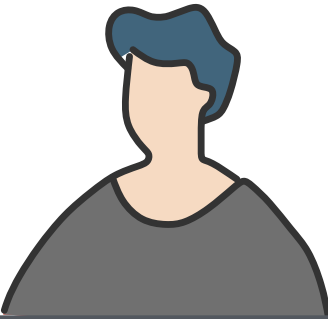

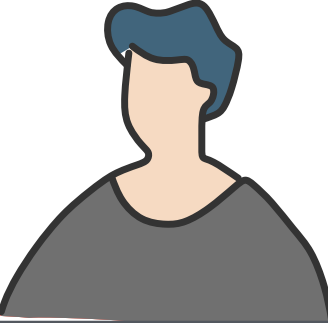




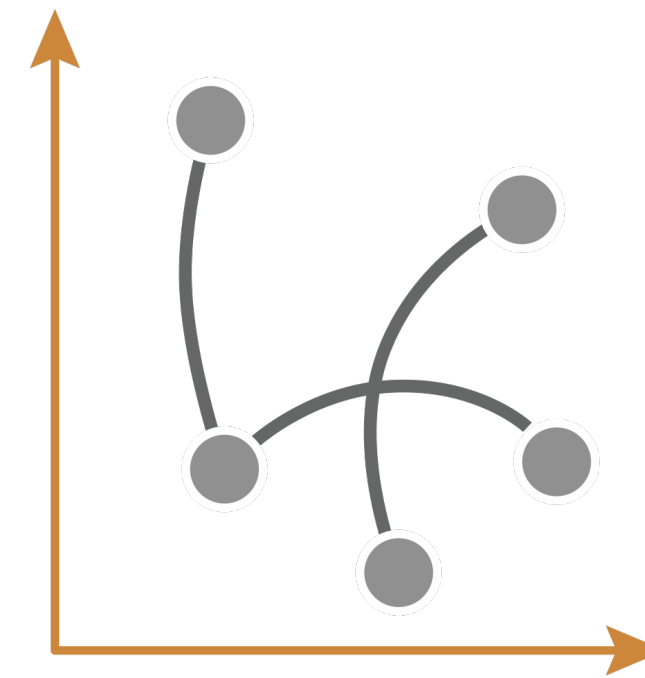
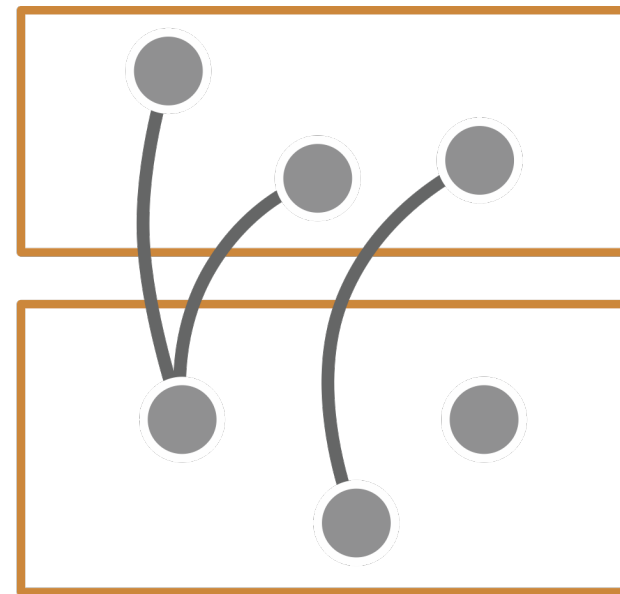
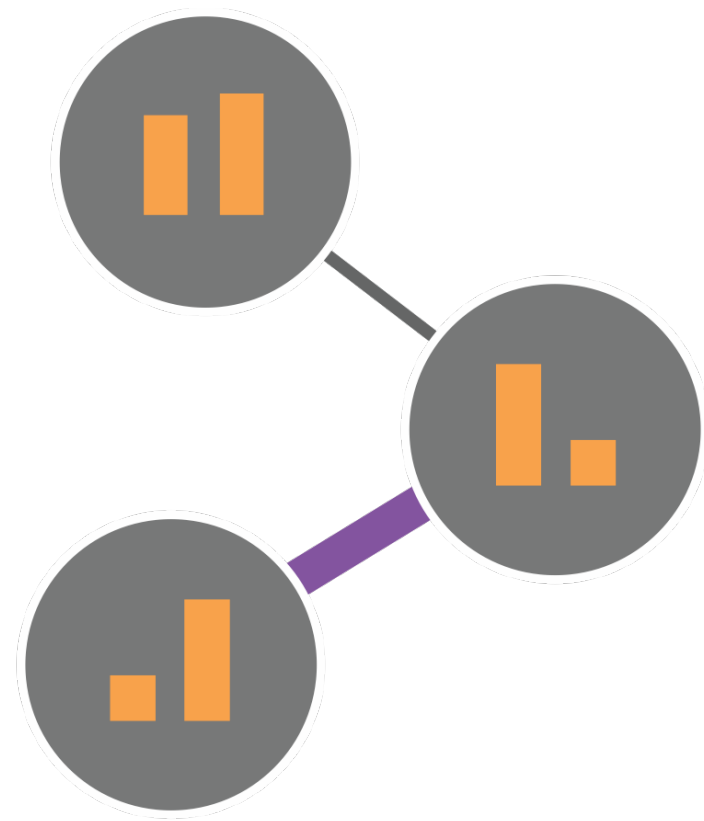


Name	Cole	Tom	Abby	Jon	Sue	Mark
Beverage	Port	Beer	Port	Coke	Coke	Beer
Day 1	1	0	4	3	3	5
Day 2	0	2	5	3	5	5
Day 3	4	1	2	2	4	3

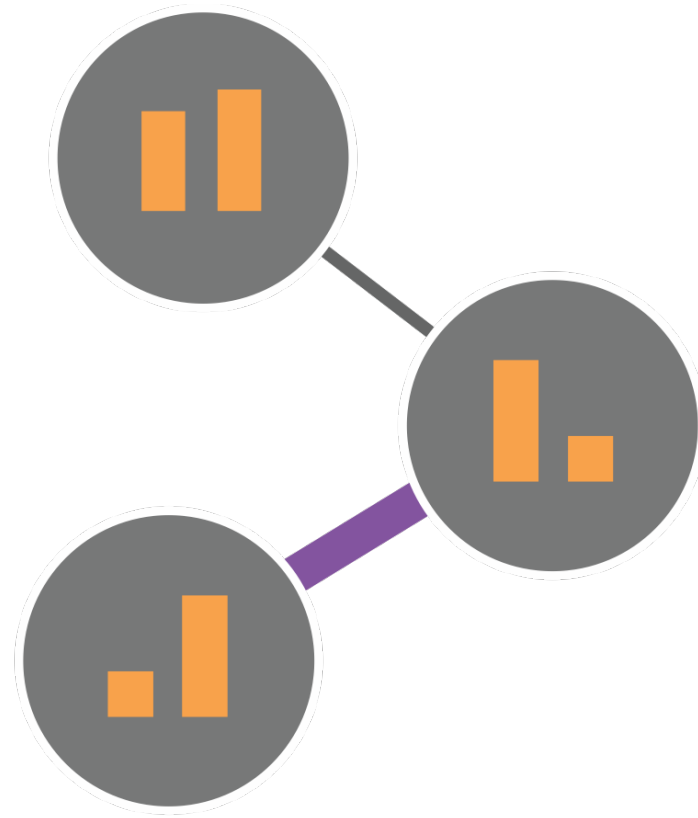


Source	Target	Type	Duration
		Co-workers	3 years
		Soccer Coach	2 years
		Dating	1 year
		Mother / Son	7 years
		Friends	12 years
		Friends	3 years
		Married	6 years

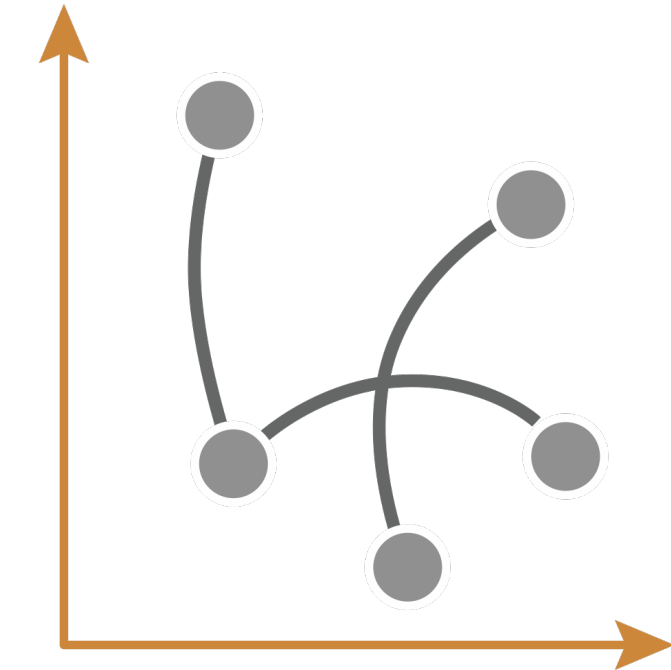
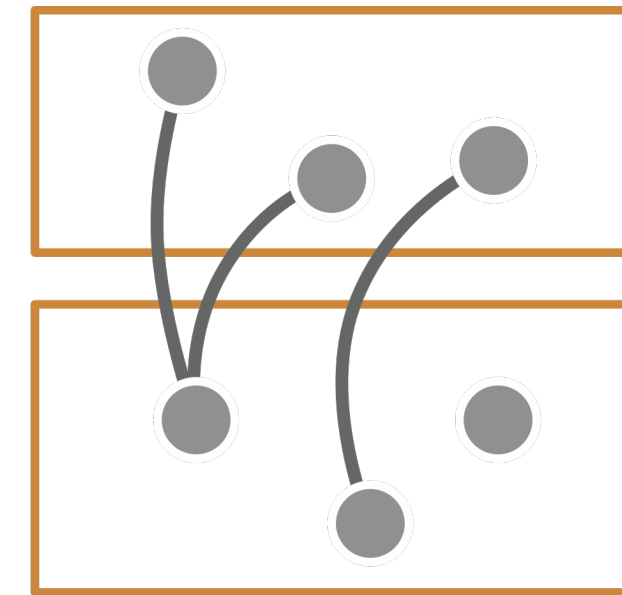
# Node-Link Layouts



## Topology Driven Layout

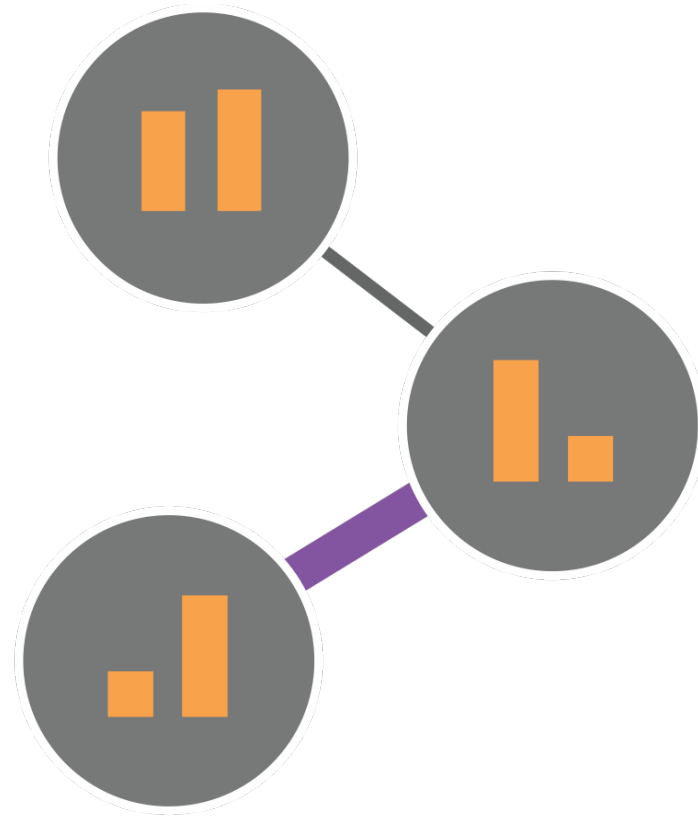


## Attribute Driven Layouts



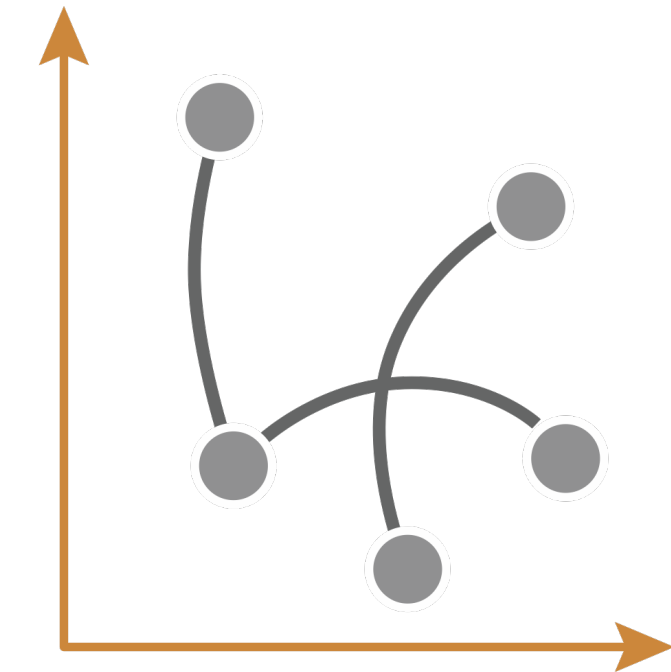
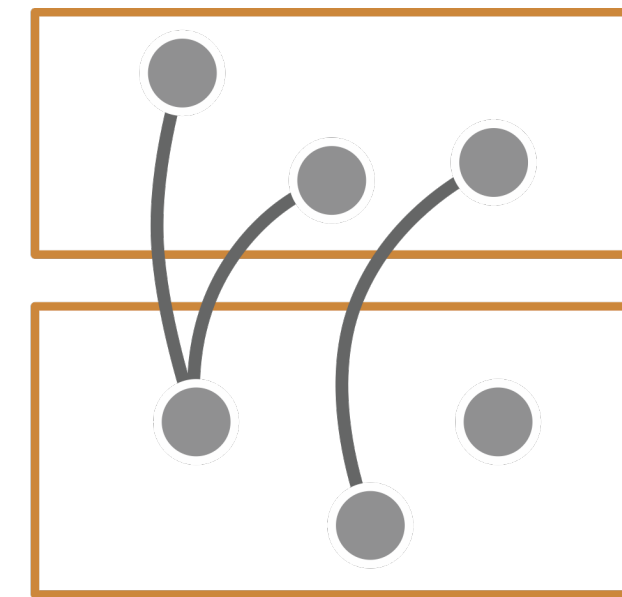


## Topology Driven Layout

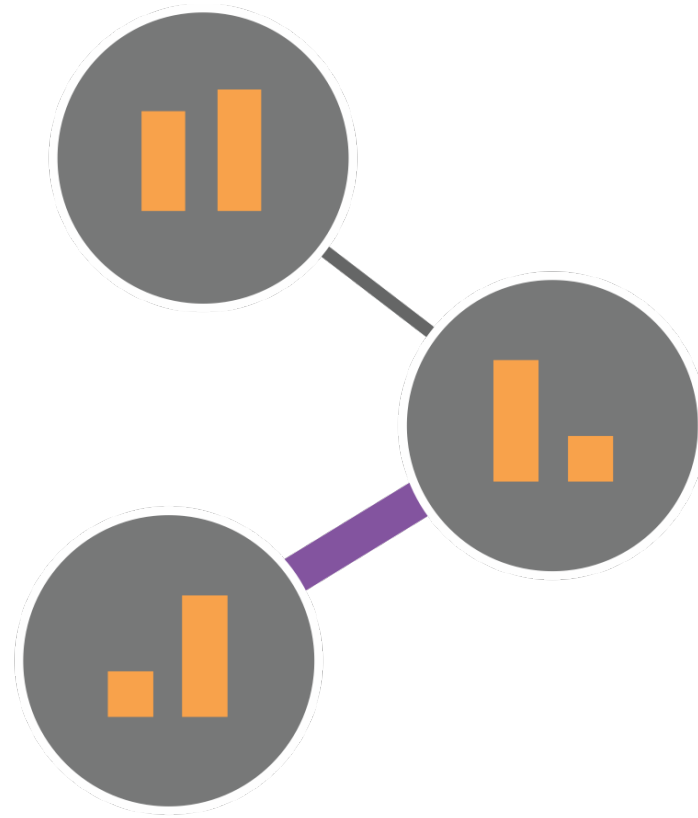


On-Node / On-Edge  
Encoding

## Attribute Driven Layouts

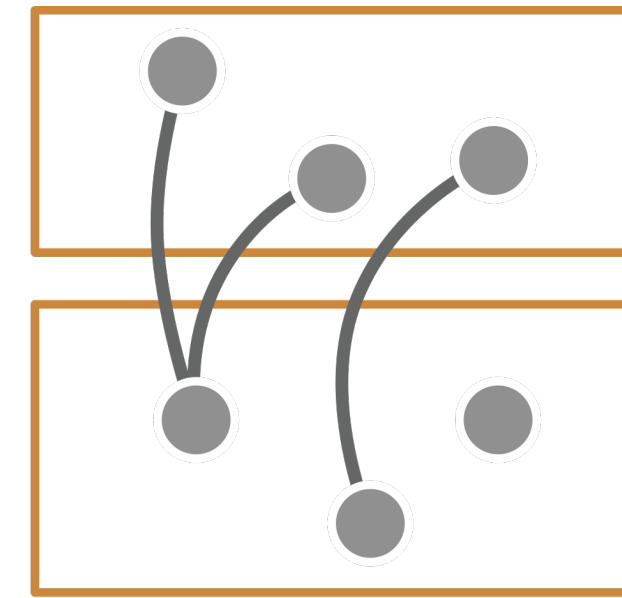


## Topology Driven Layout

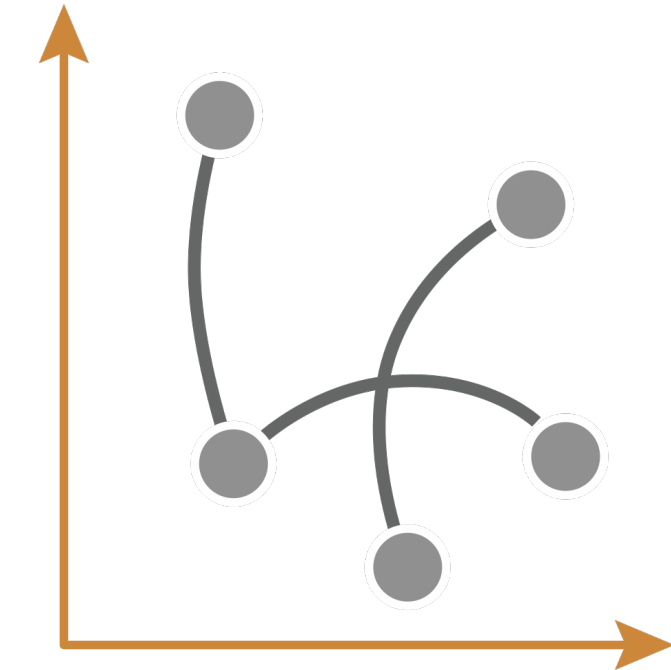


On-Node / On-Edge  
Encoding

## Attribute Driven Layouts

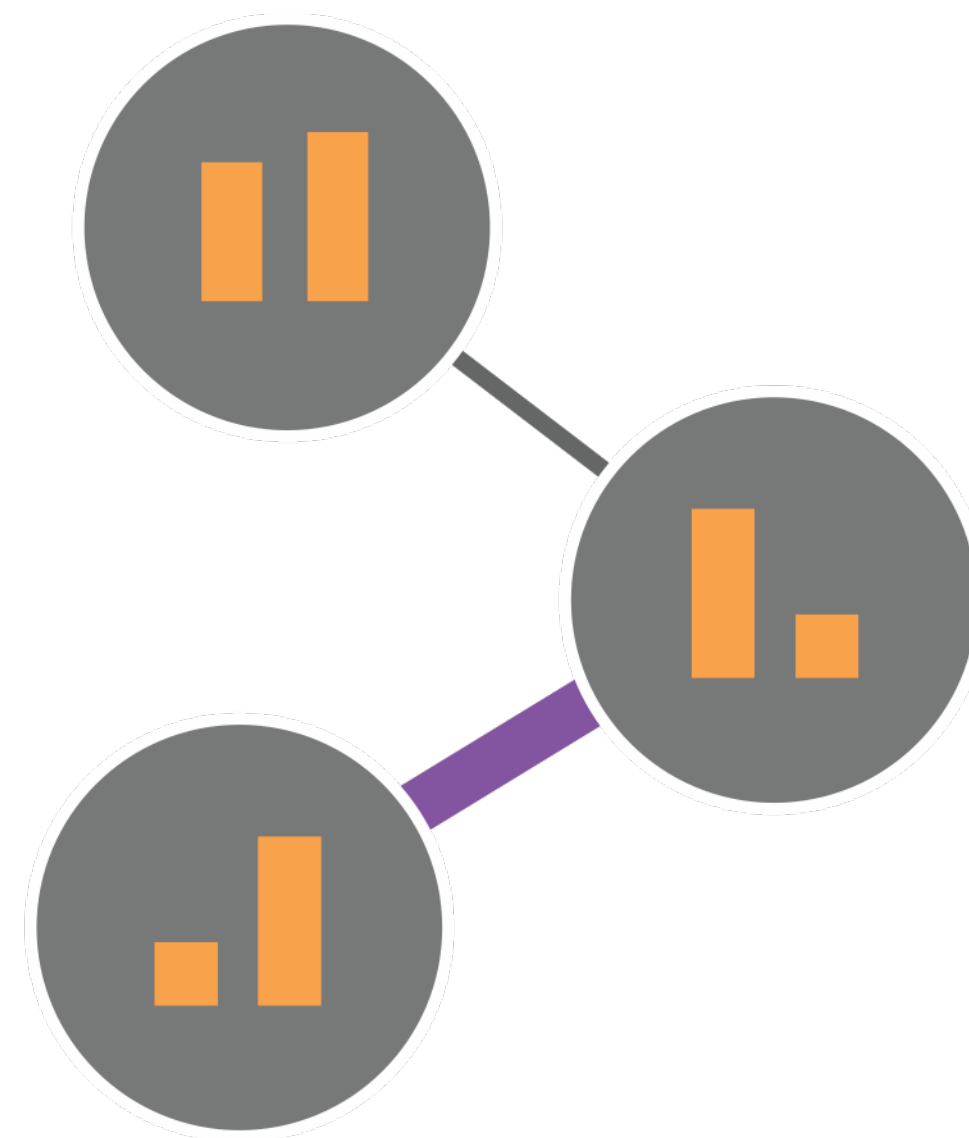


Attribute-Driven  
Faceting



Attribute-Driven  
Positioning

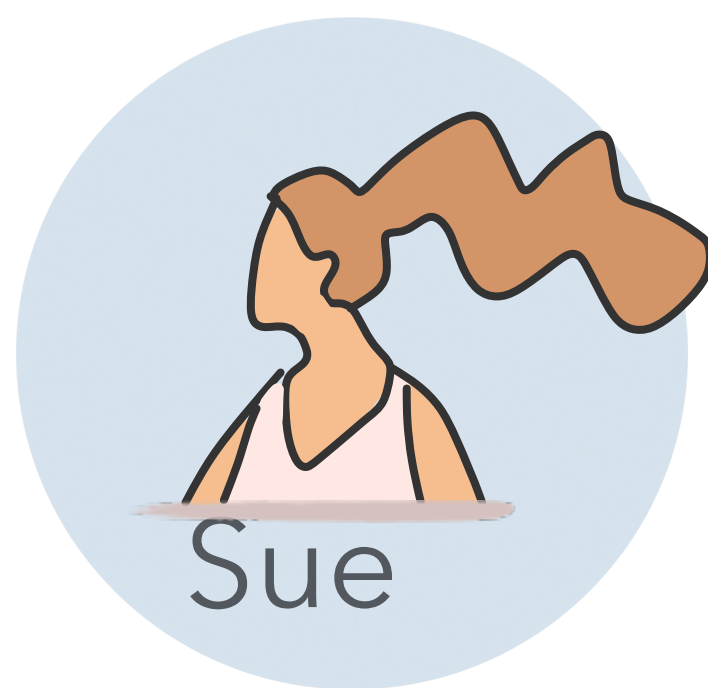
# On-Node / On-Edge Encoding







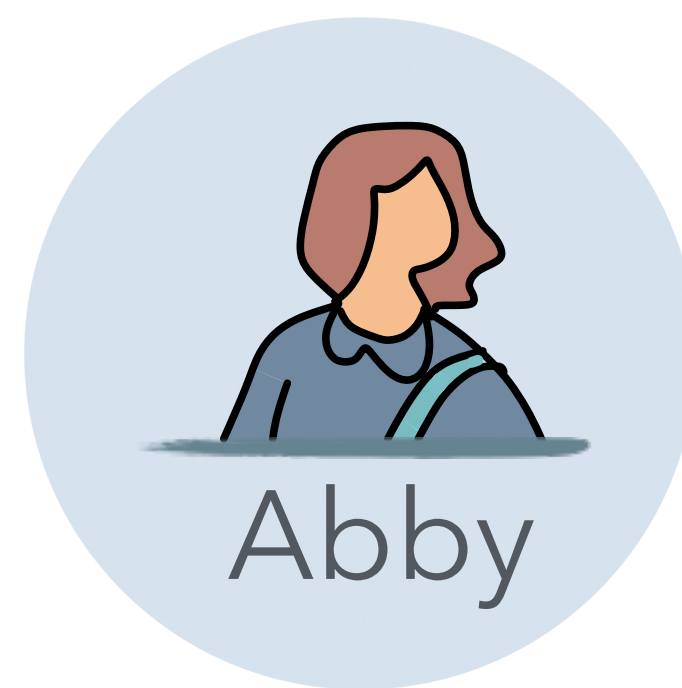
Mark



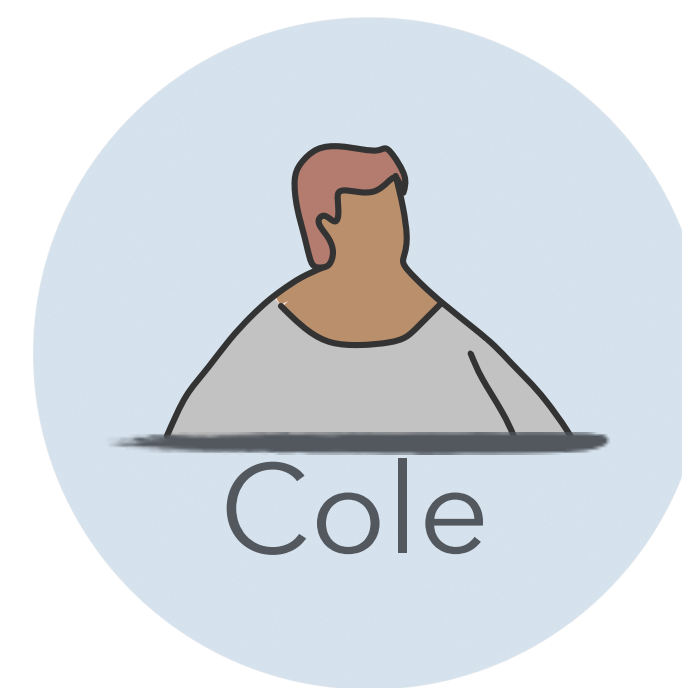
Sue



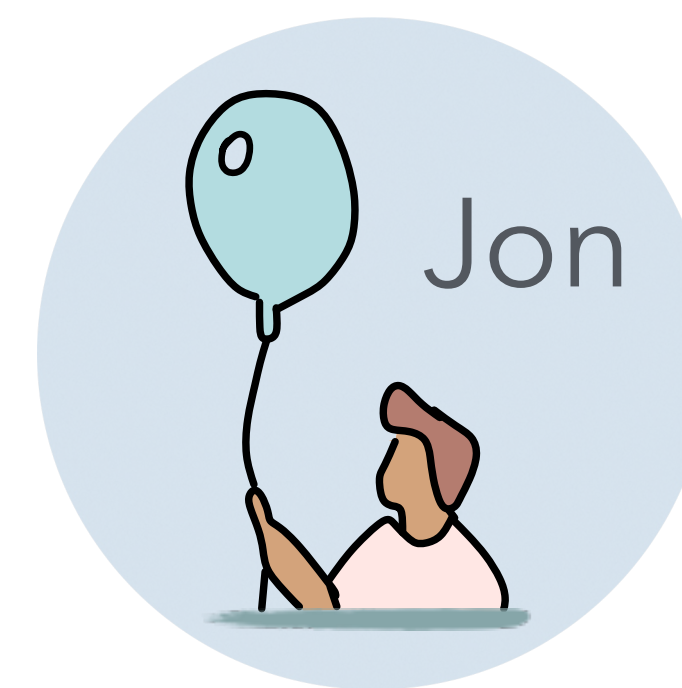
Tom



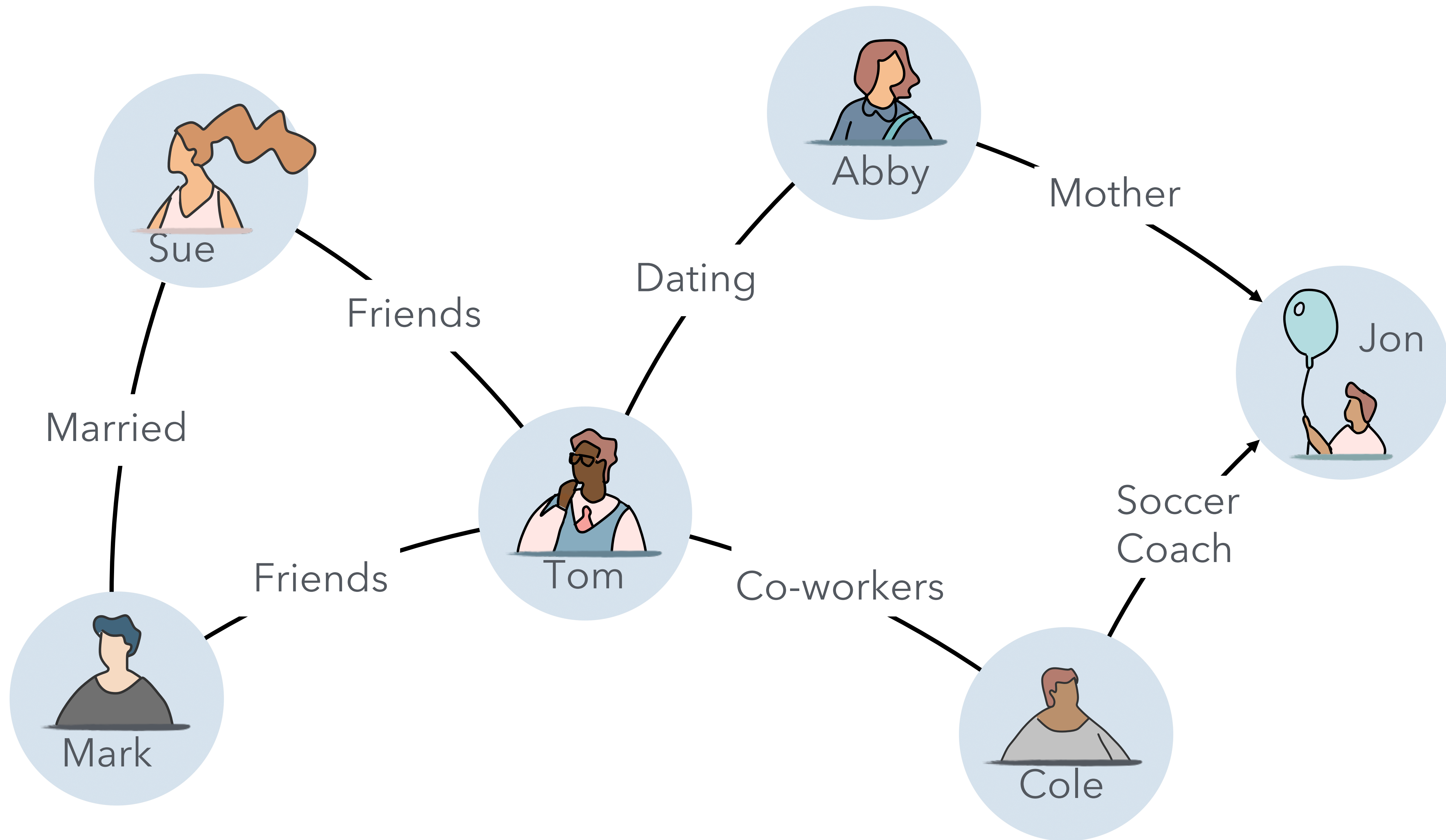
Abby



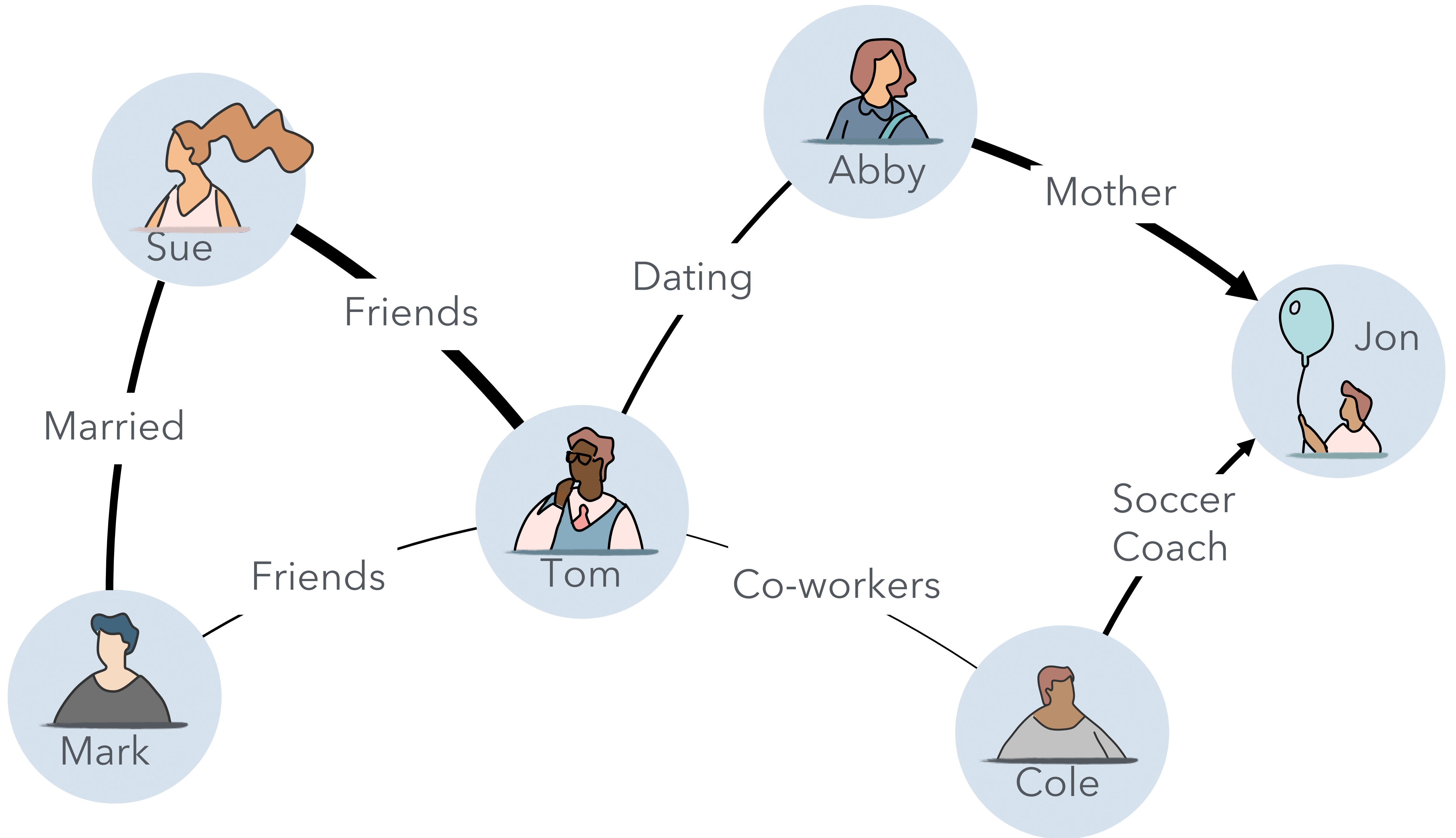
Cole



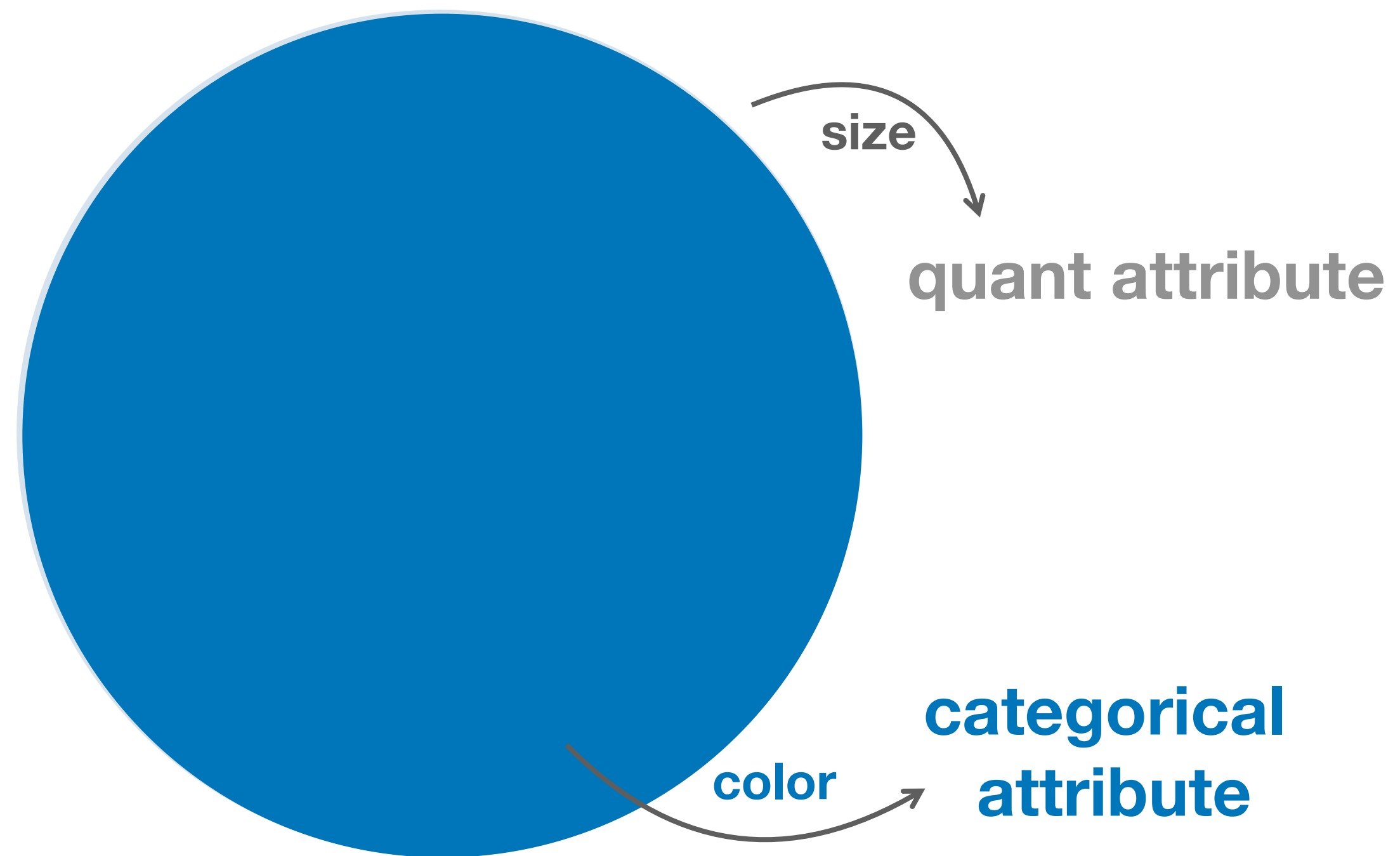
Jon

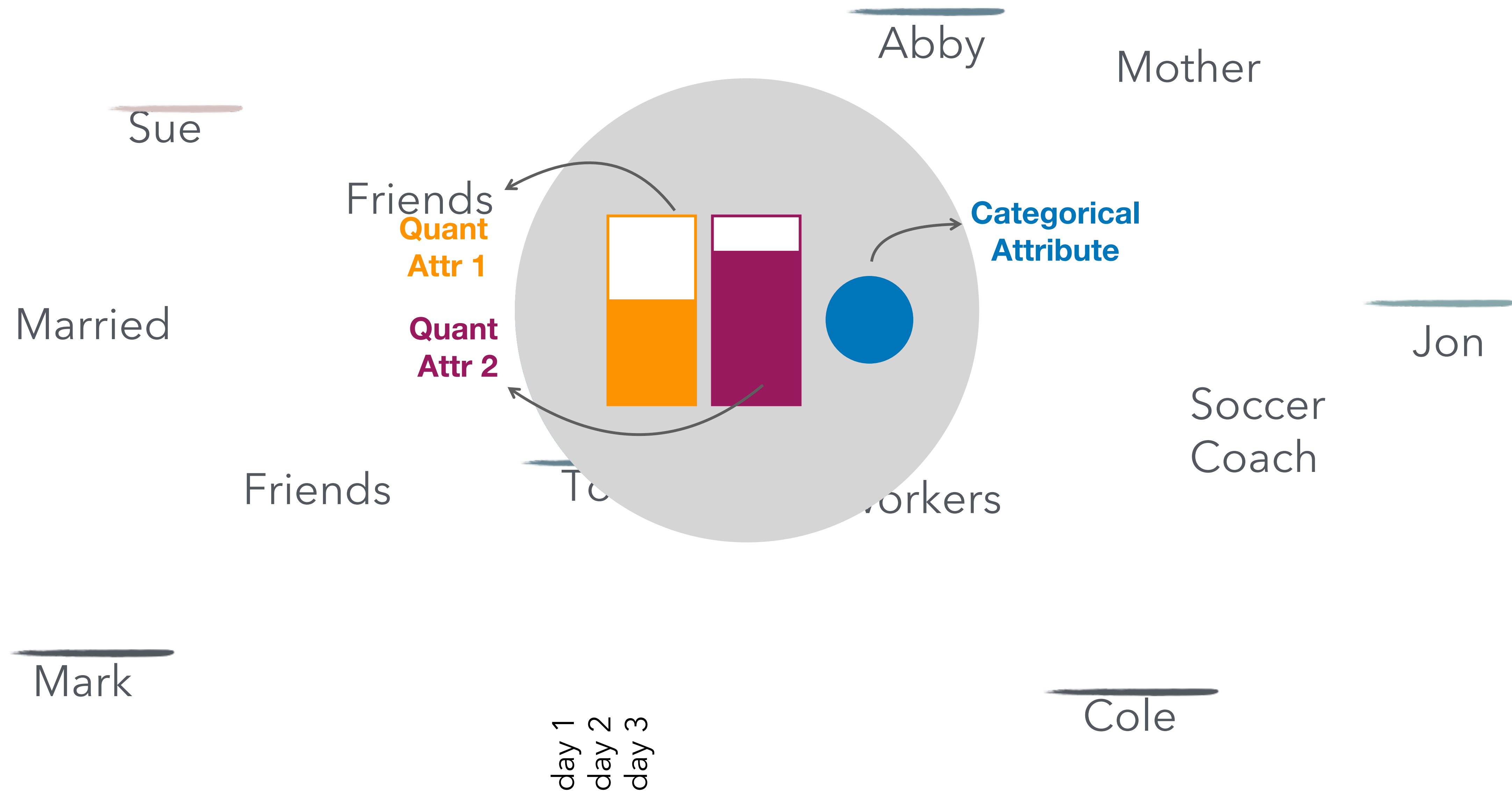


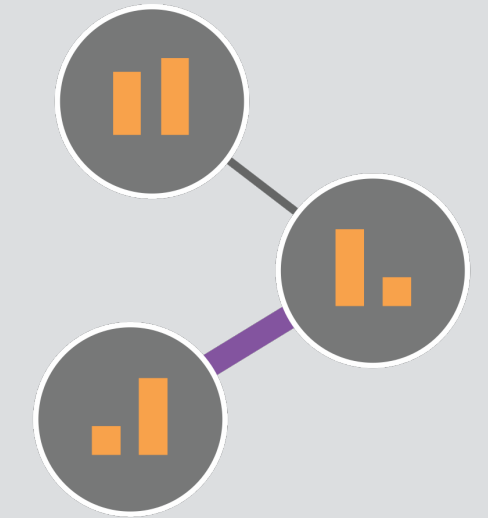
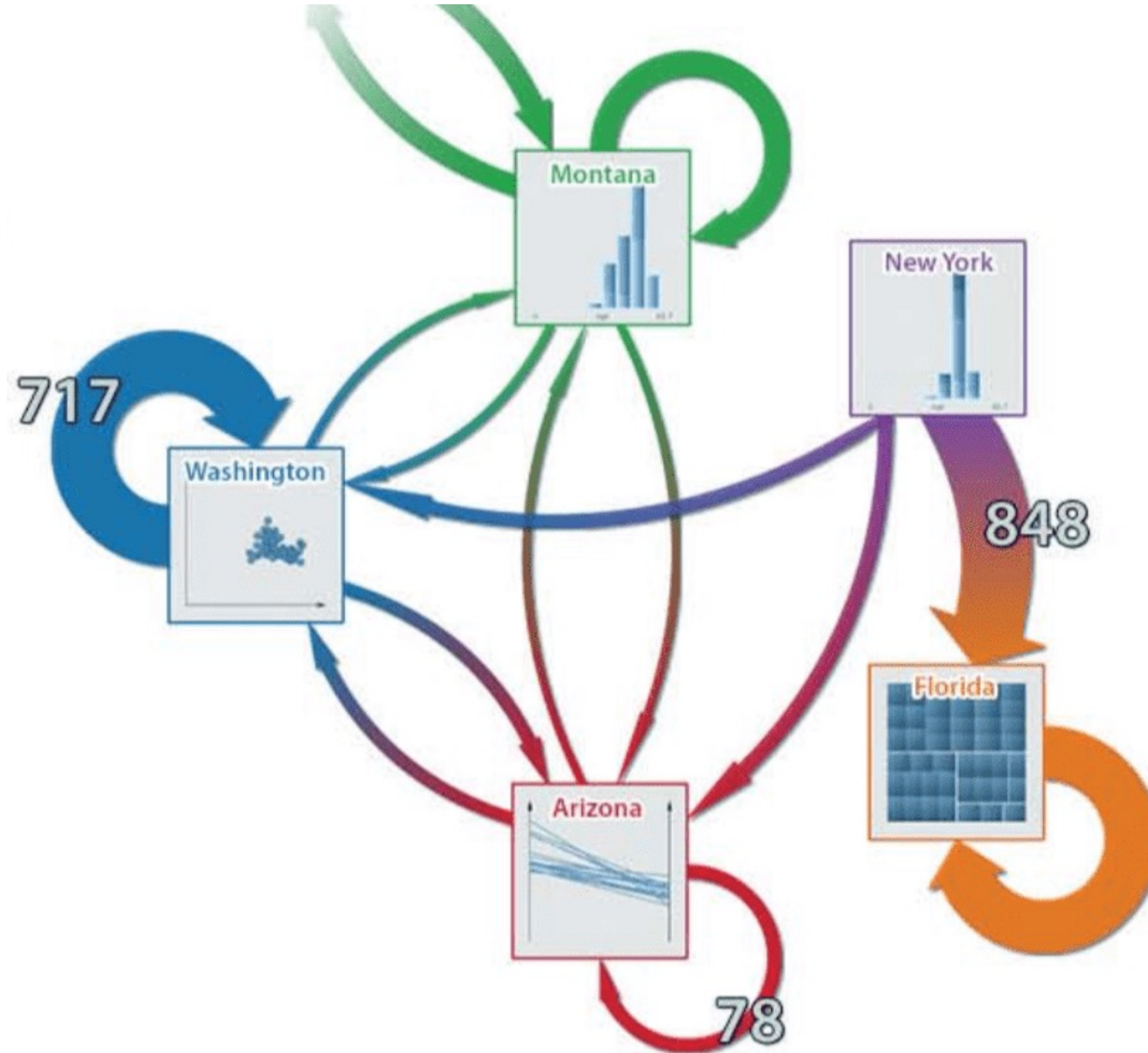








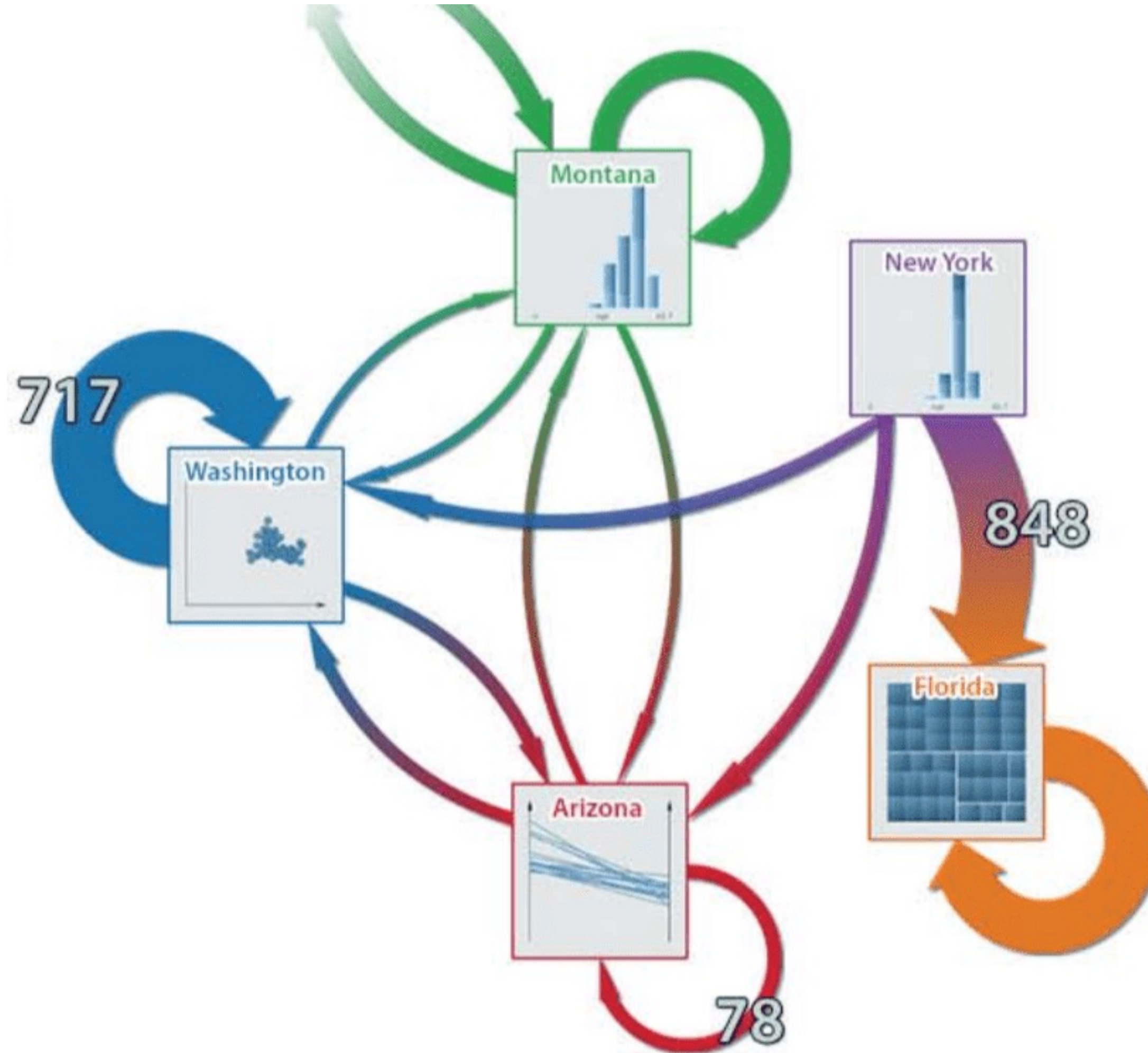




On-Node / On-Edge  
Encoding

*Elzen and Wijk, 2014*

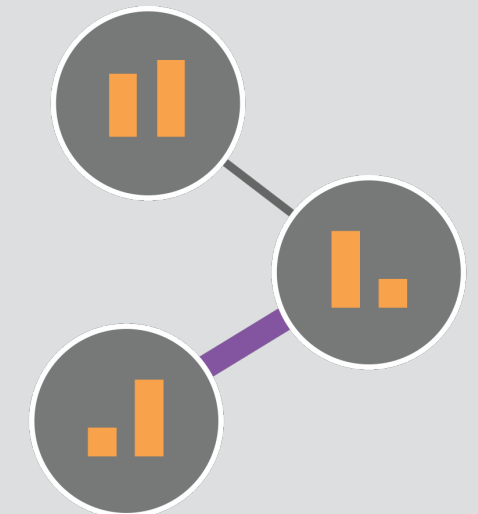




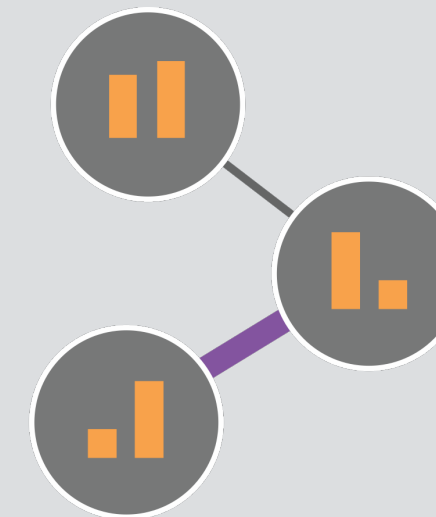
*Elzen and Wijk, 2014*



Aggregating Nodes/Edges



On-Node / On-Edge  
Encoding

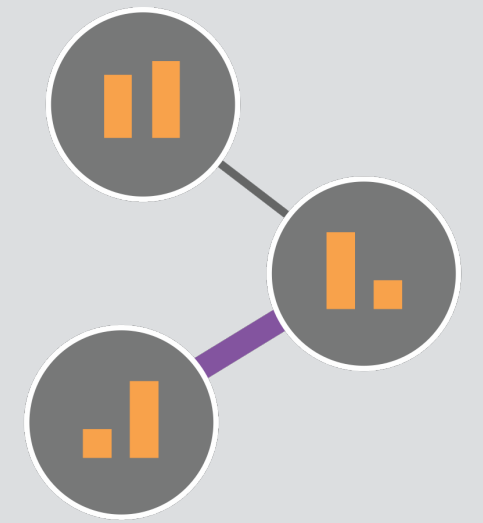


On-Node / On-Edge  
Encoding

Is easily understood by most users  
Works well for all types of networks



Scalability.  
Node size leaves little space to encode attributes.

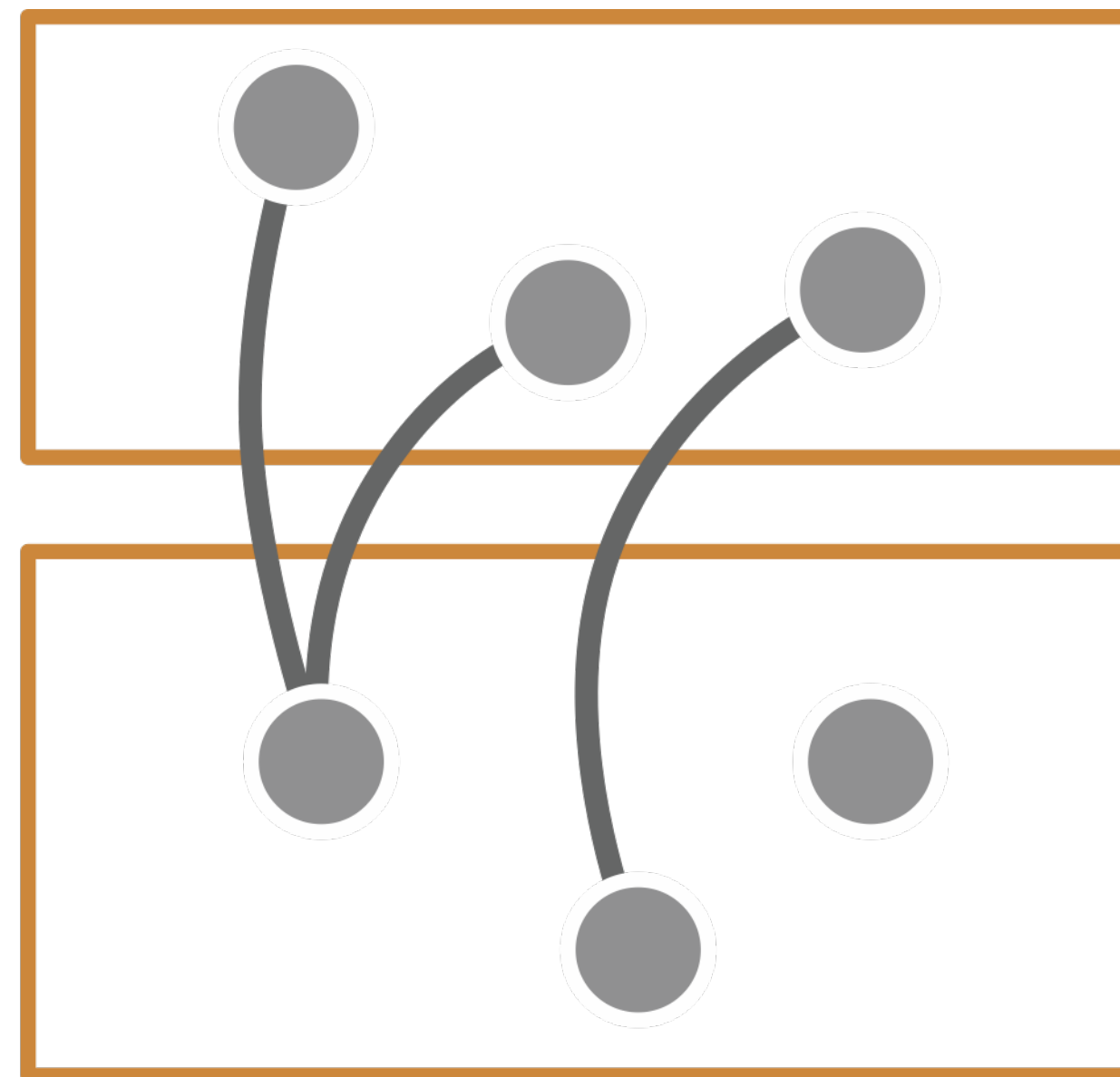


On-Node / On-Edge  
Encoding

*Recommended for small networks when only a few (usually under five) attributes on the nodes are shown, or in combination with a zooming/filtering strategy*



# Attribute-Driven Faceting







A large, empty, light gray rectangular box with rounded corners, intended for a description or notes related to the Coca-Cola can.

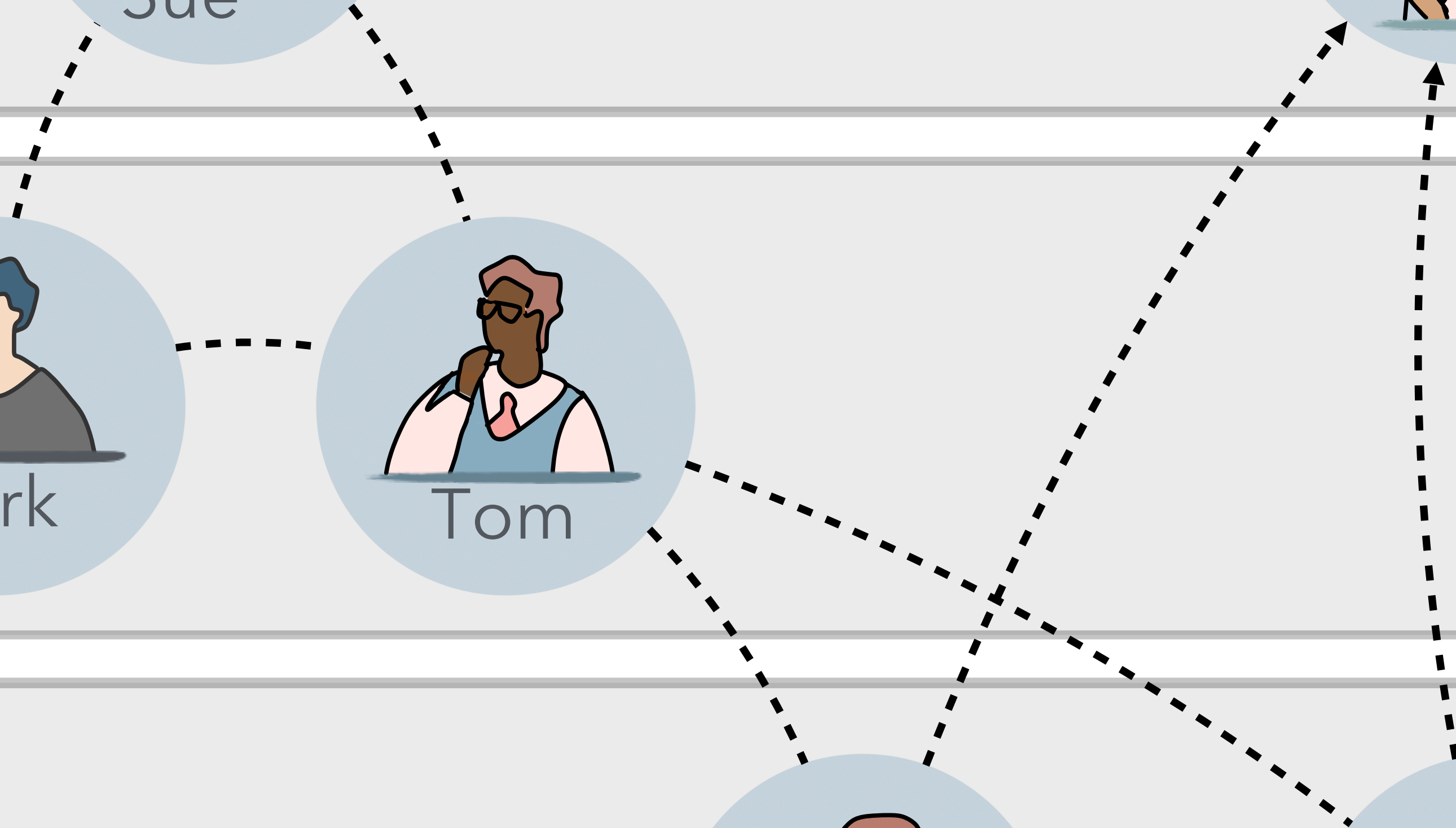
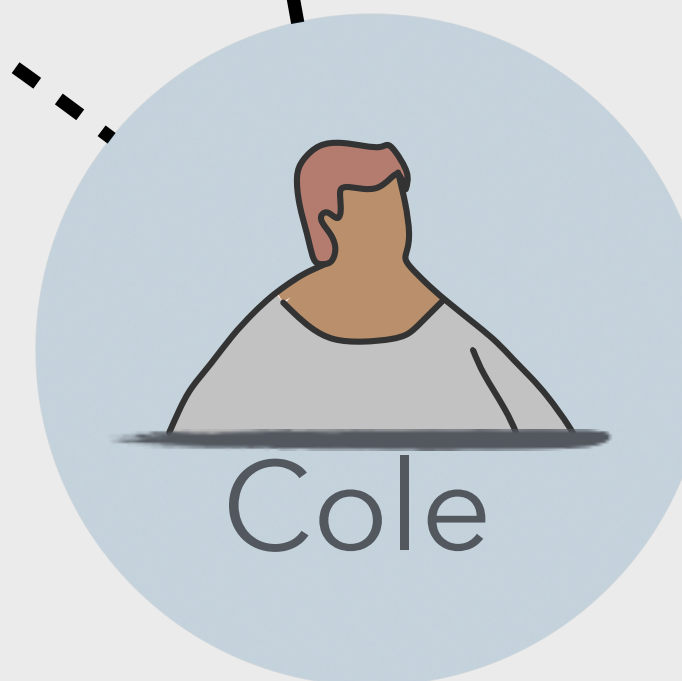
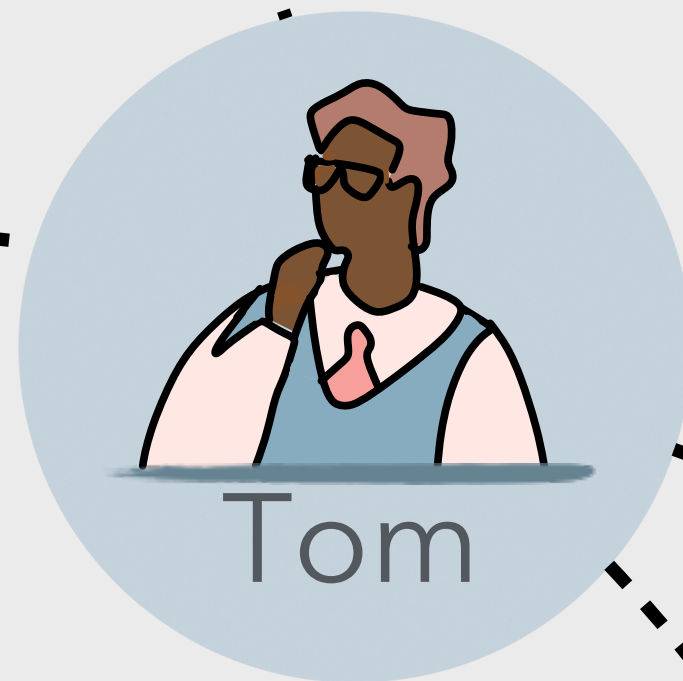
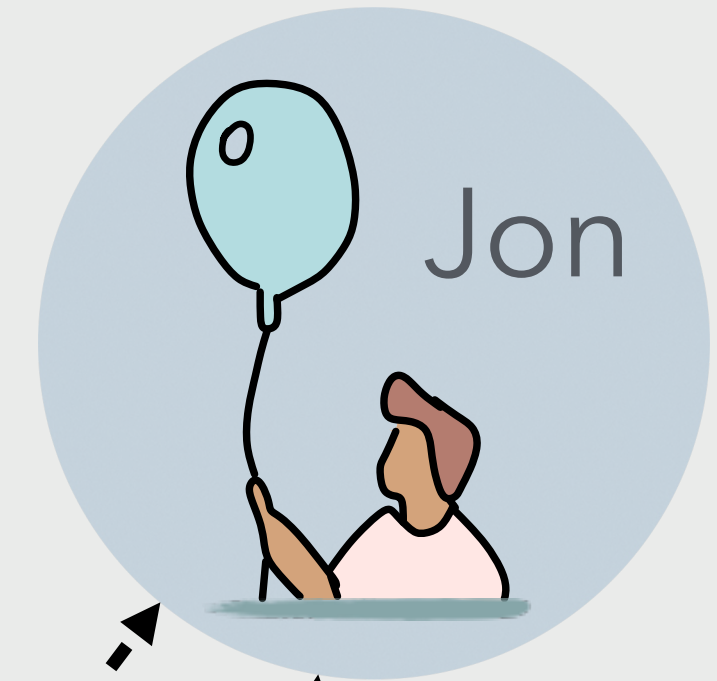
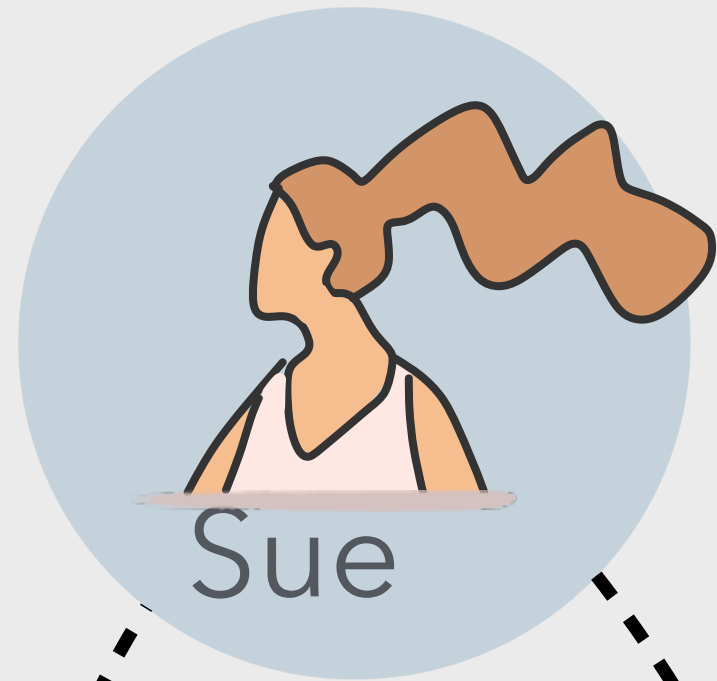
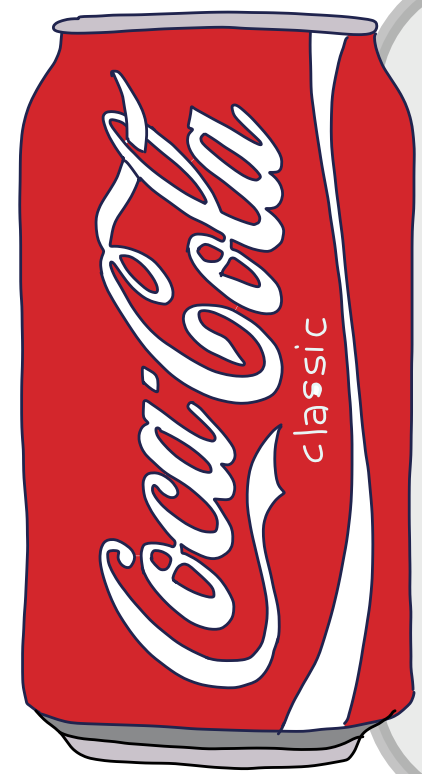


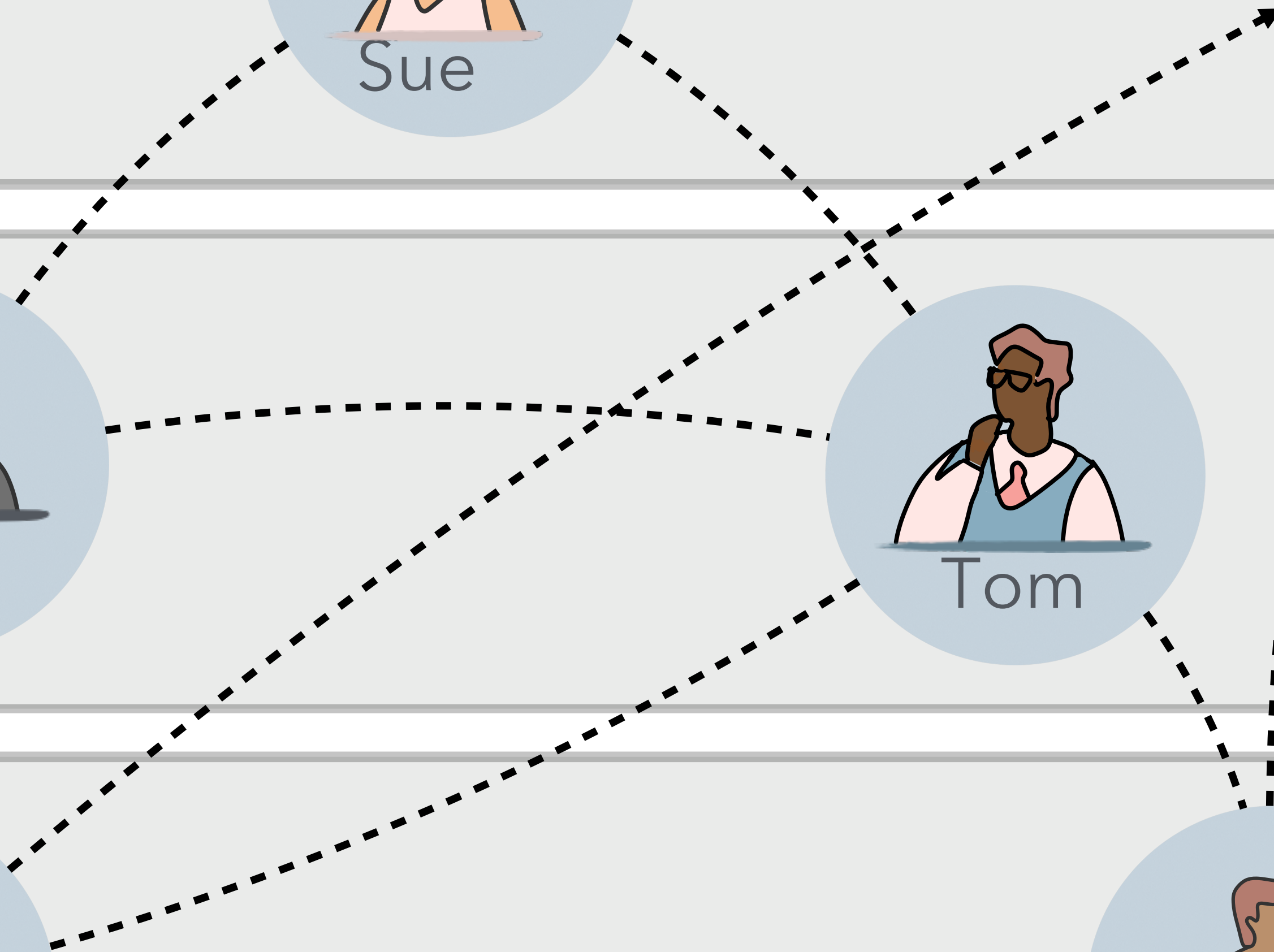
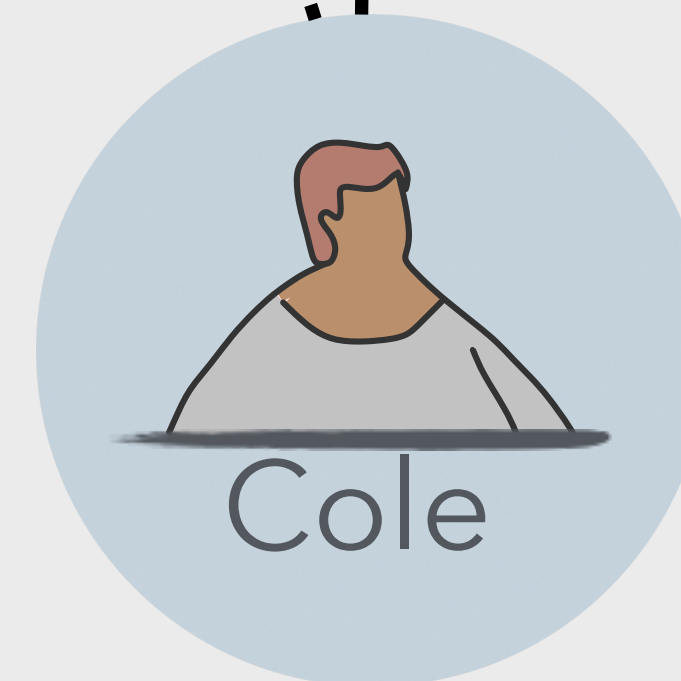
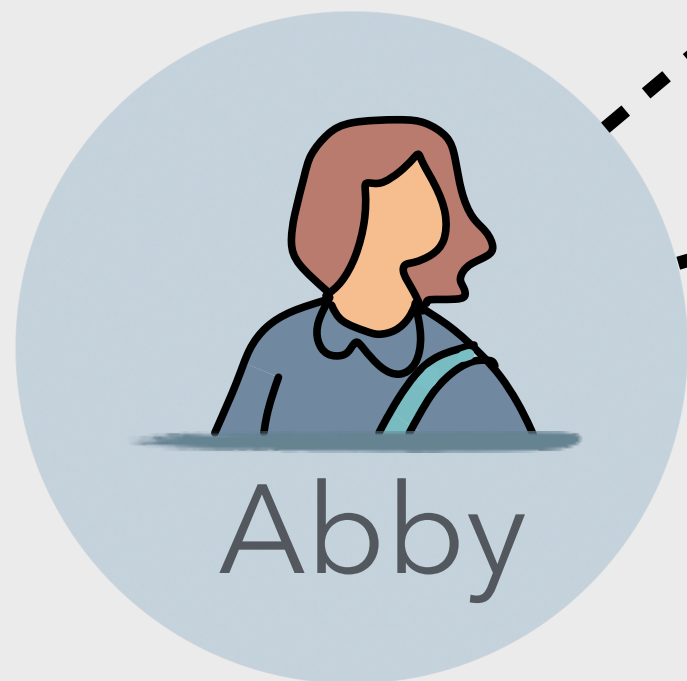
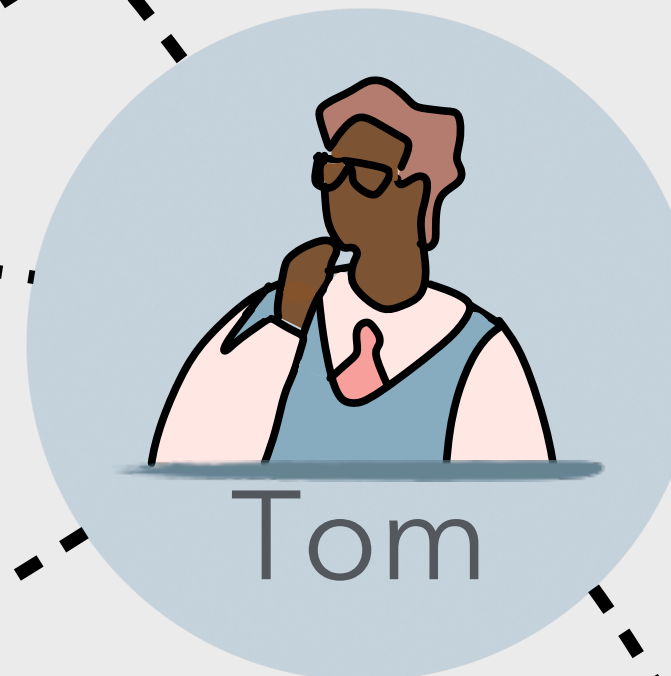
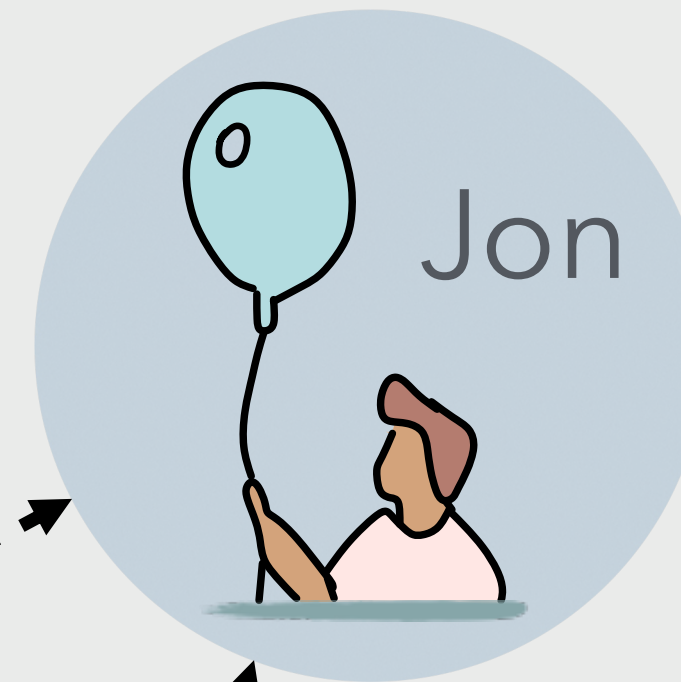
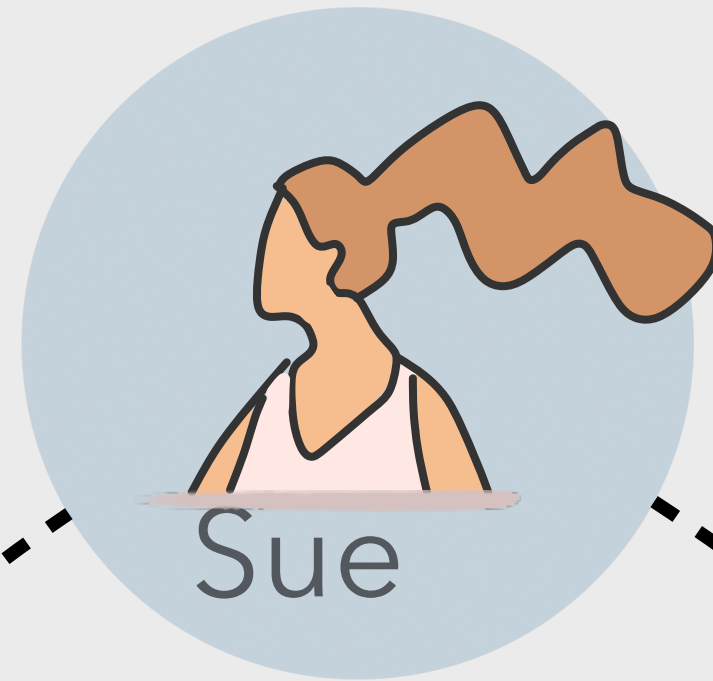
A large, empty, light gray rectangular box with rounded corners, intended for a description or notes related to the beer bottle.



A large, empty, light gray rectangular box with rounded corners, intended for a description or notes related to the Porto bottle.

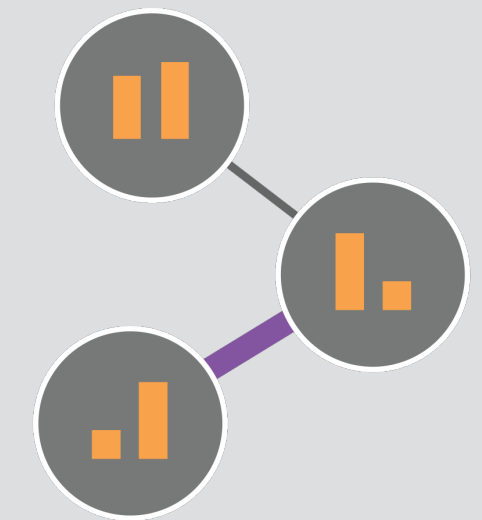
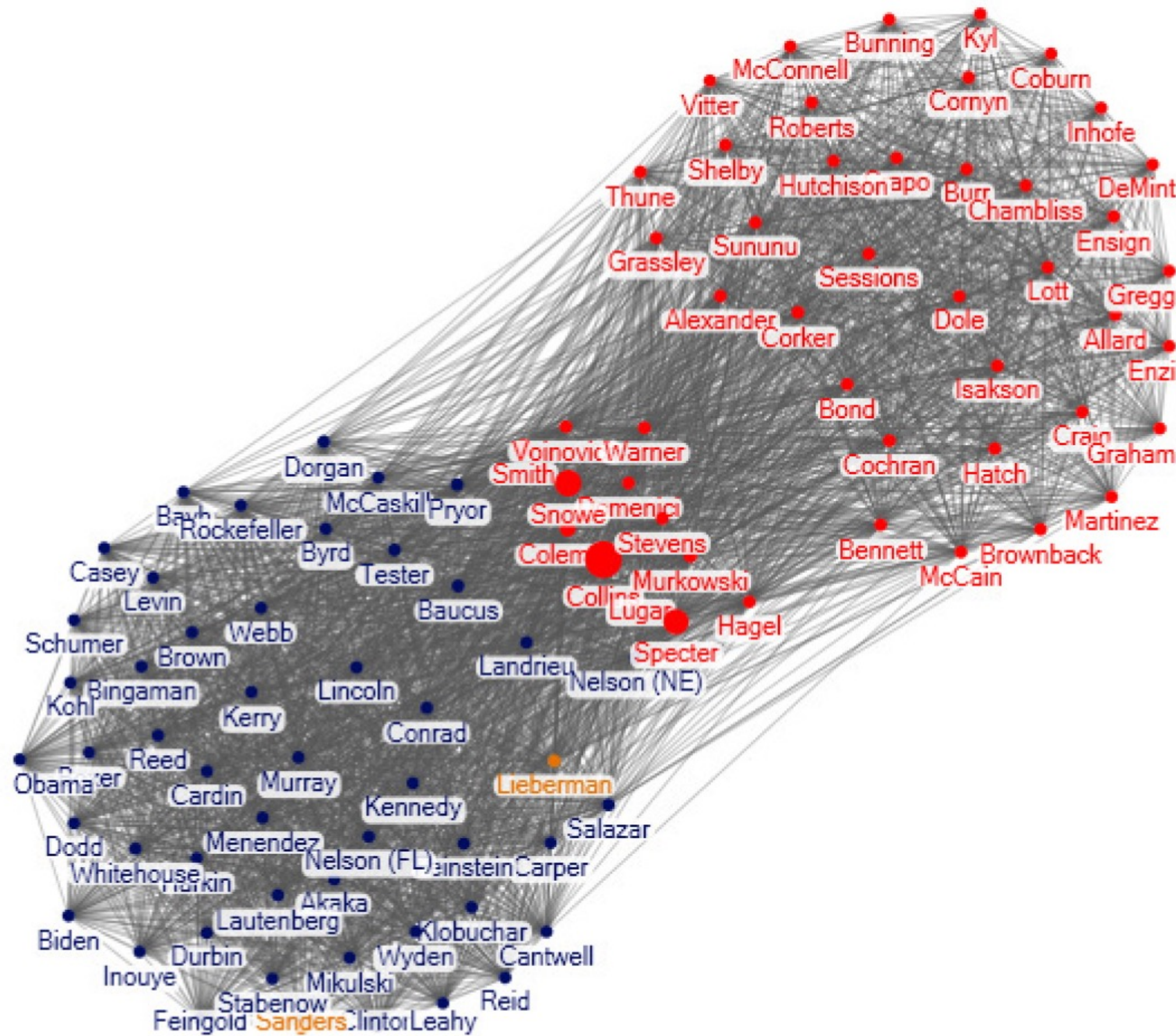








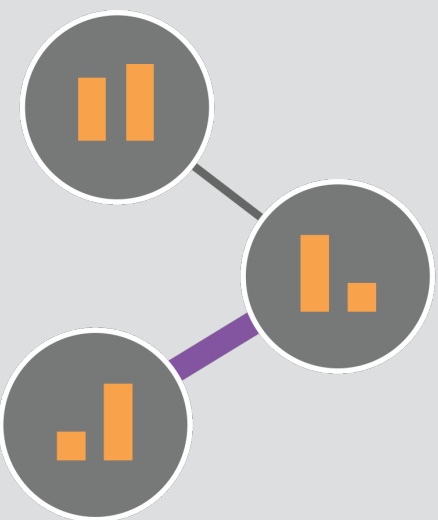
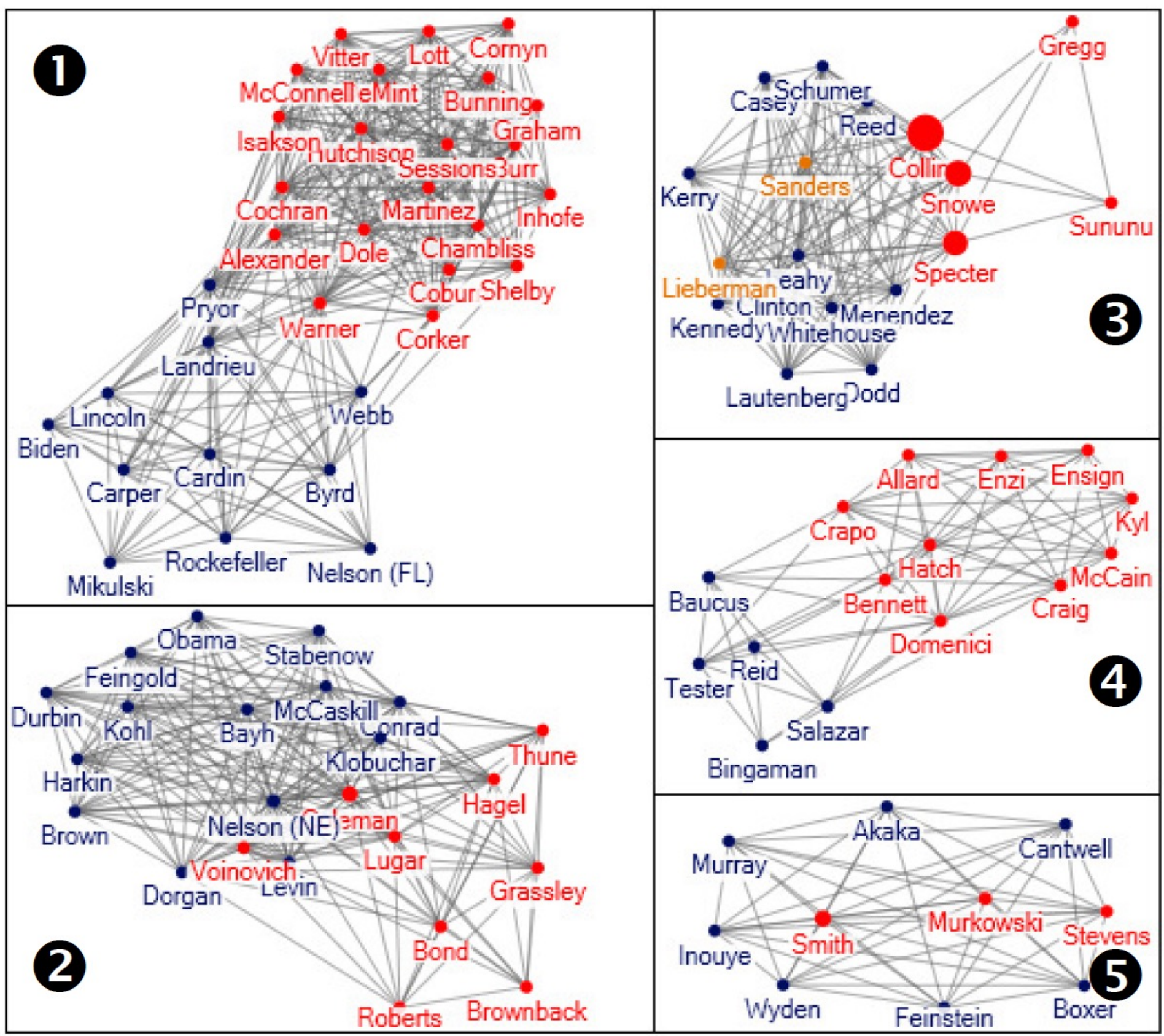
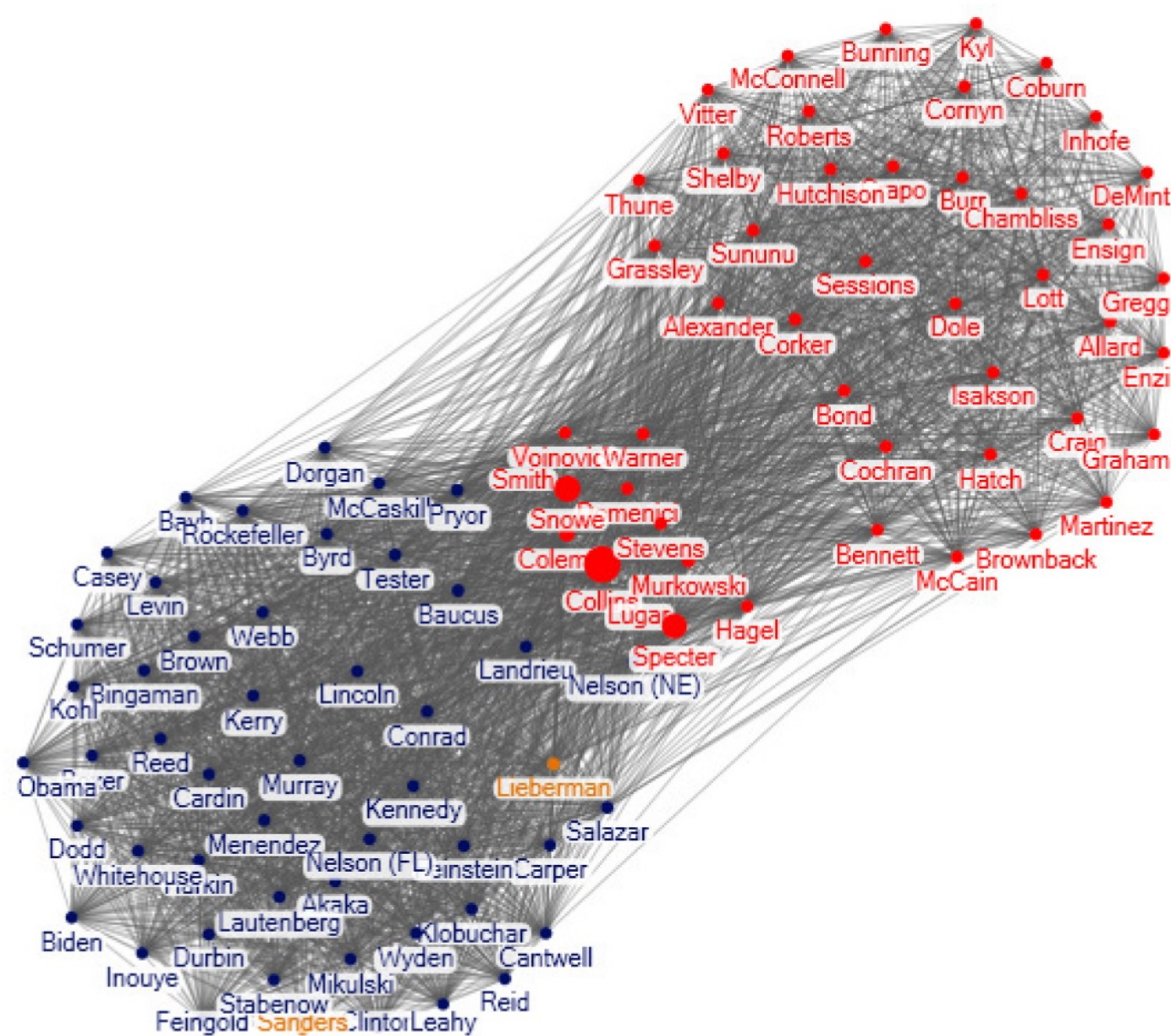
# Group-in-a-box *Rodrigues et al. 2011*



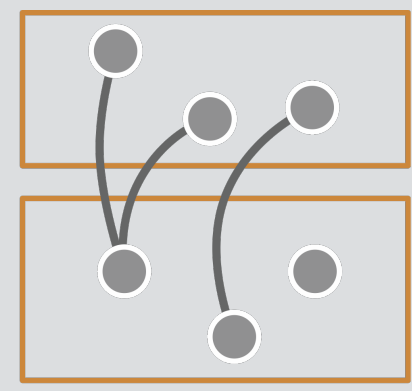
On-Node / On-Edge  
Encoding



# Group-in-a-box *Rodrigues et al. 2011*



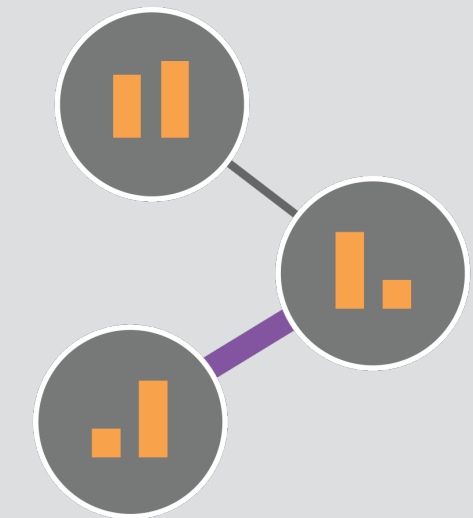
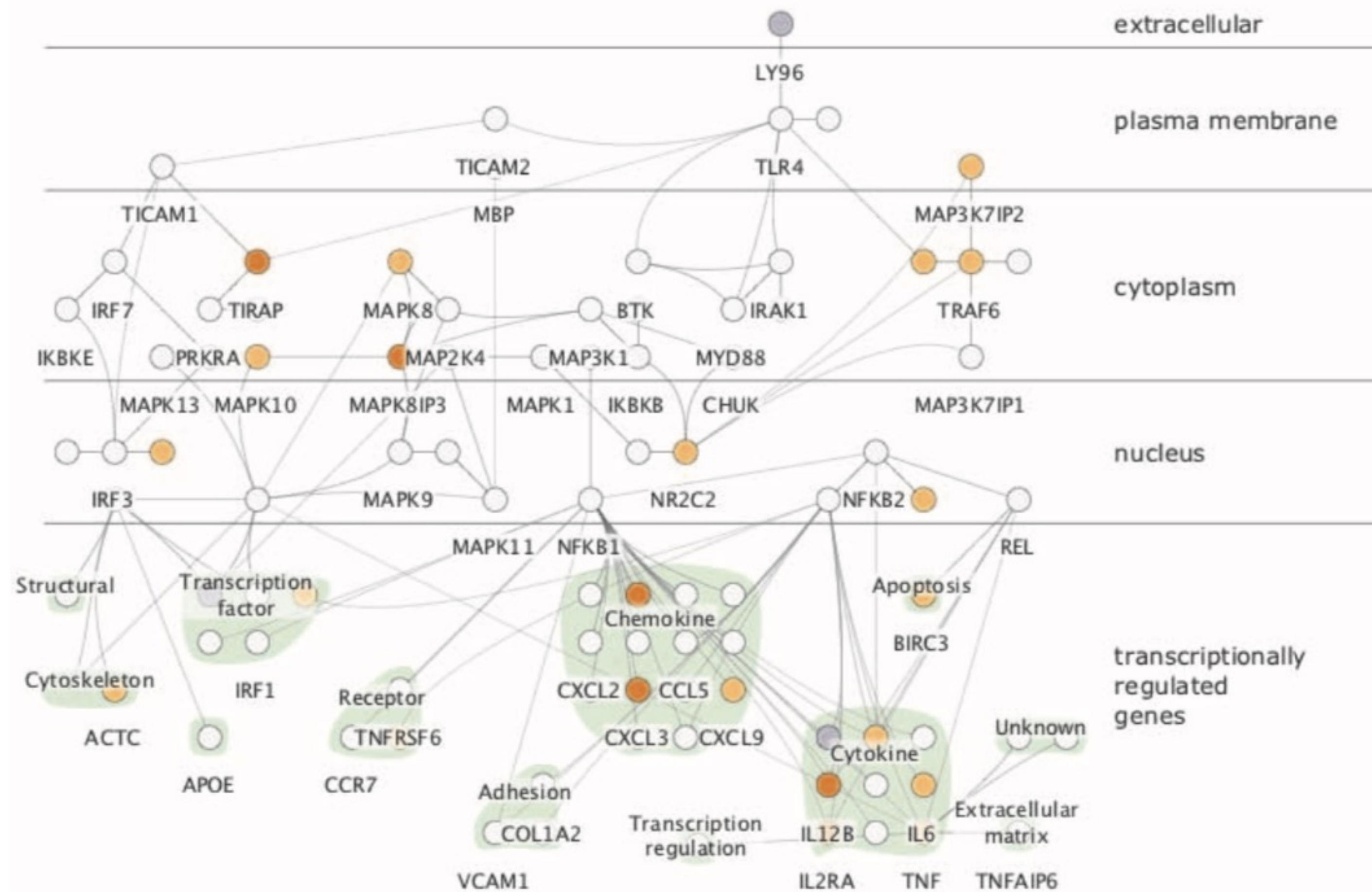
On-Node / On-Edge  
Encoding



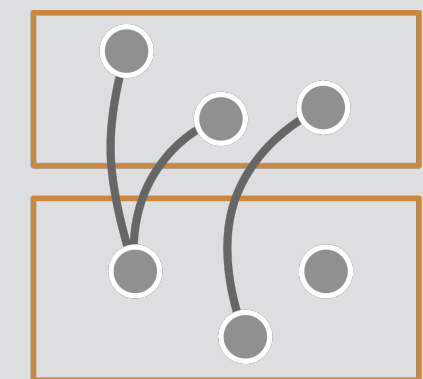
Attribute-Driven  
Faceting



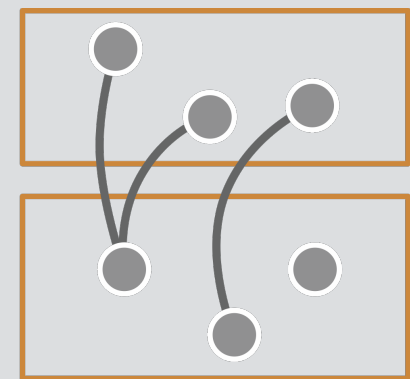
# Cerebral Barsky et al. 2008



On-Node / On-Edge  
Encoding



Attribute-Driven  
Faceting

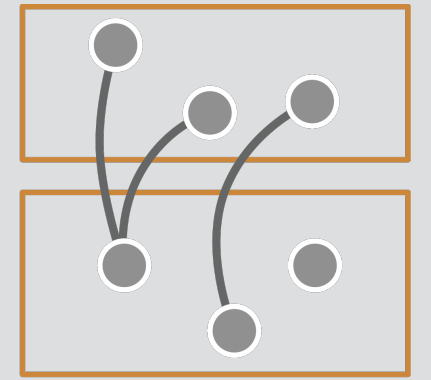


Attribute-Driven  
Faceting





Well suited for networks with different node types or with an important categorical or set-like attribute.



Attribute-Driven  
Faceting

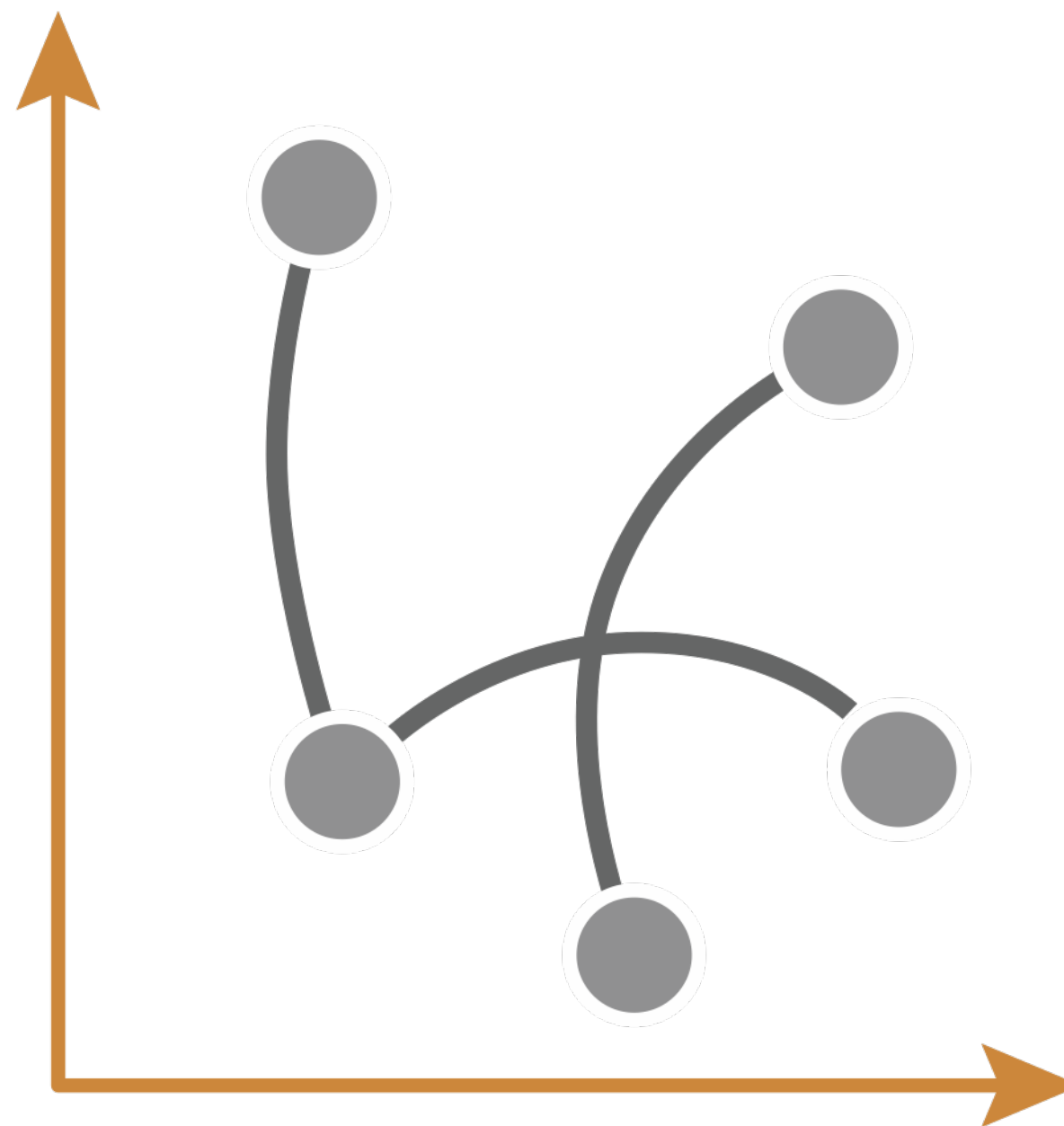


Less scalable with respect to the number of nodes and network density than node-link layouts.

Neighborhoods, paths, and clusters are not easily visible if they span different facets.

*Recommended for networks where nodes can be separated into groups easily and where these groups are central to the analysis*

# Attribute-Driven Positioning

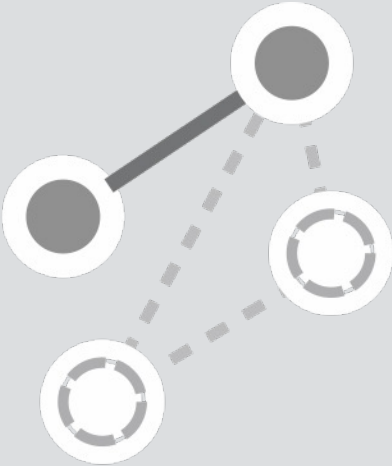
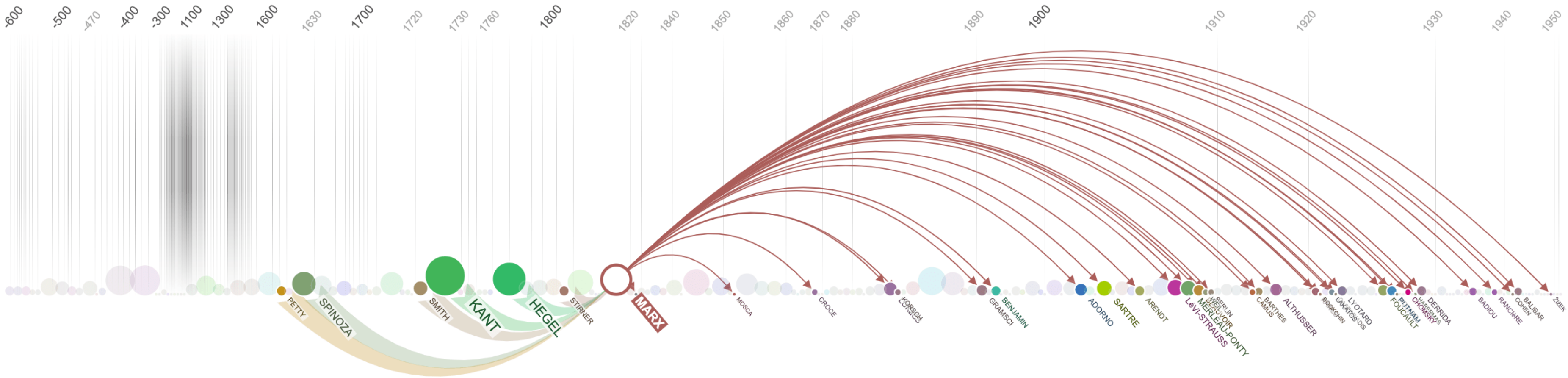




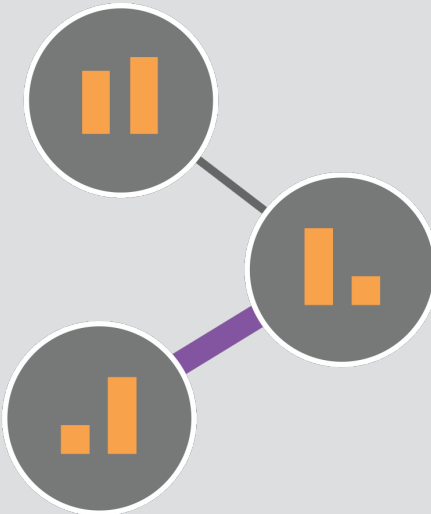




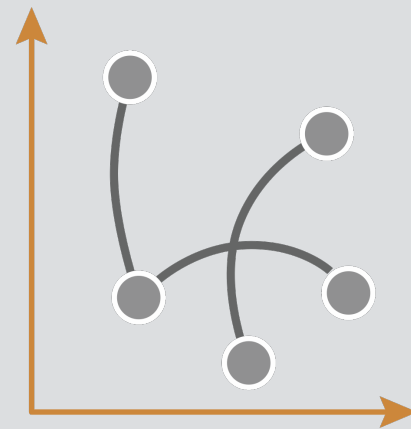
# Edge Map *Dork et al. 2011*



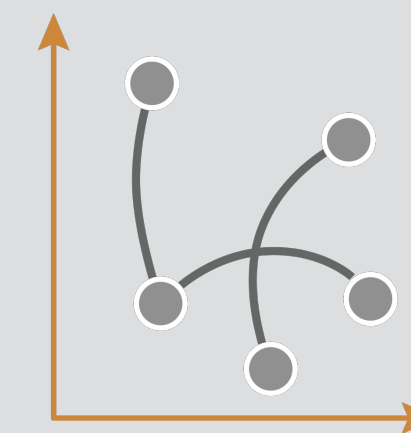
Querying and Filtering



On-Node / On-Edge  
Encoding



Attribute-Driven  
Positioning 71



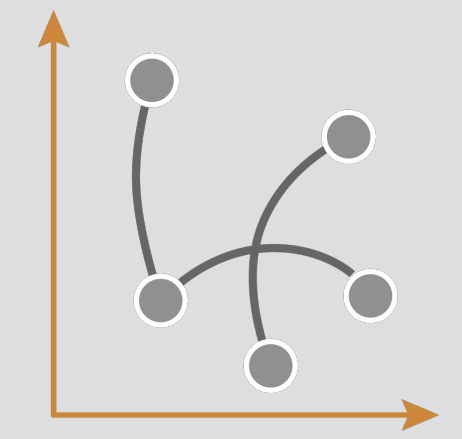
Attribute-Driven  
Positioning



Well suited for quantitative attributes



Does not lend itself well to visualizing the topology of the network.



Attribute-Driven  
Positioning

*Recommended for smaller, sparse networks where relationships between node attributes are paramount to the analysis task, and topological features only provide context*




# Tools and Applications

For graphic designer and developers

developer



 Observable

[Teams](#) [Demo](#) [Fork](#) [Sign in](#)

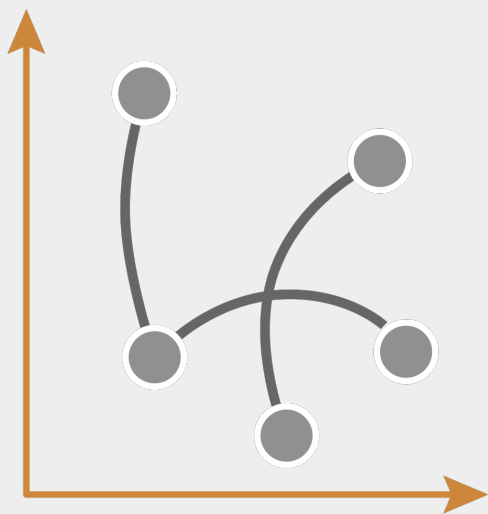
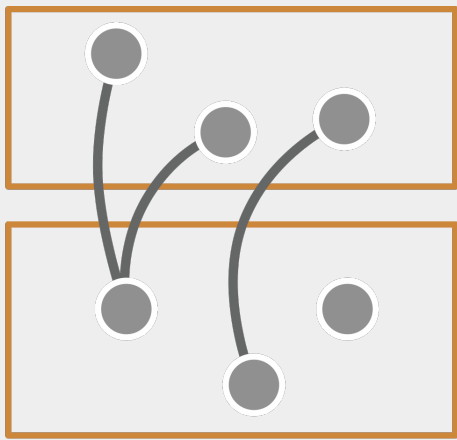
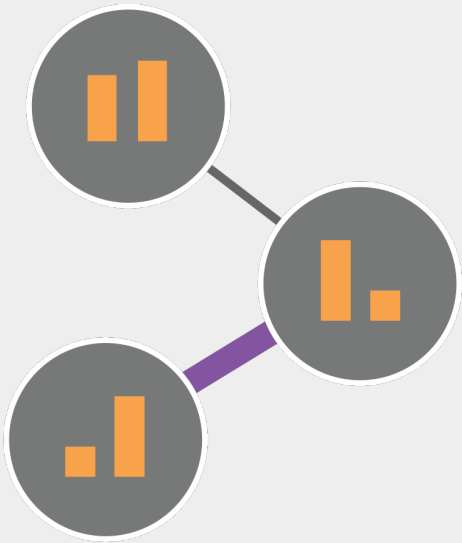
Welcome. This is [live code](#)! Click the left margin to view or edit. **D3** · Nov 15, 2017  
Bring your data to life.  
By  **Mike Bostock**Listed in d3-drag, d3-force, and Visualization  178 forks

# Force-Directed Graph

This network of character co-occurrence in *Les Misérables* is positioned by simulated forces using [d3-force](#). See also a [disconnected graph](#), and compare to [WebCoLa](#).



```
chart = {  
  const links = data.links.map(d => Object.create(d));  
  const nodes = data.nodes.map(d => Object.create(d));  
  
  const simulation = d3.forceSimulation(nodes)  
    .force("link", d3.forceLink(links).id(d => d.id))  
    .force("charge", d3.forceManyBody())  
    .force("center", d3.forceCenter(width / 2, height / 2));  
  
  const svg = d3.create("svg")
```



developer

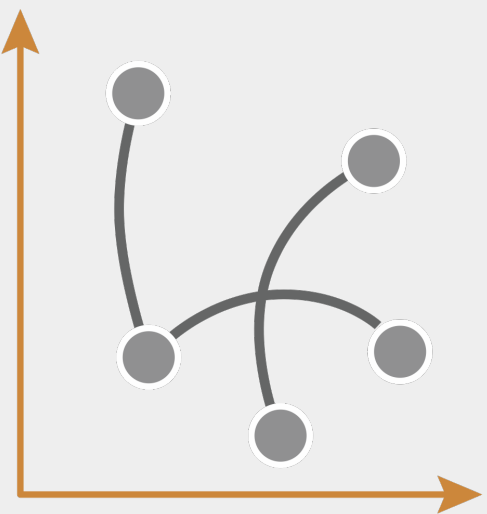
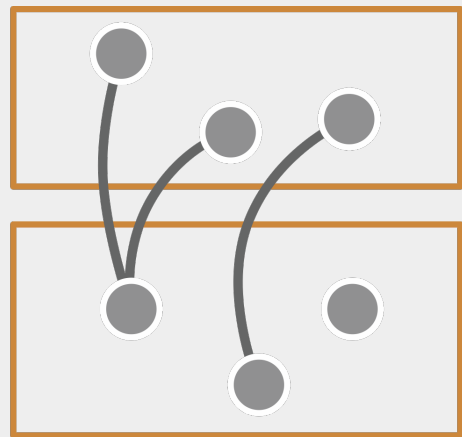
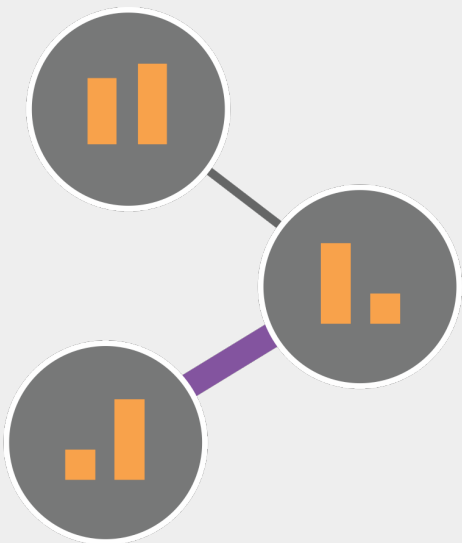
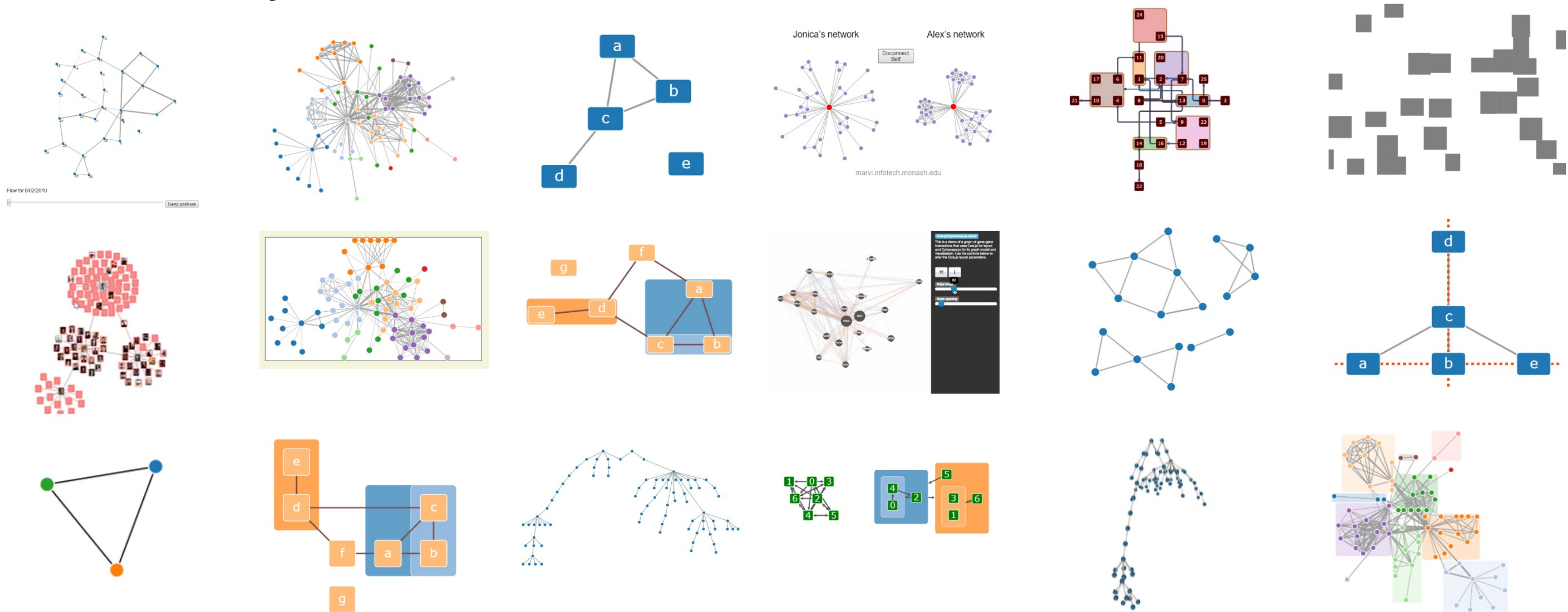


Cola.js (A.K.A. "WebCoLa") is an open-source JavaScript library for arranging your HTML5 documents and diagrams using constraint-based optimization techniques.

[Overview](#) [Wiki](#) [API](#) [Source](#)

cola.js

Constraint-Based Layout in the Browser







GGRAPH 1.0.2.9999



Reference

Getting Started ▾

Articles ▾

News ▾

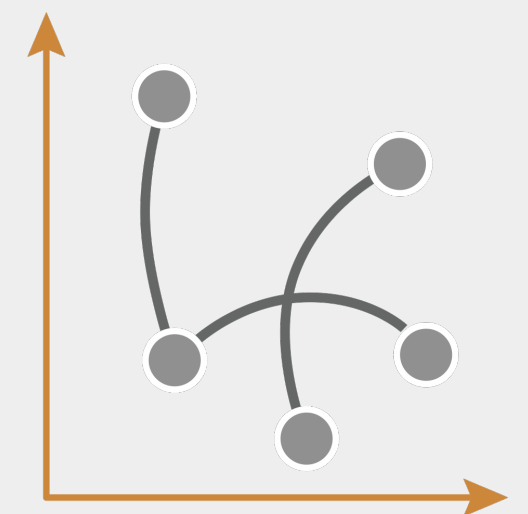
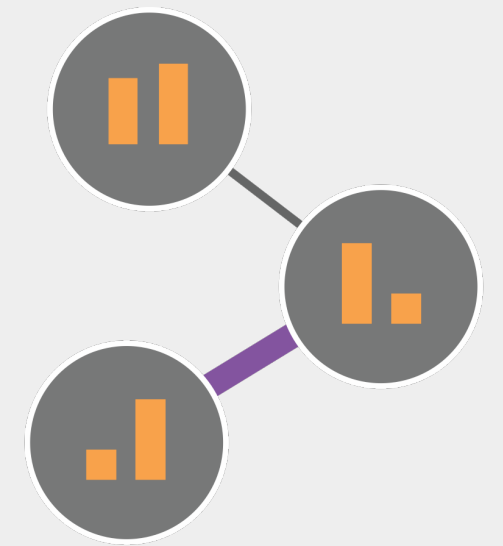
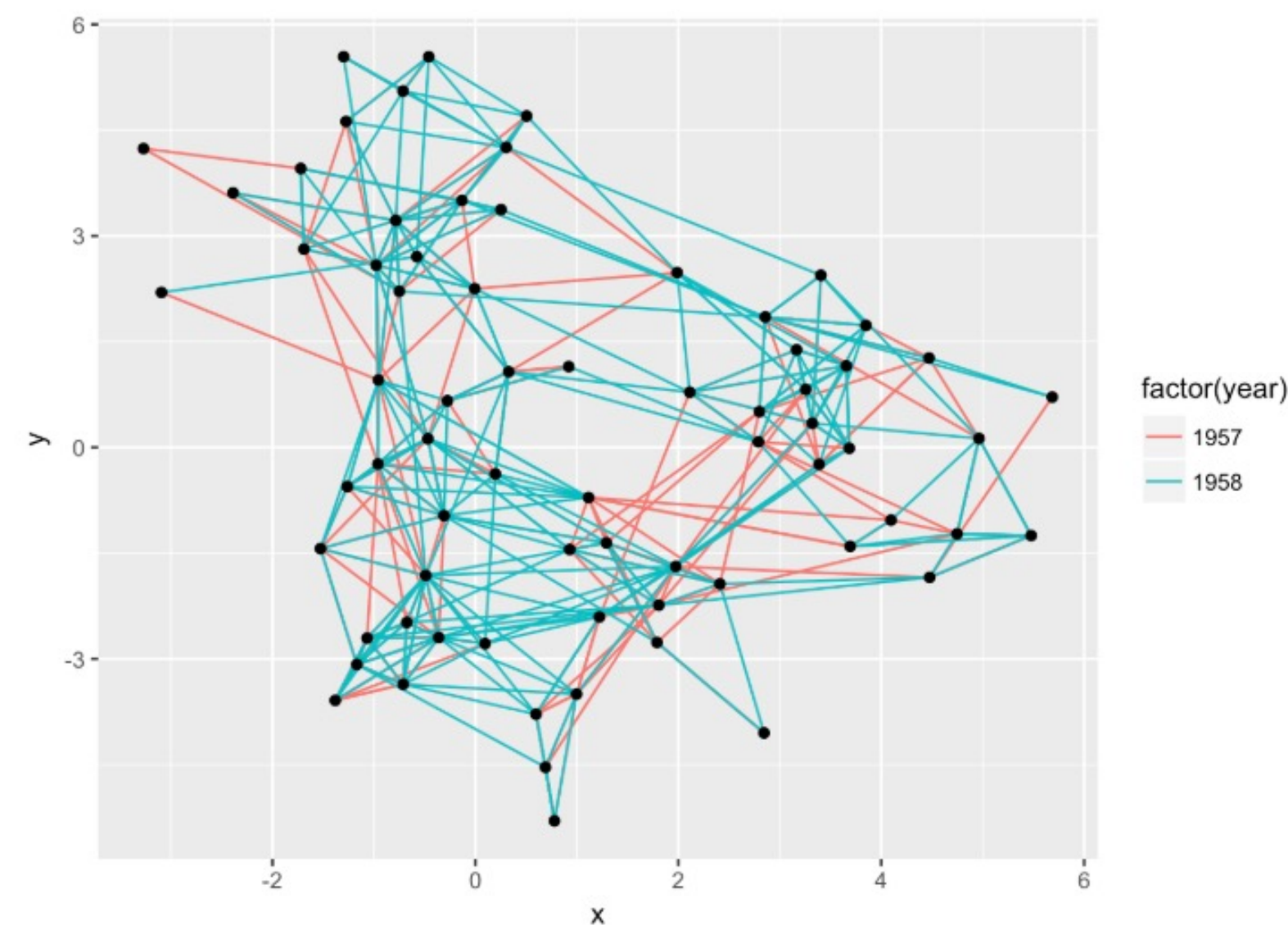
# ggraph

/dʒiː.dʒɪˈrɑːf/ (or g-giraffe)

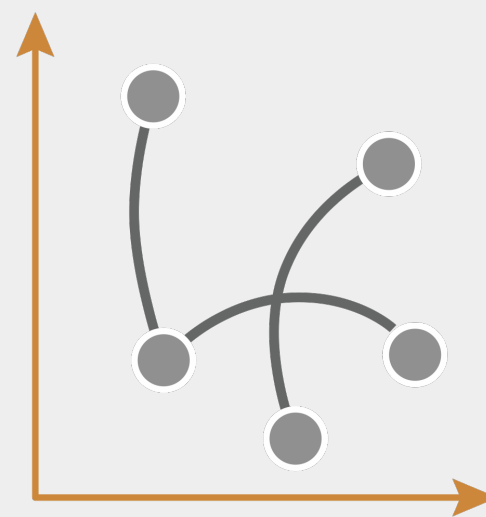
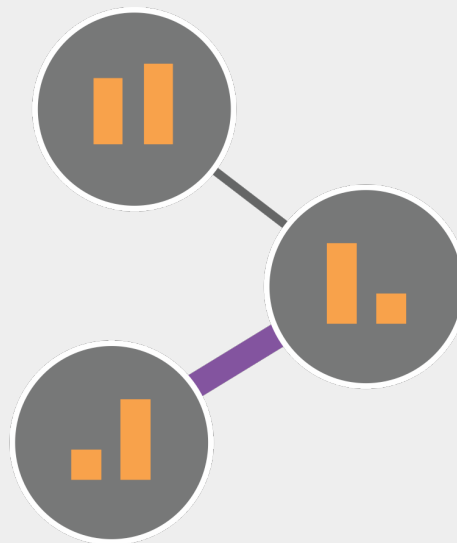
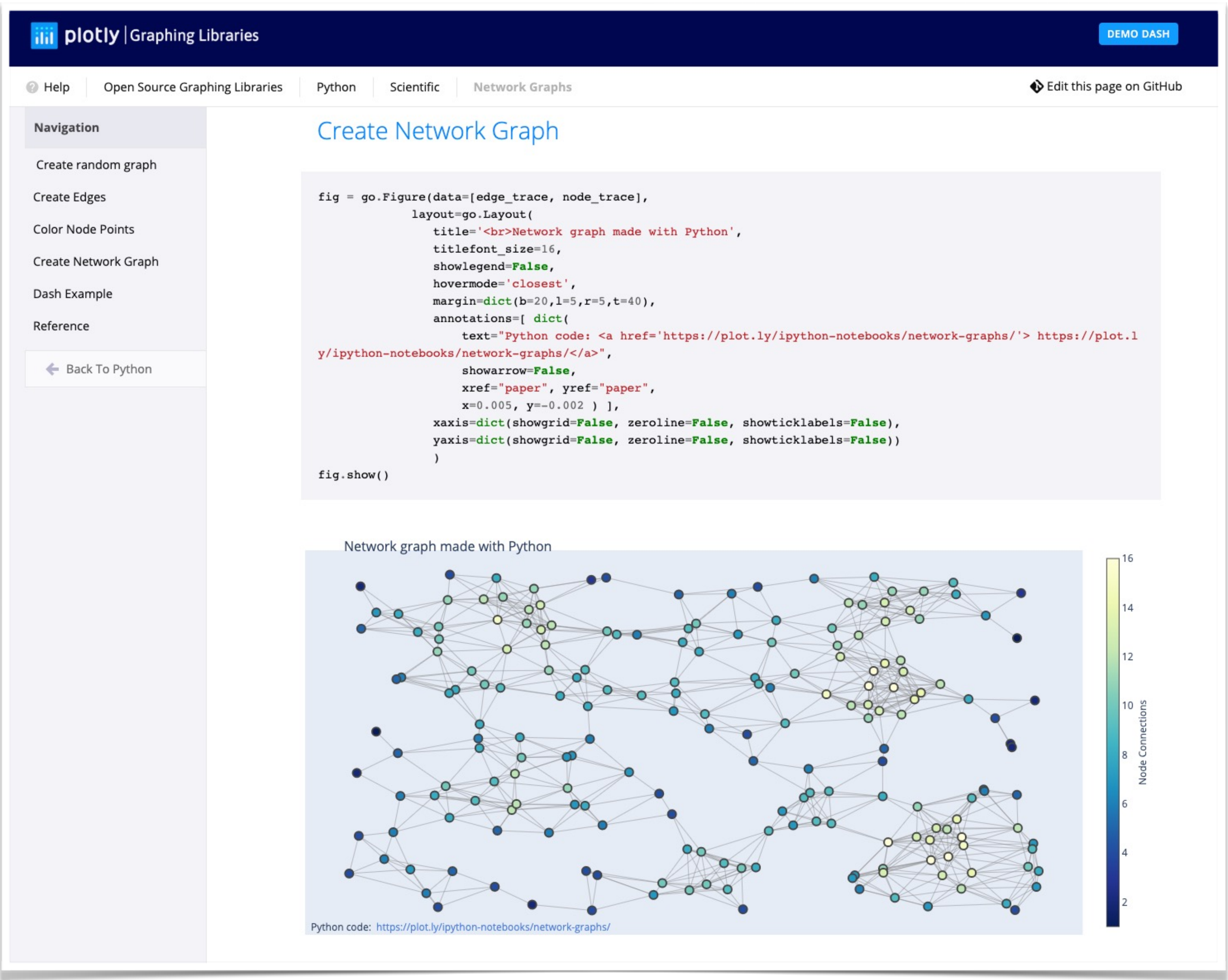


## A grammar of graphics for relational data

`ggraph` is an extension of `ggplot2` aimed at supporting relational data structures such as networks, graphs, and trees. While it builds upon the foundation of `ggplot2` and its API it comes with its own self-contained set of geoms, facets, etc., as well as adding the concept of *layouts* to the grammar.



developer





developer



## NetworkX

### Stable (notes)

2.3 — April 2019

[download](#) | [doc](#) | [pdf](#)

### Latest (notes)

2.4 development

[github](#) | [doc](#) | [pdf](#)

### Archive

### Contact

[Mailing list](#)

[Issue tracker](#)



## Software for complex networks

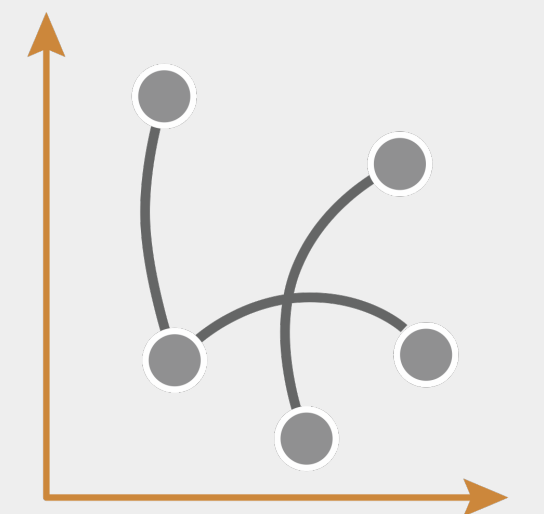
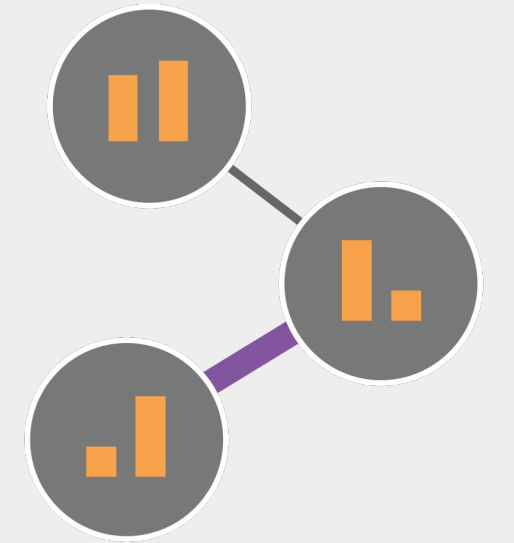
NetworkX is a Python package for the creation, manipulation, and study of the structure, dynamics, and functions of complex networks.



### Features

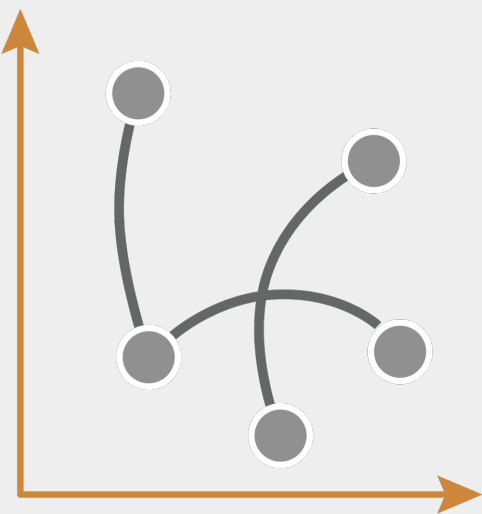
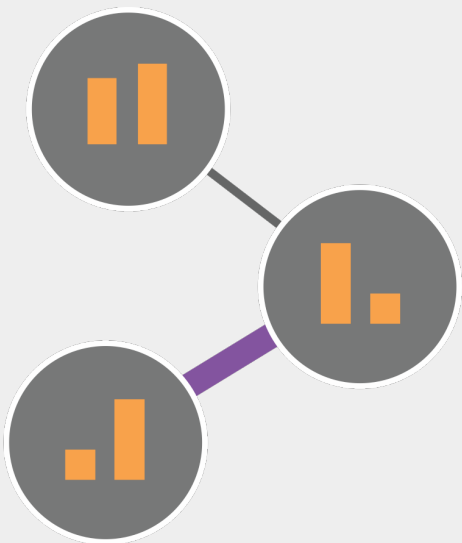
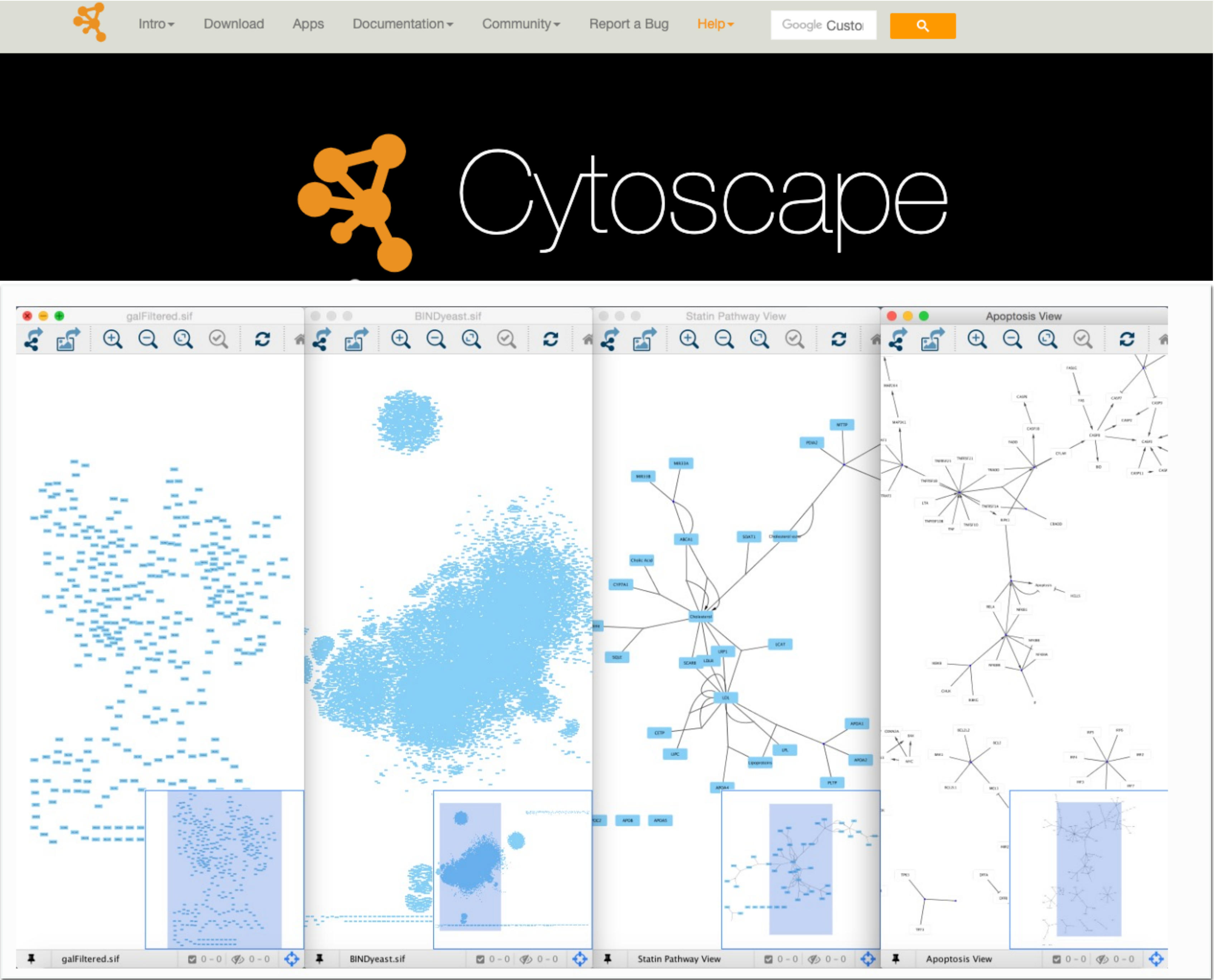
- Data structures for graphs, digraphs, and multigraphs
- Many standard graph algorithms
- Network structure and analysis measures
- Generators for classic graphs, random graphs, and synthetic networks
- Nodes can be "anything" (e.g., text, images, XML records)
- Edges can hold arbitrary data (e.g., weights, time-series)
- Open source [3-clause BSD license](#)
- Well tested with over 90% code coverage
- Additional benefits from Python include fast prototyping, easy to teach, and multi-platform

©2014-2019, NetworkX developers. | Powered by [Sphinx 2.0.1](#) & [Alabaster 0.7.12](#)



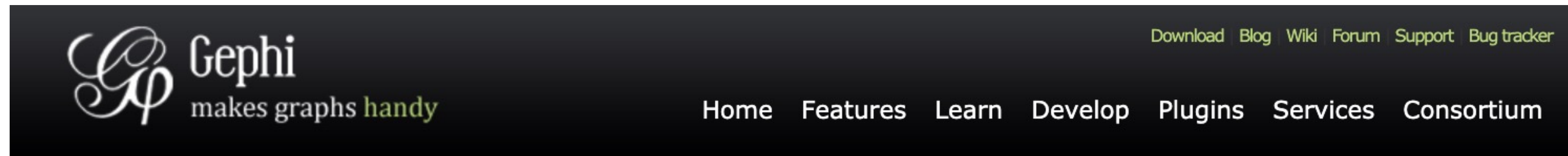


graphic  
designer





graphic  
designer



## The Open Graph Viz Platform

Gephi is the leading visualization and exploration software for all kinds of graphs and networks. Gephi is open-source and free.

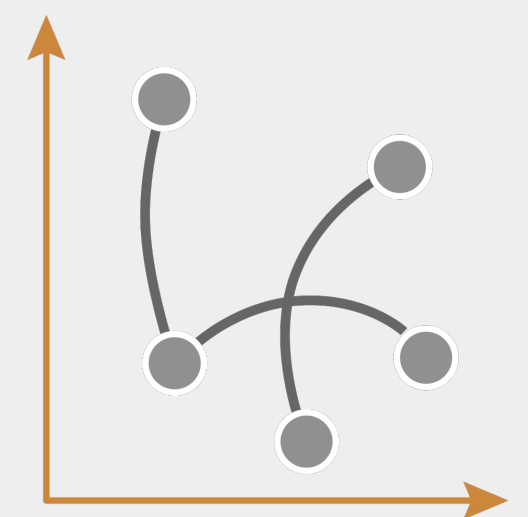
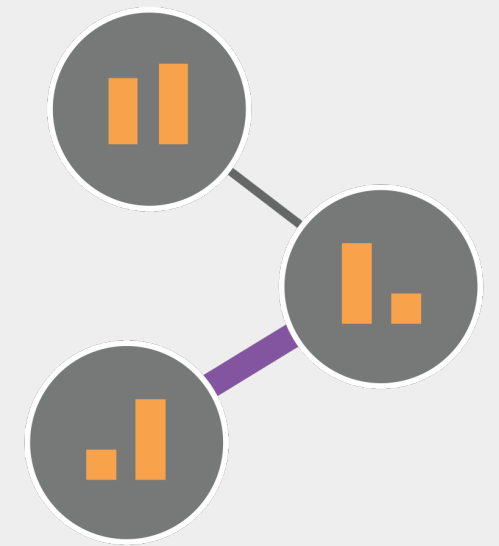
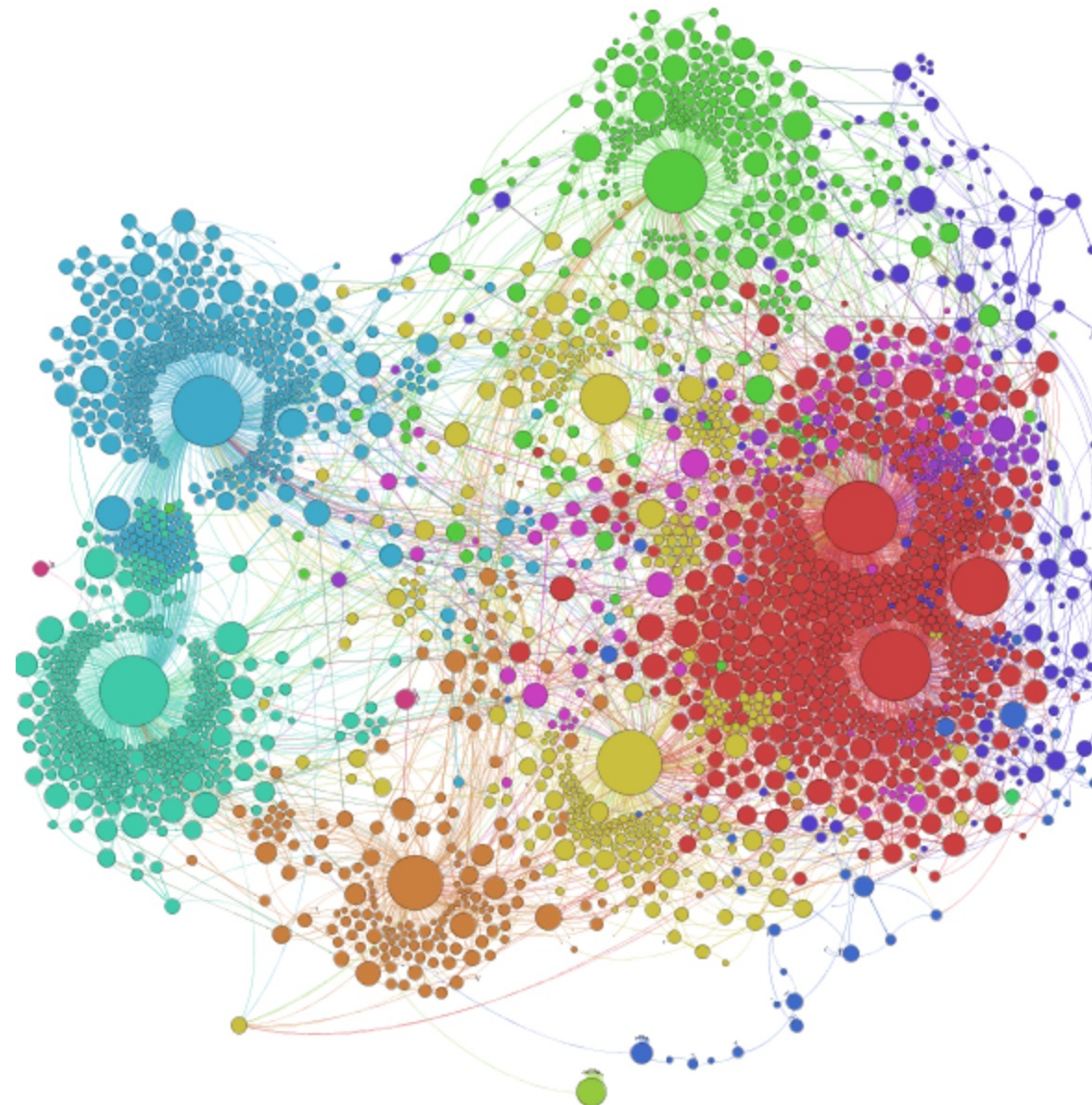
Runs on Windows, Mac OS X and Linux.

[Learn More on Gephi Platform »](#)



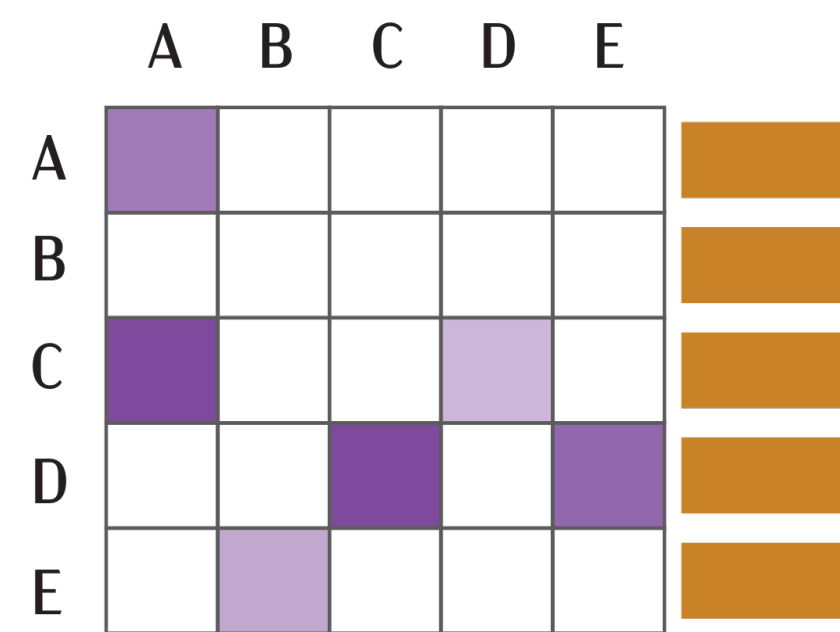
[Release Notes](#) | [System Requirements](#)

- [Features](#)
- [Screenshots](#)
- [Quick start](#)
- [Videos](#)

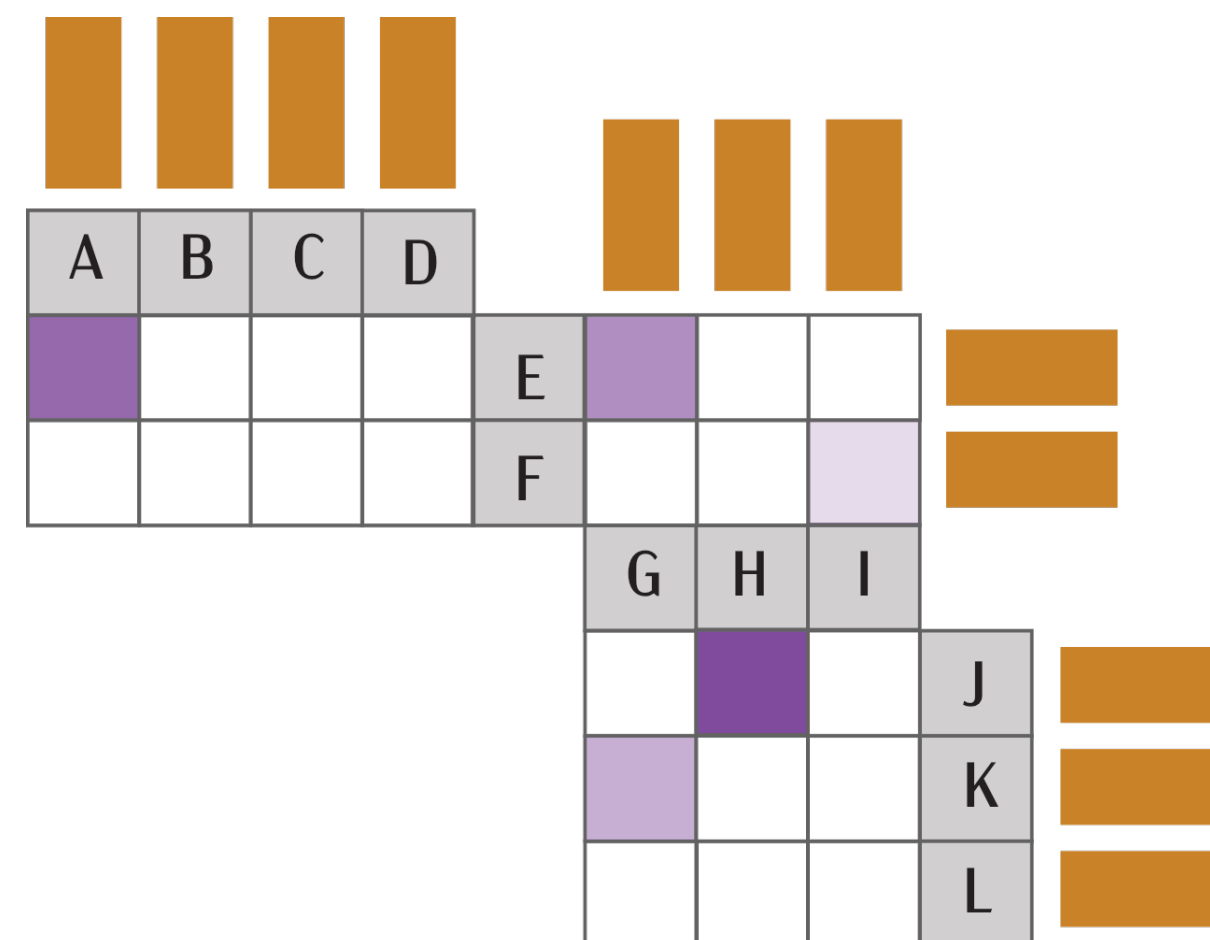




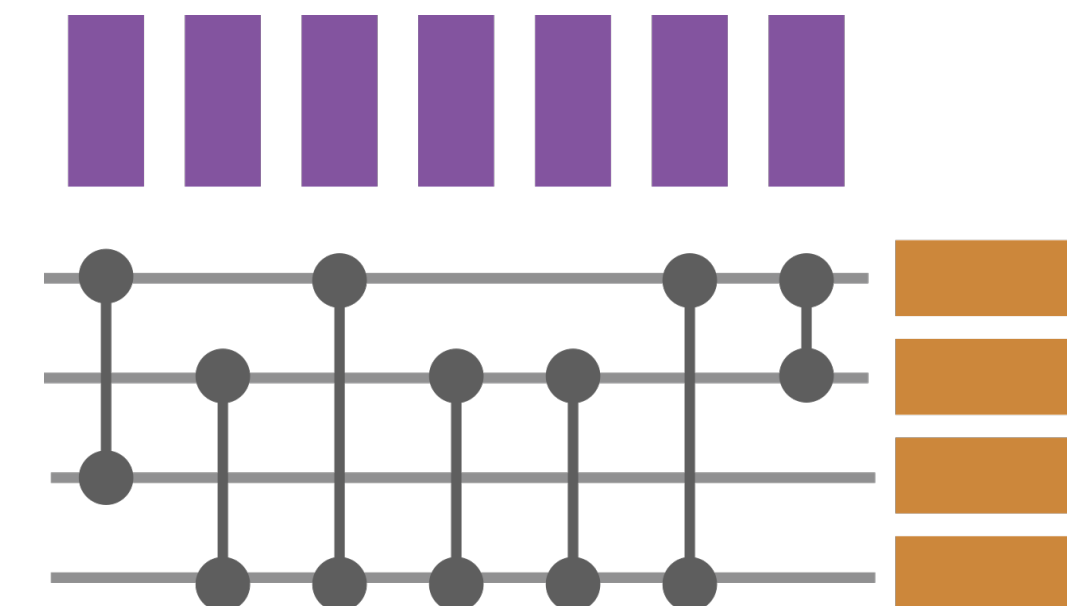
# Tabular Layouts



Adjacency  
Matrix



Quilts

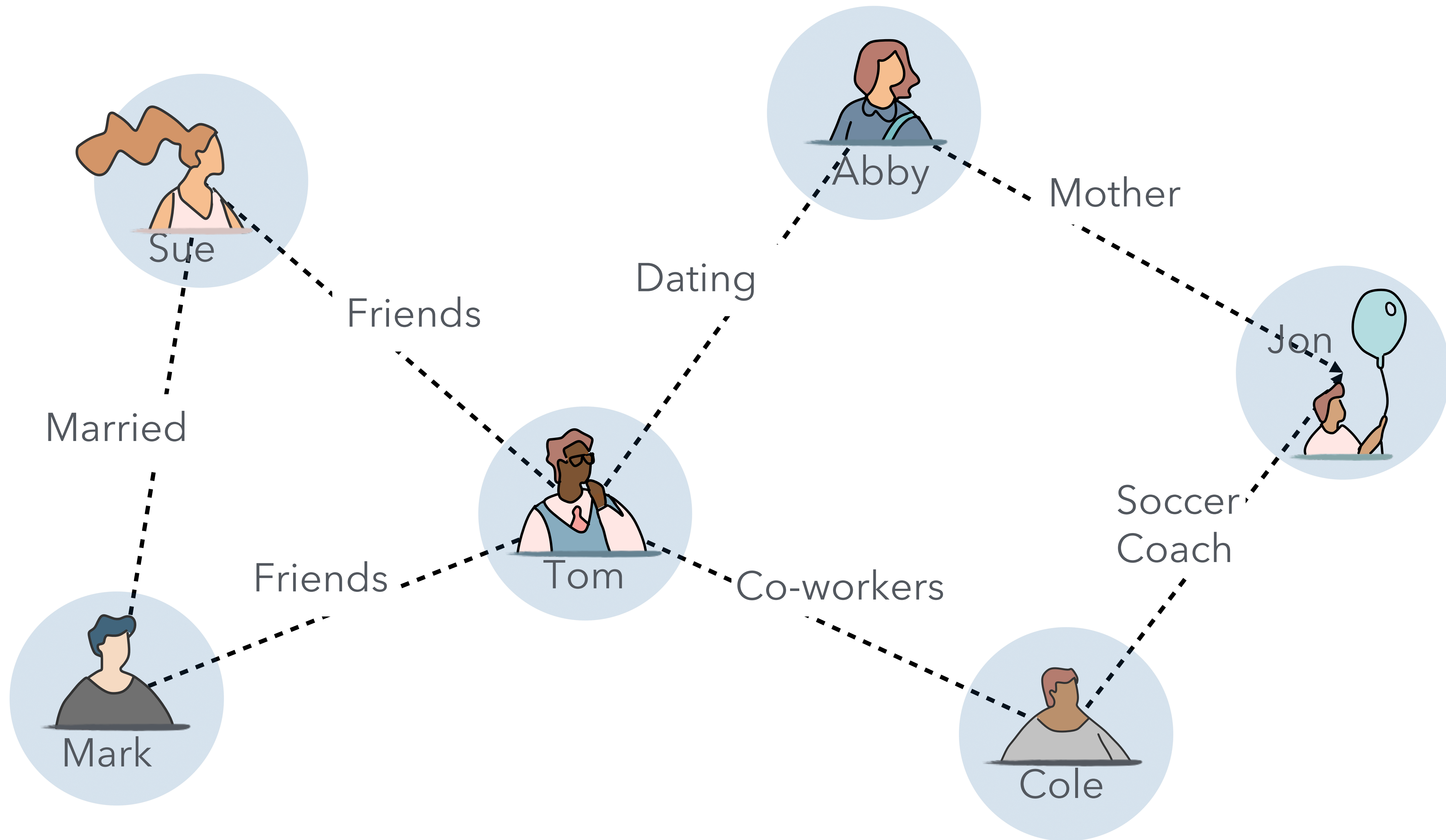


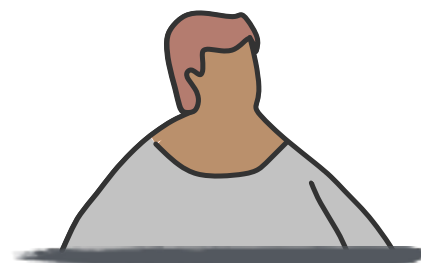
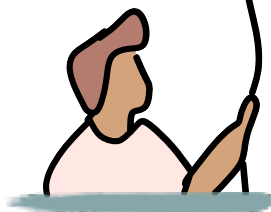
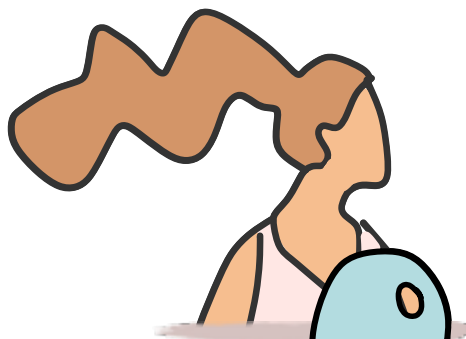
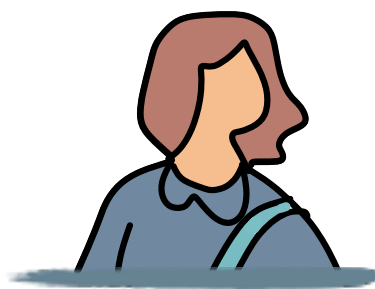
BioFabric



# Adjacency Matrix

	A	B	C	D	E	
A						
B						
C						
D						
E						





.....

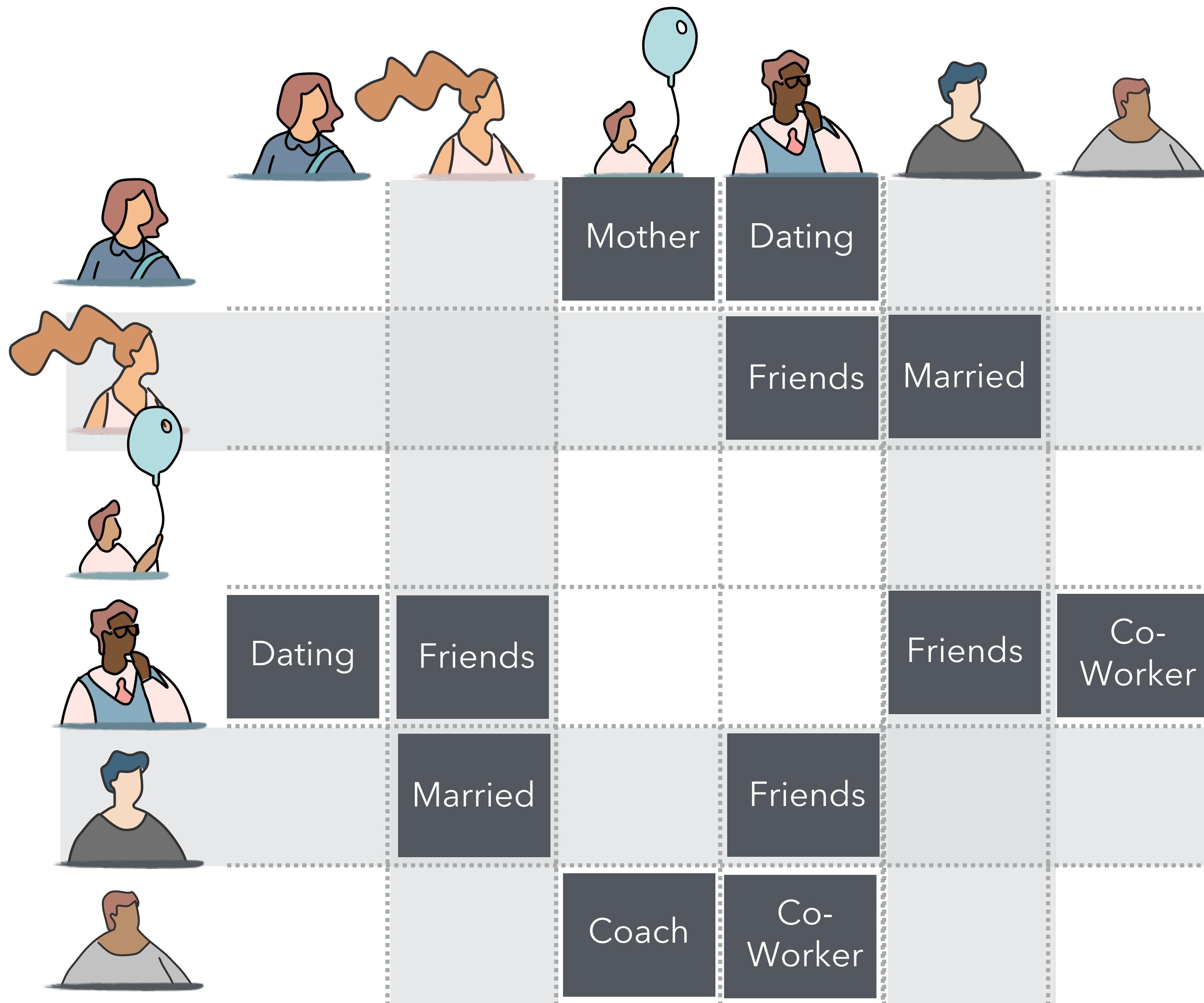
.....

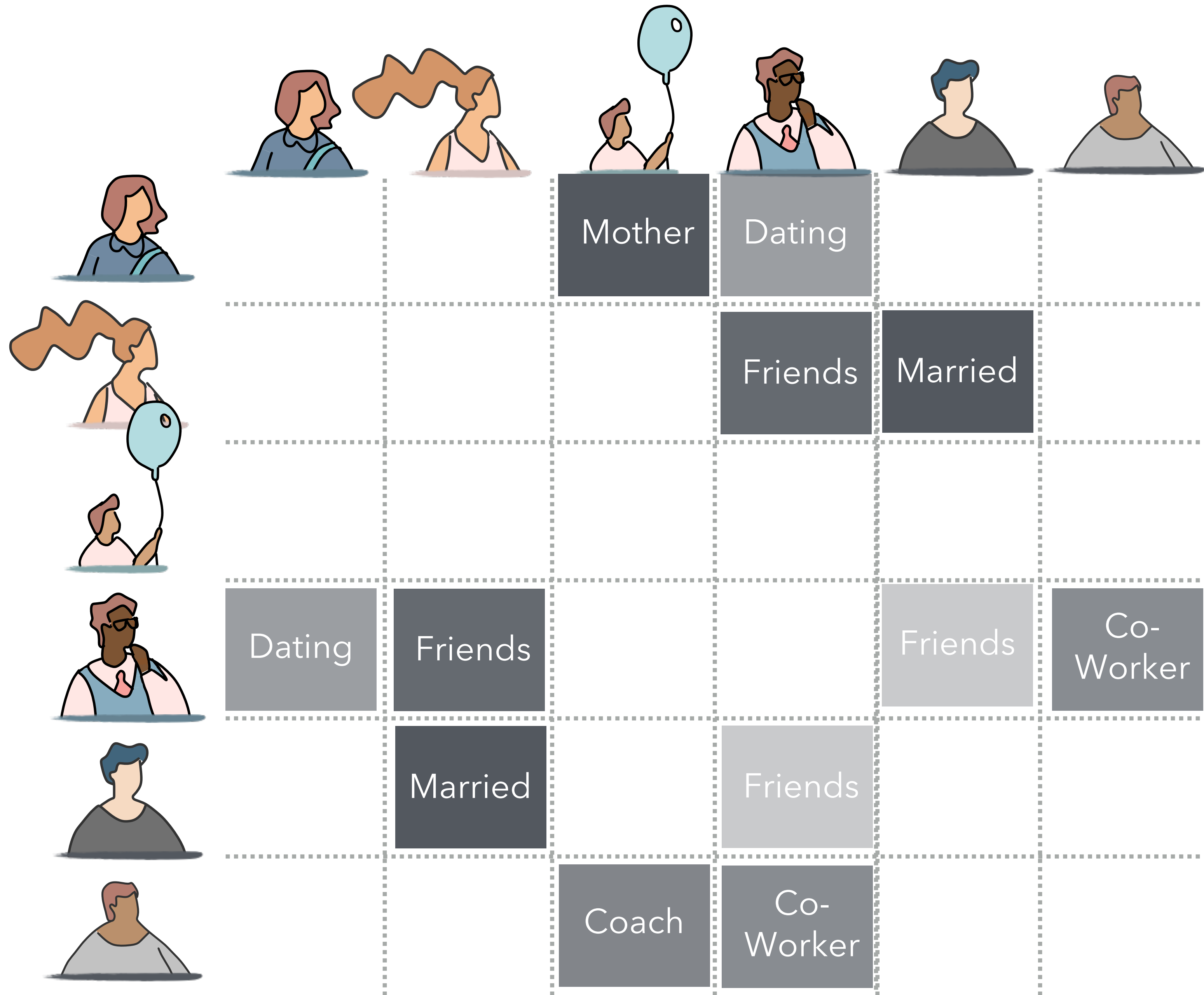
.....

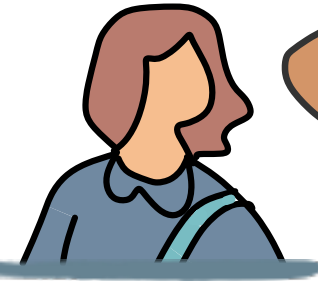
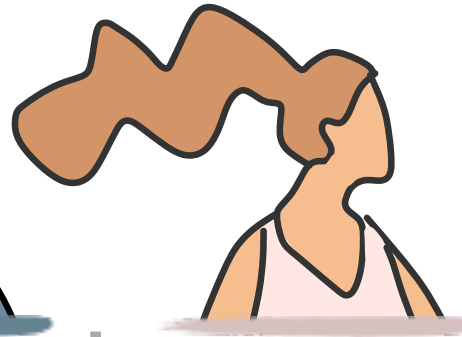
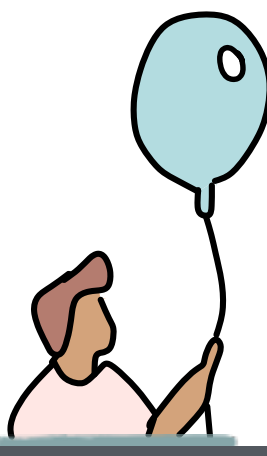

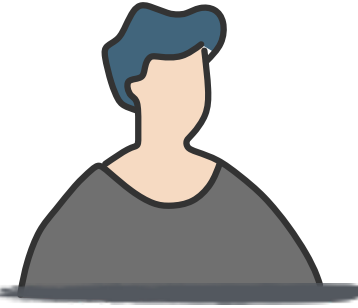
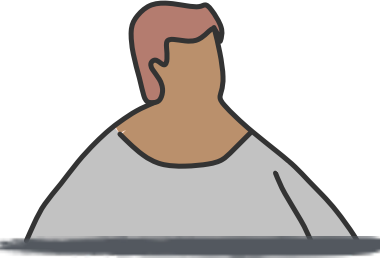
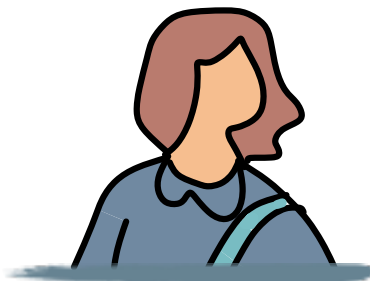
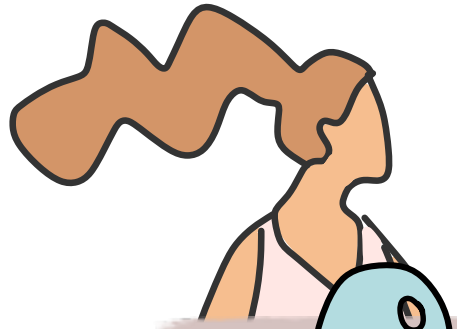
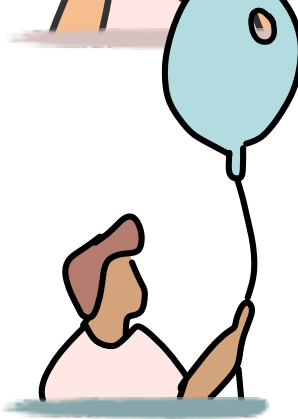

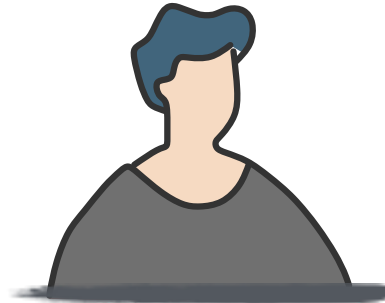
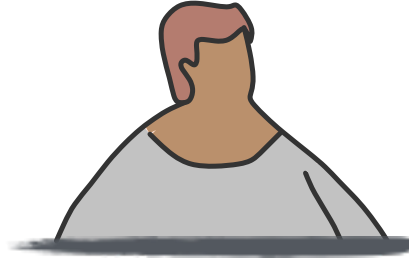
.....

.....


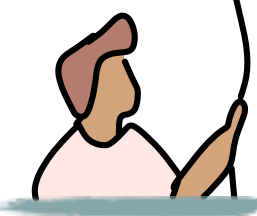

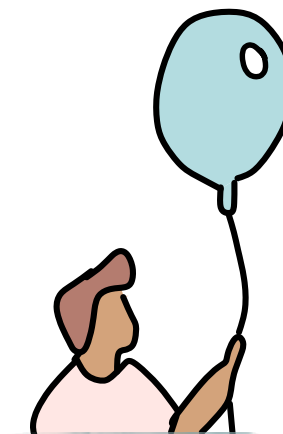
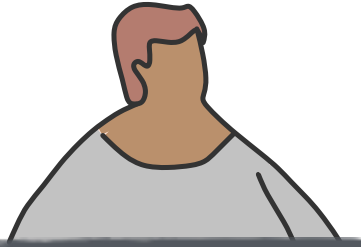
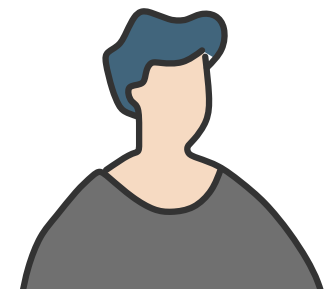
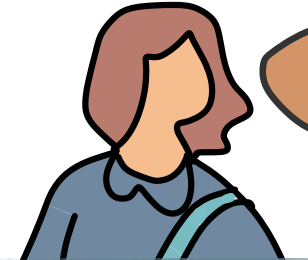

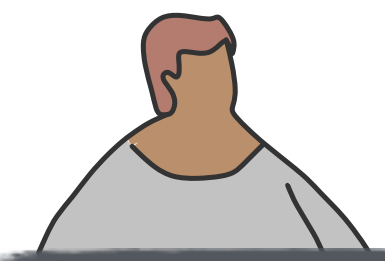
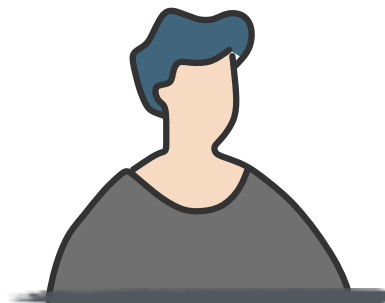
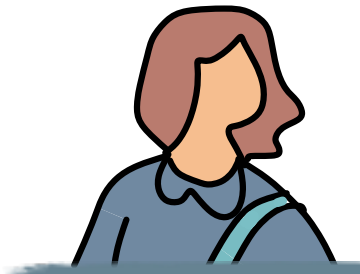



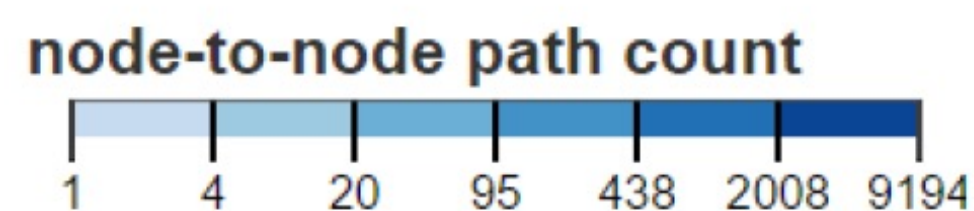
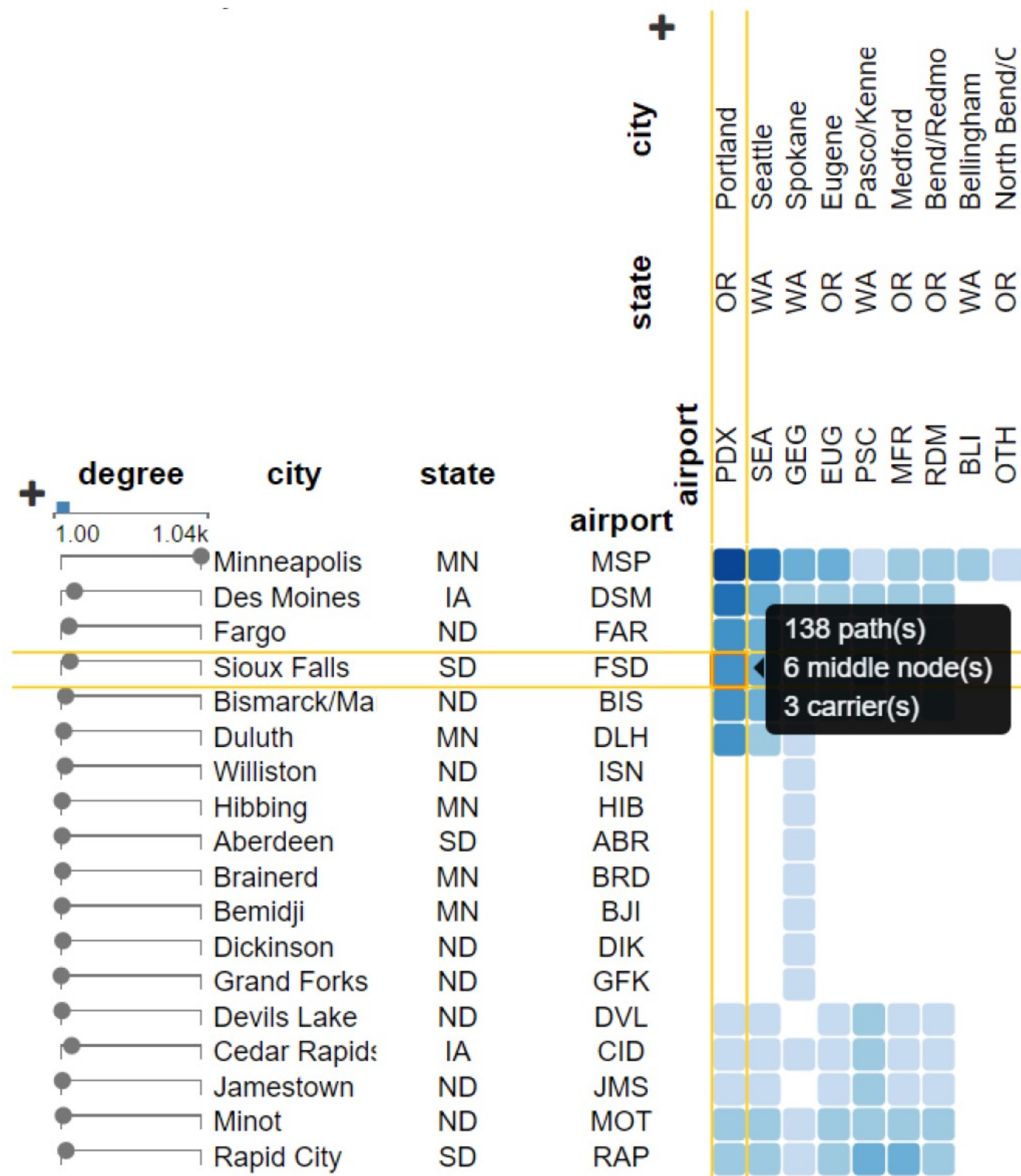




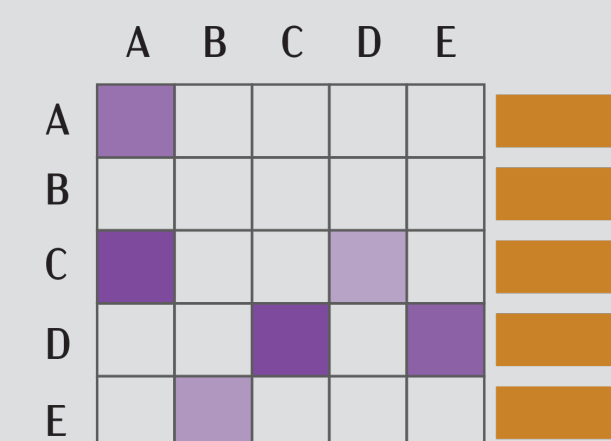
							Name	Beverage	Day 1
			Mother	Dating			Abby	Port	1
				Friends	Married		Sue	Coke	0
							Jon	Coke	4
	Dating	Friends			Friends	Co-Worker	Tom	Beer	5
		Married		Friends			Mark	Beer	2
			Coach	Co-Worker			Cole	Port	3



						Name	Beverage	Day 1
 					 	Tom	Beer	5
			Co-Worker	Friends	Dating	Friends	Jon	Coke
	Co-Worker	Coach				Cole	Port	3
	Friends				Married	Mark	Beer	2
	Dating	Mother				Abby	Port	1
	Friends			Married		Sue	Coke	0

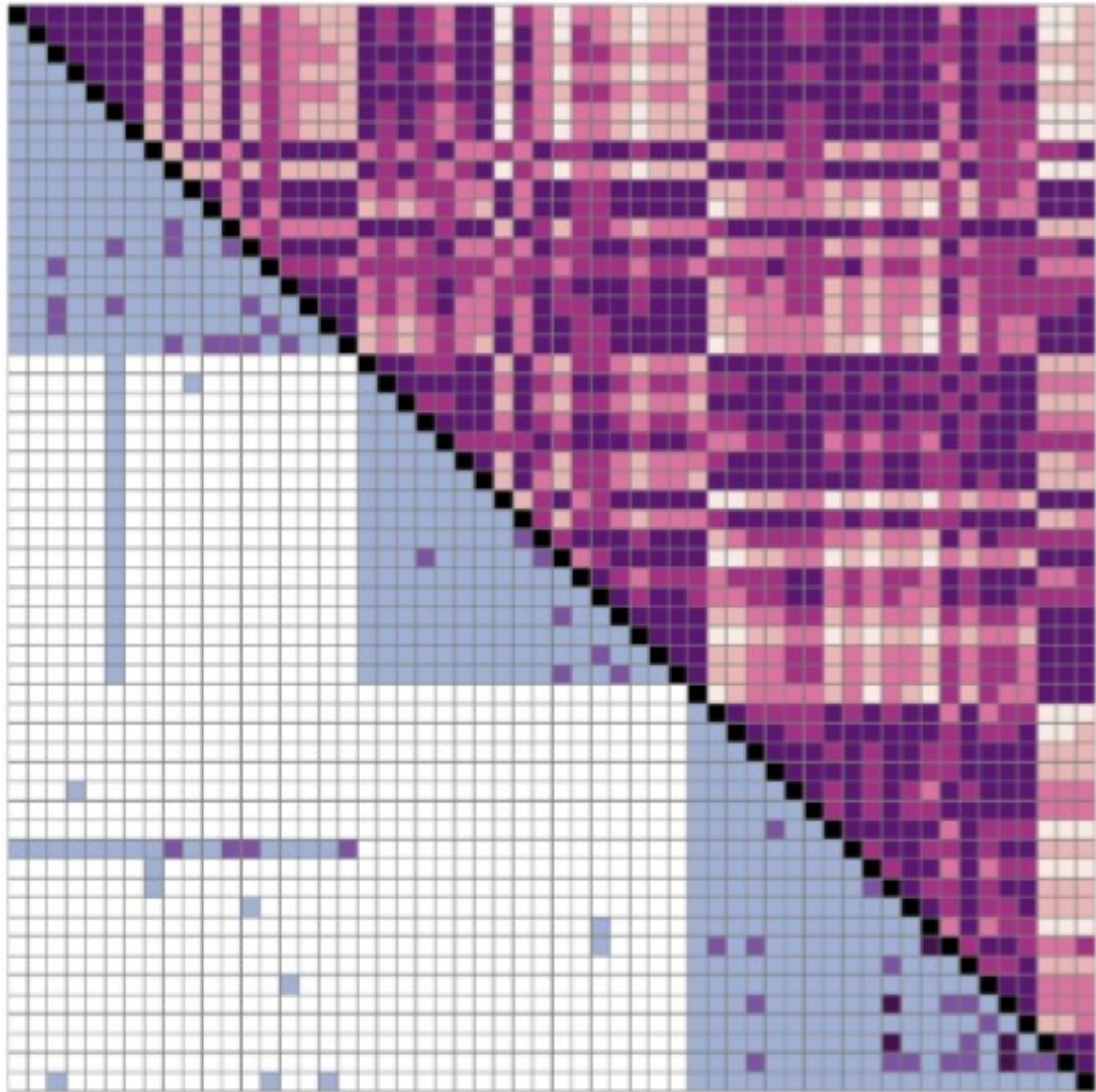


Kerzner et al, 2017

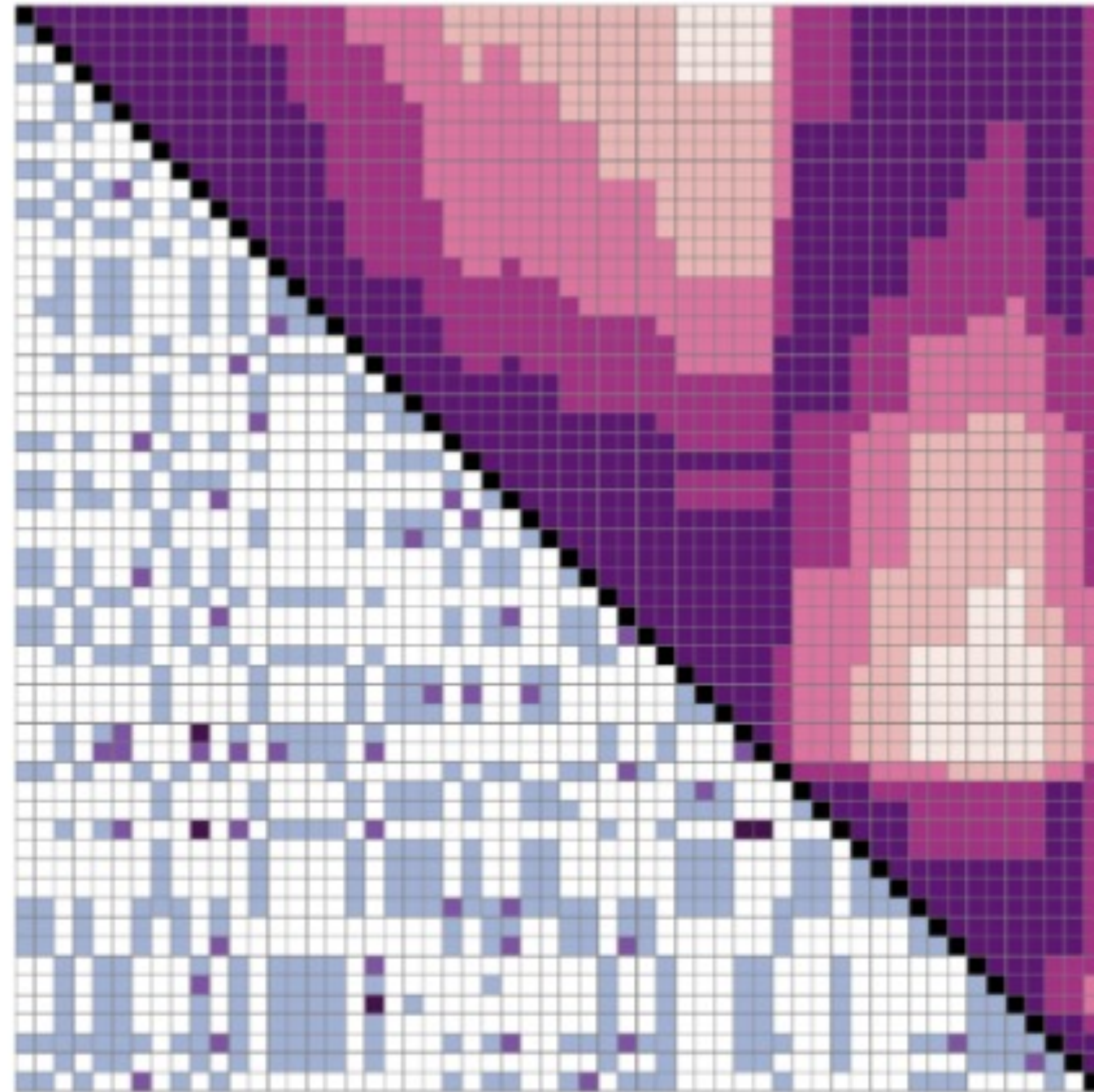


Adjacency  
Matrix





(a) Sorted by structure.



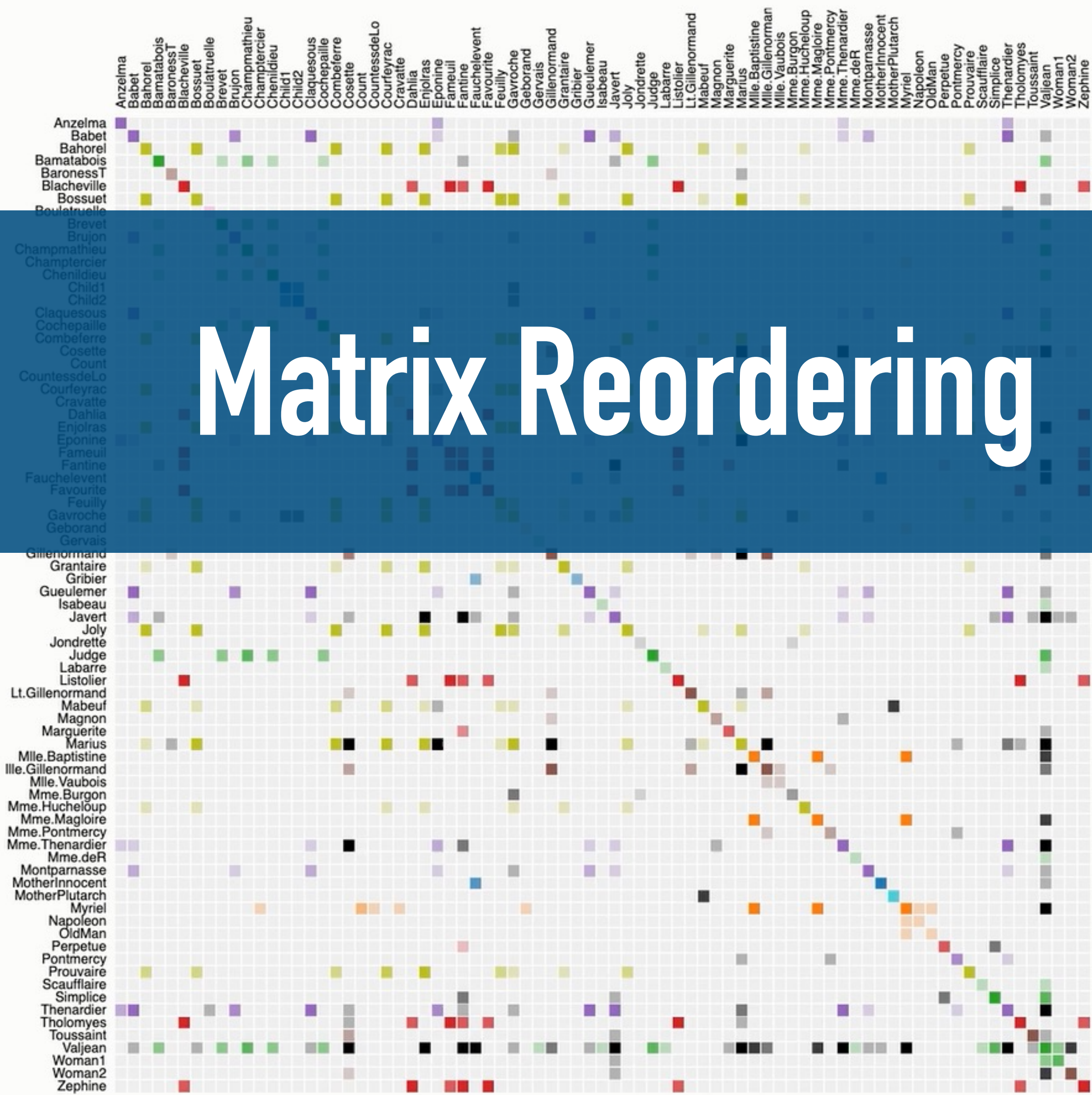
(b) Sorted by attribute similarity.

	A	B	C	D	E	
A						
B						
C						
D						
E						

Adjacency  
Matrix



# Les Misérables Co-occurrence



Order:

This matrix diagram visualizes character co-occurrences in Victor Hugo's *Les Misérables*.

Each colored cell represents two characters that appeared in the same chapter; darker cells indicate characters that co-occurred more frequently.

Use the drop-down menu to reorder the matrix and explore the data.

Built with d3.js.



# Home

[Edit](#) [New Page](#)

Jean-Daniel Fekete edited this page on Apr 23, 2015 · 2 revisions

Reorder.js is a library to reorder tables and graph/networks.

## Resources

- [Introduction](#)
- [API Reference](#)

## Browser / Platform Support

Reorder.js is mainly developed on Chrome and [Node.js](#). Use `npm install reorder.js` to install, and `require("reorder")` to load.

## Installing

Download the latest version here:

- <https://github.com/jdfekete/reorder.js/releases>

# Reorder.js

[+ Add a custom footer](#)

### ▼ Pages 12

[Home](#)[API Reference](#)[Conversion](#)[Core](#)[Gallery](#)[Graph](#)[Introduction](#)[LinearAlgebra](#)[Matrix](#)[Measure](#)[Permutation](#)[Reordering](#)

[+ Add a custom sidebar](#)



	A	B	C	D	E	
A						
B						
C						
D						
E						

Adjacency  
Matrix



Ideal for dense and completely connected networks



Requires quadratic space with respect to the number of nodes.

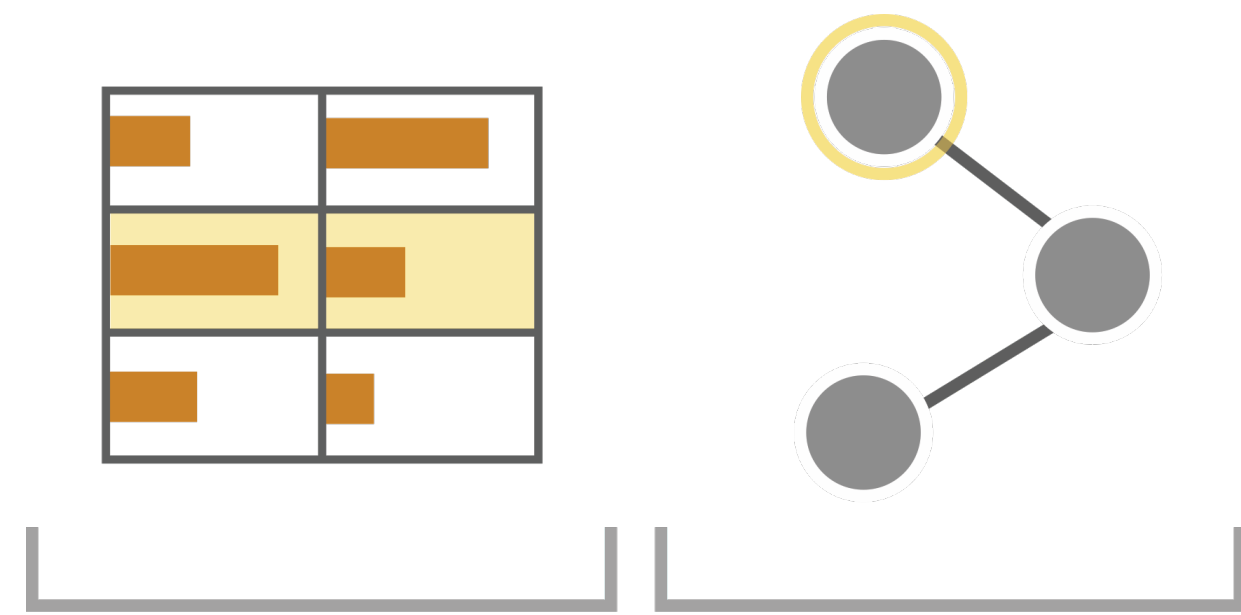
Complexity of choosing the right reordering algorithm

	A	B	C	D	E	
A						
B						
C						
D						
E						

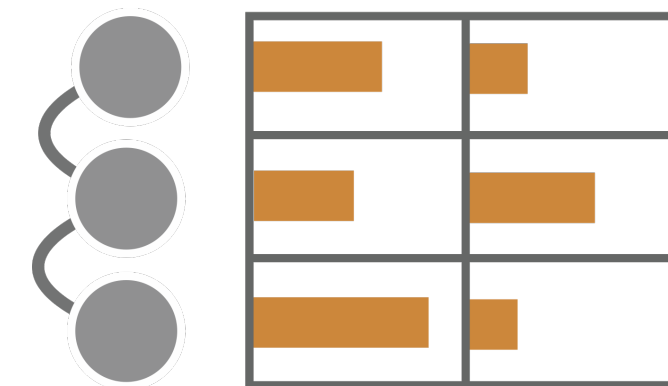
Adjacency Matrix

*Recommended for smaller, complex and dense networks with rich node and/or edge attributes, for all tasks except for those involving paths*

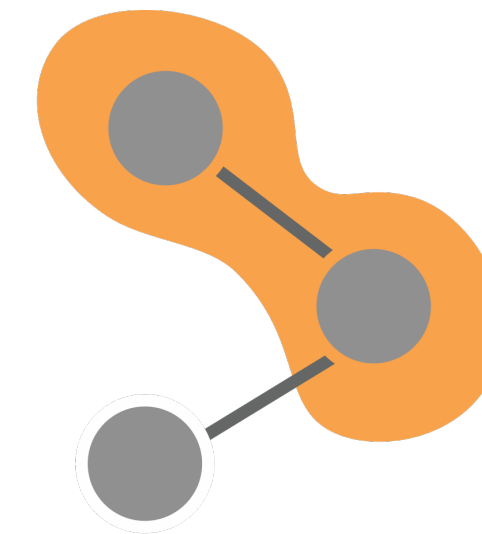
# View Operations



Juxtaposed

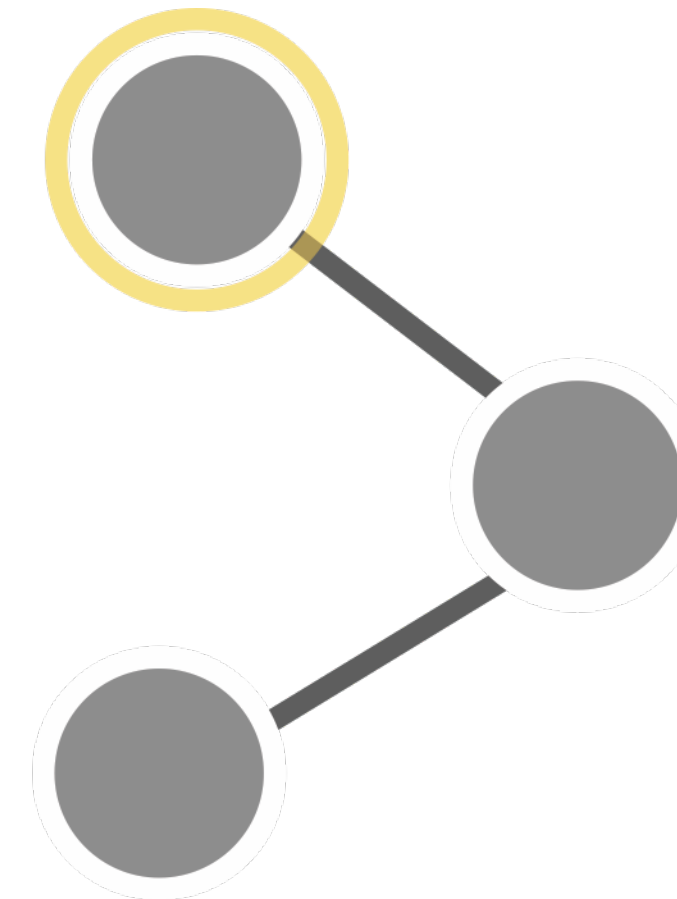
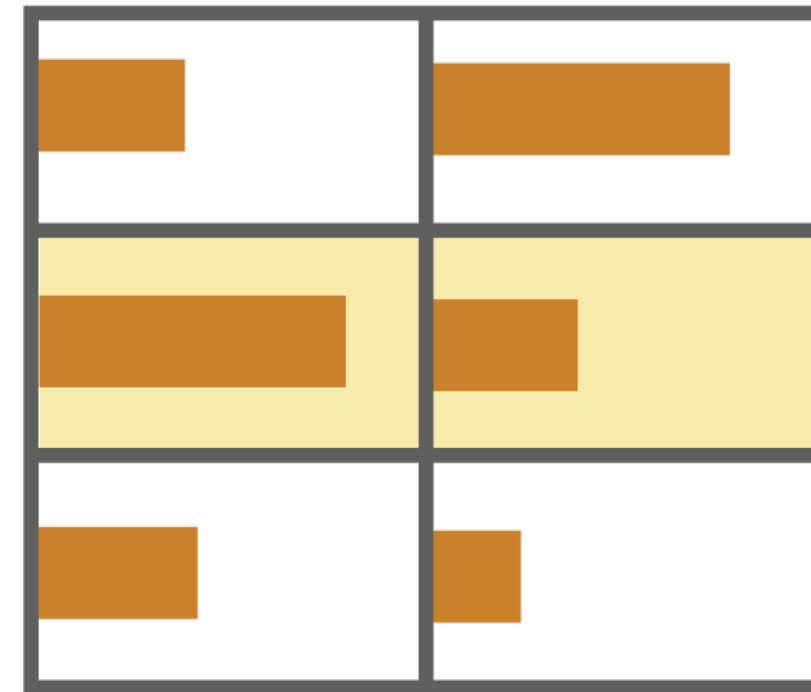


Integrated

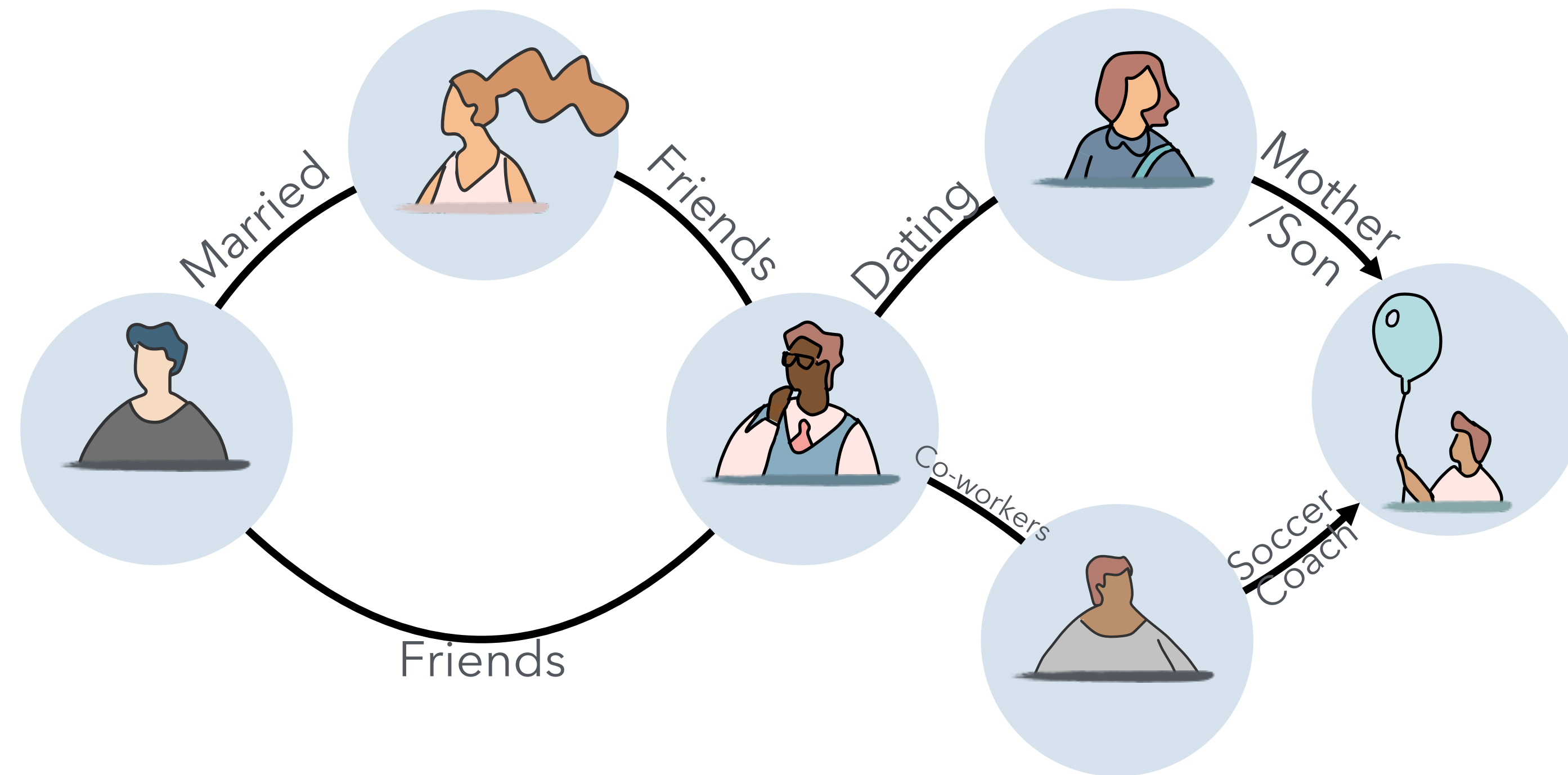


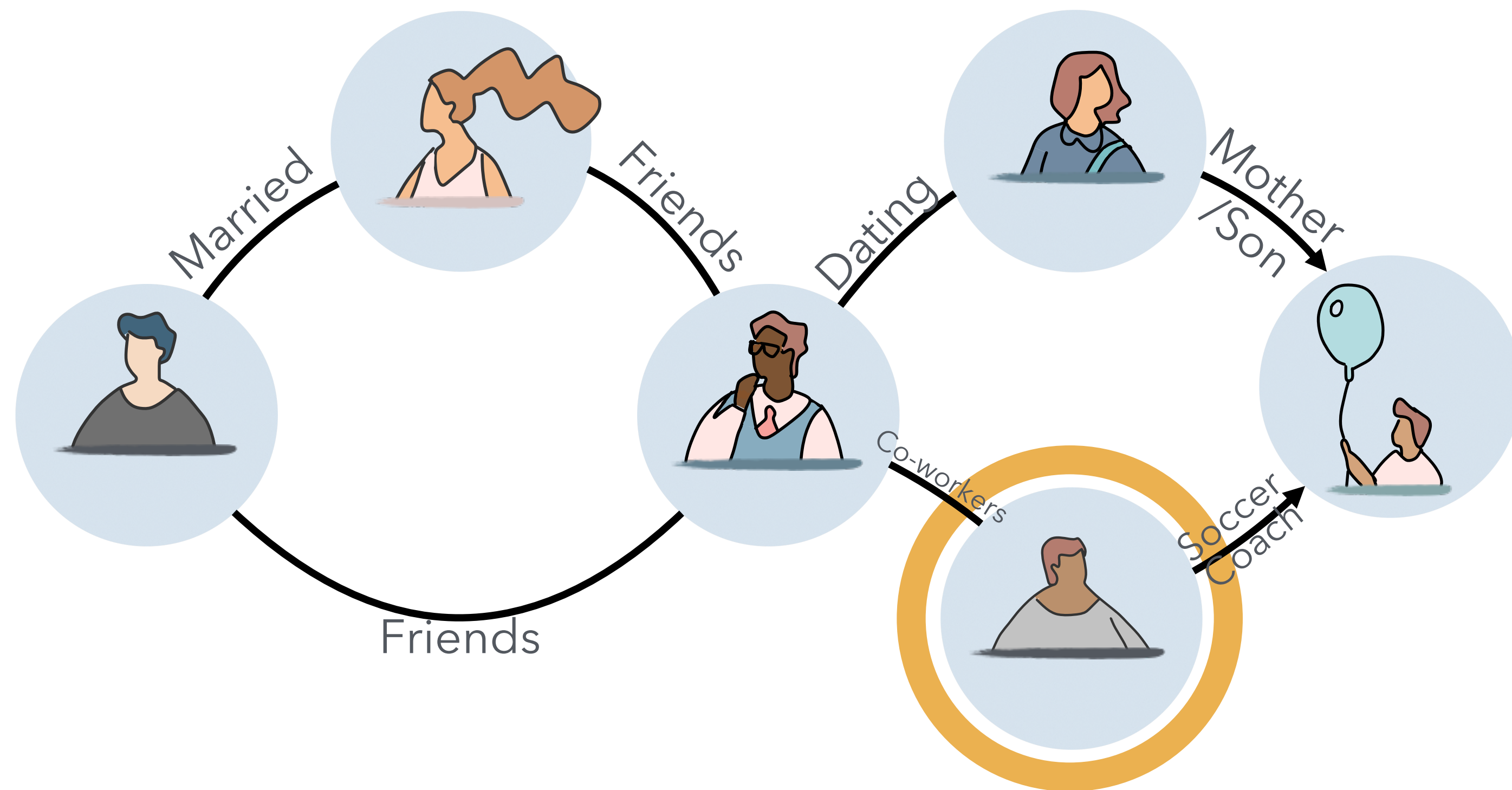
Overloaded

# Juxtaposed

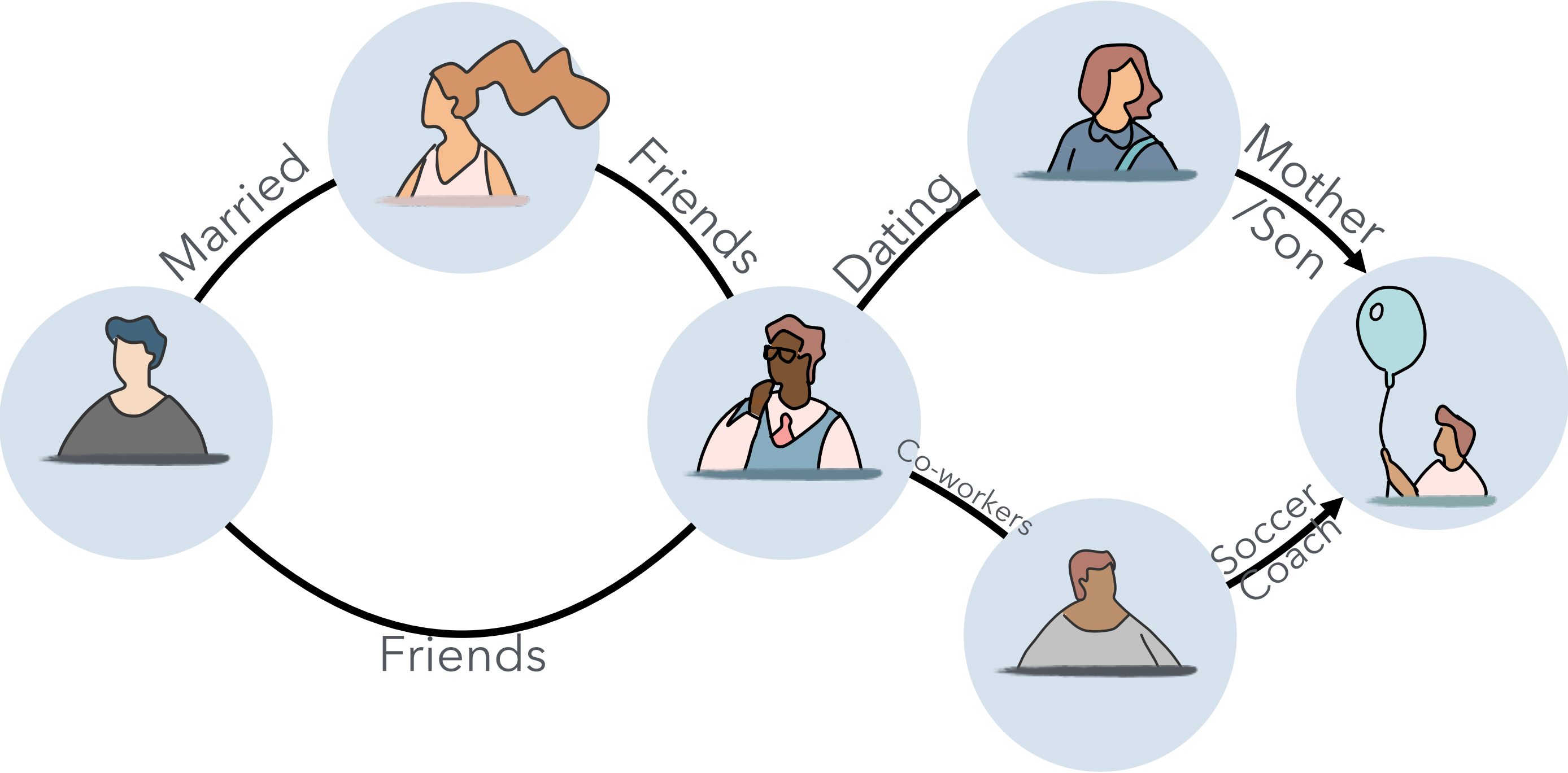






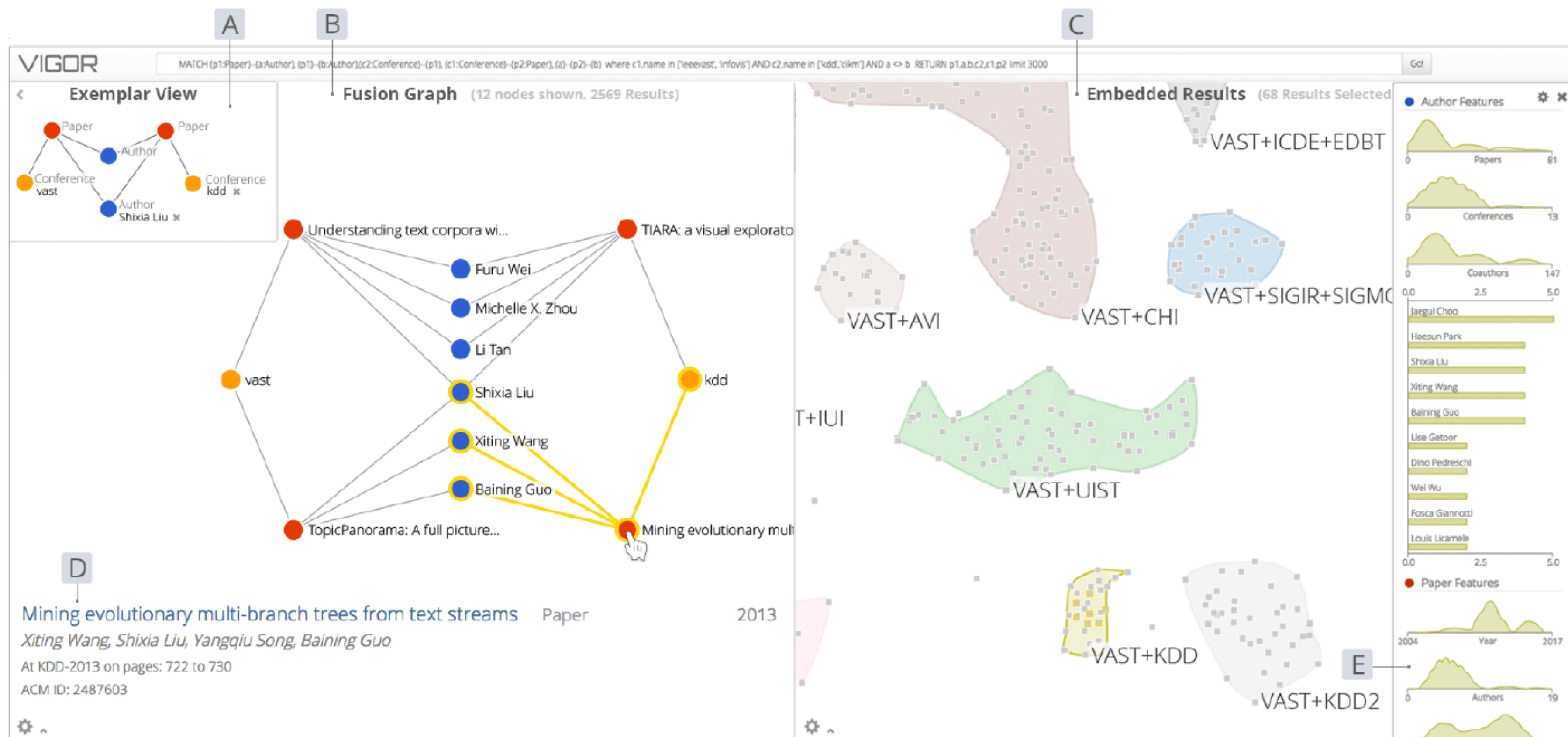


Name	Beverage	Day 1
Mark	Beer	1
Sue	Coke	0
Cole	Port	4
Jon	Coke	5
Tom	Beer	2
Abby	Port	3

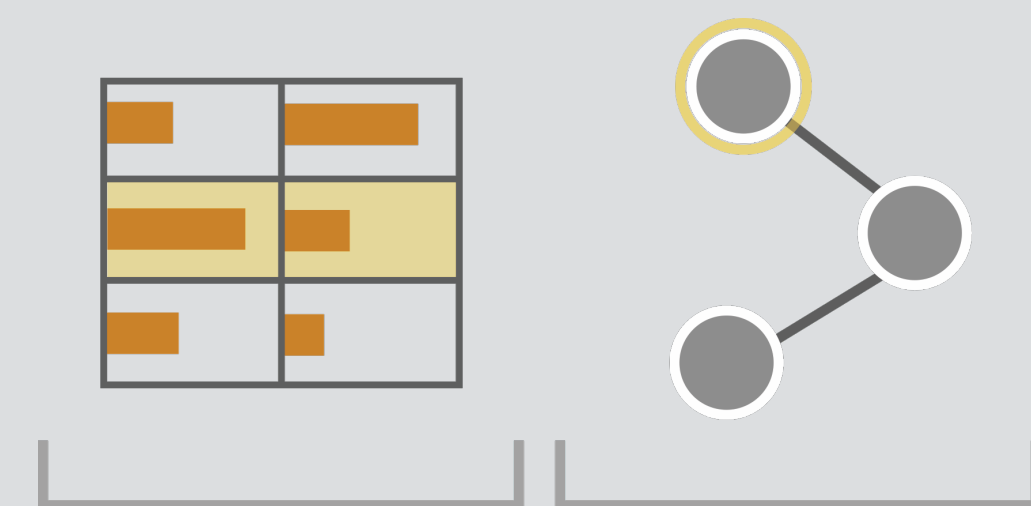


Relationship	Name	Beverage	Day 1
	Mark	Beer	1
	Sue	Coke	0
	Cole	Port	4
	Jon	Coke	5
	Tom	Beer	2
	Abby	Port	3
Years			
Dating			4
Mother / Son			12
Co-workers			3
Soccer Coach			2
Friends			8
Friends			3
Married			4

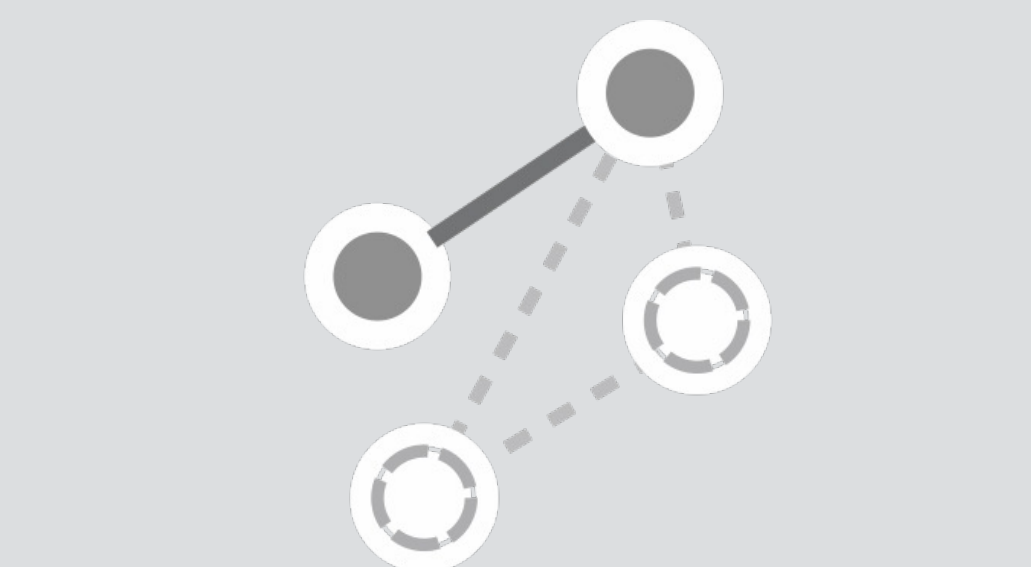




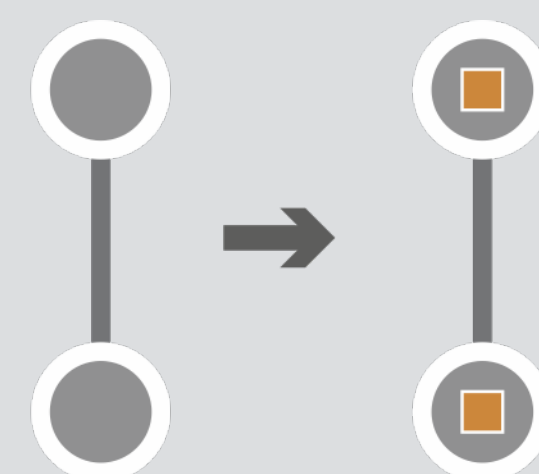
**VIGOR** Pienta et al. 2018



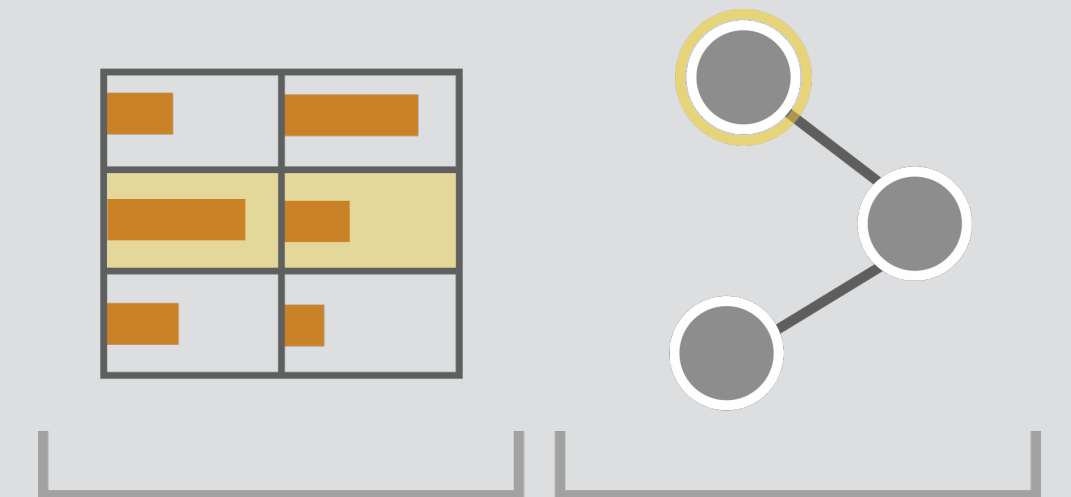
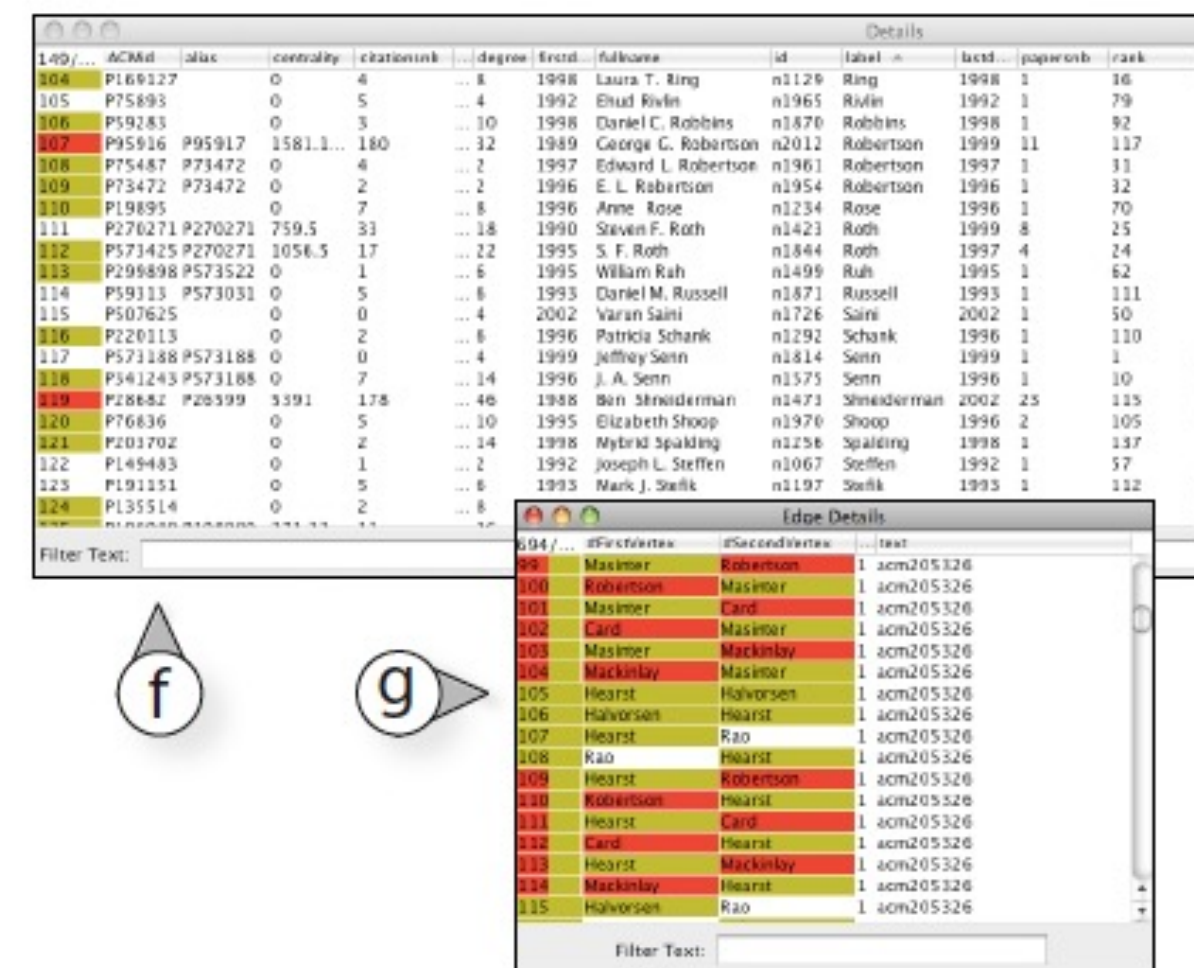
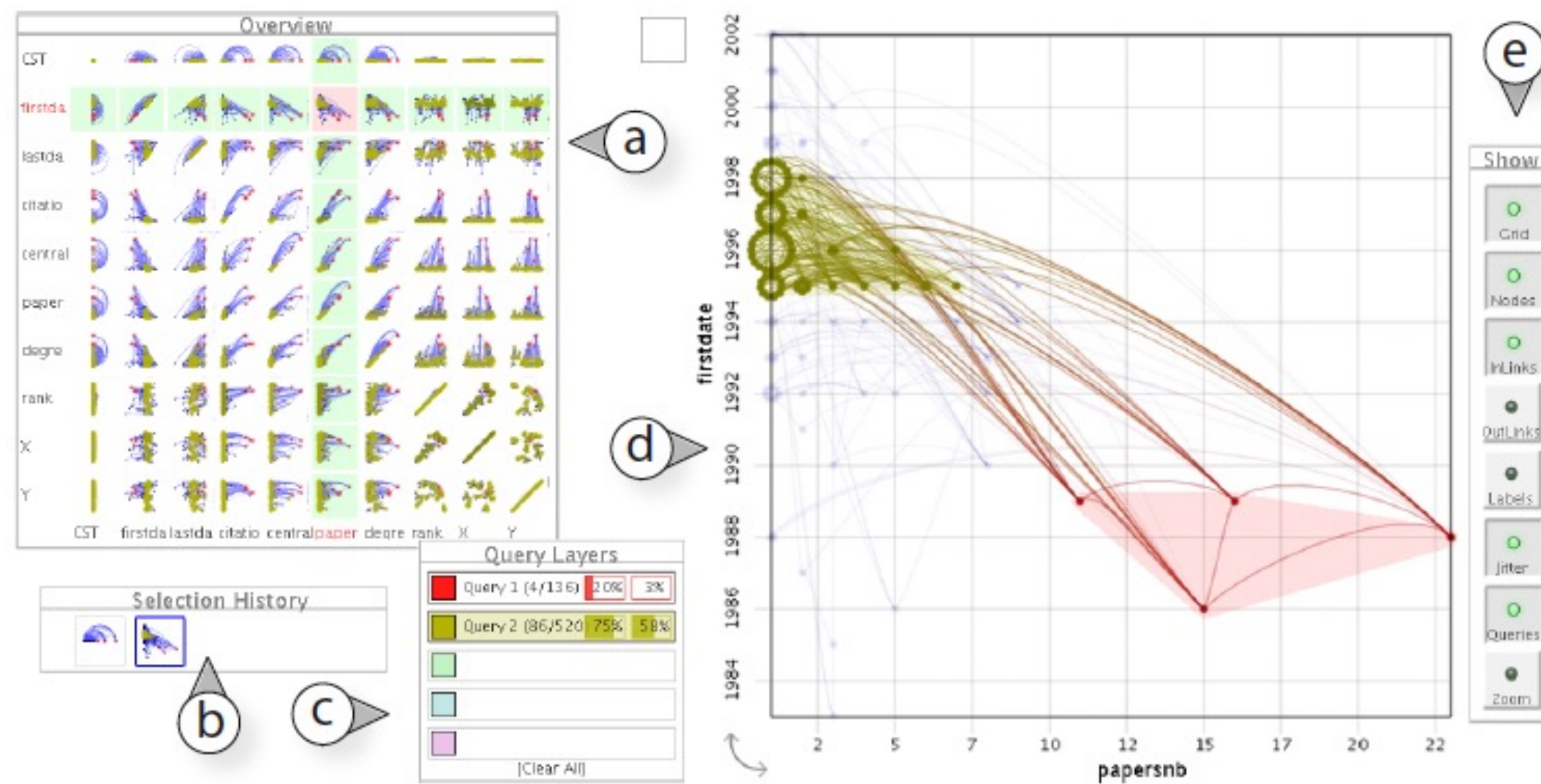
Juxtaposed



Querying and Filtering



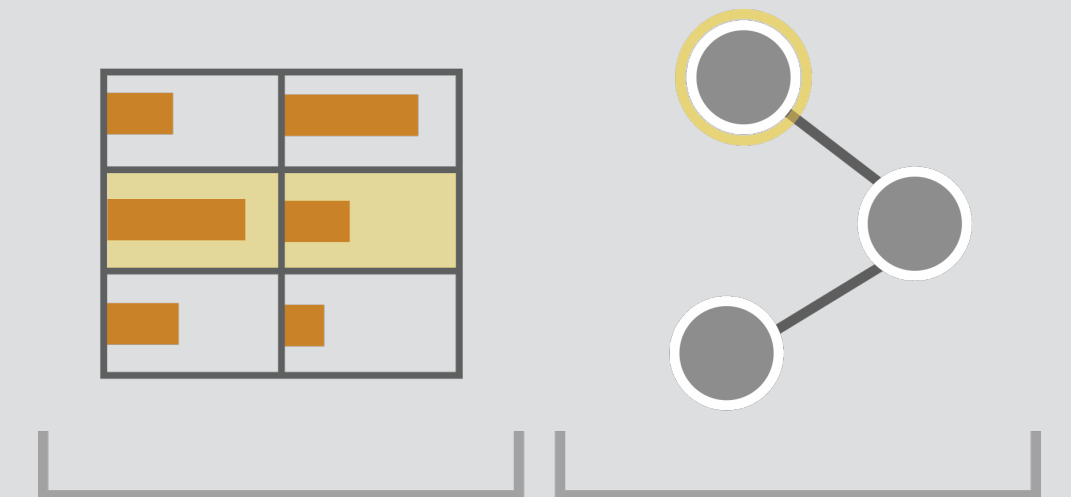
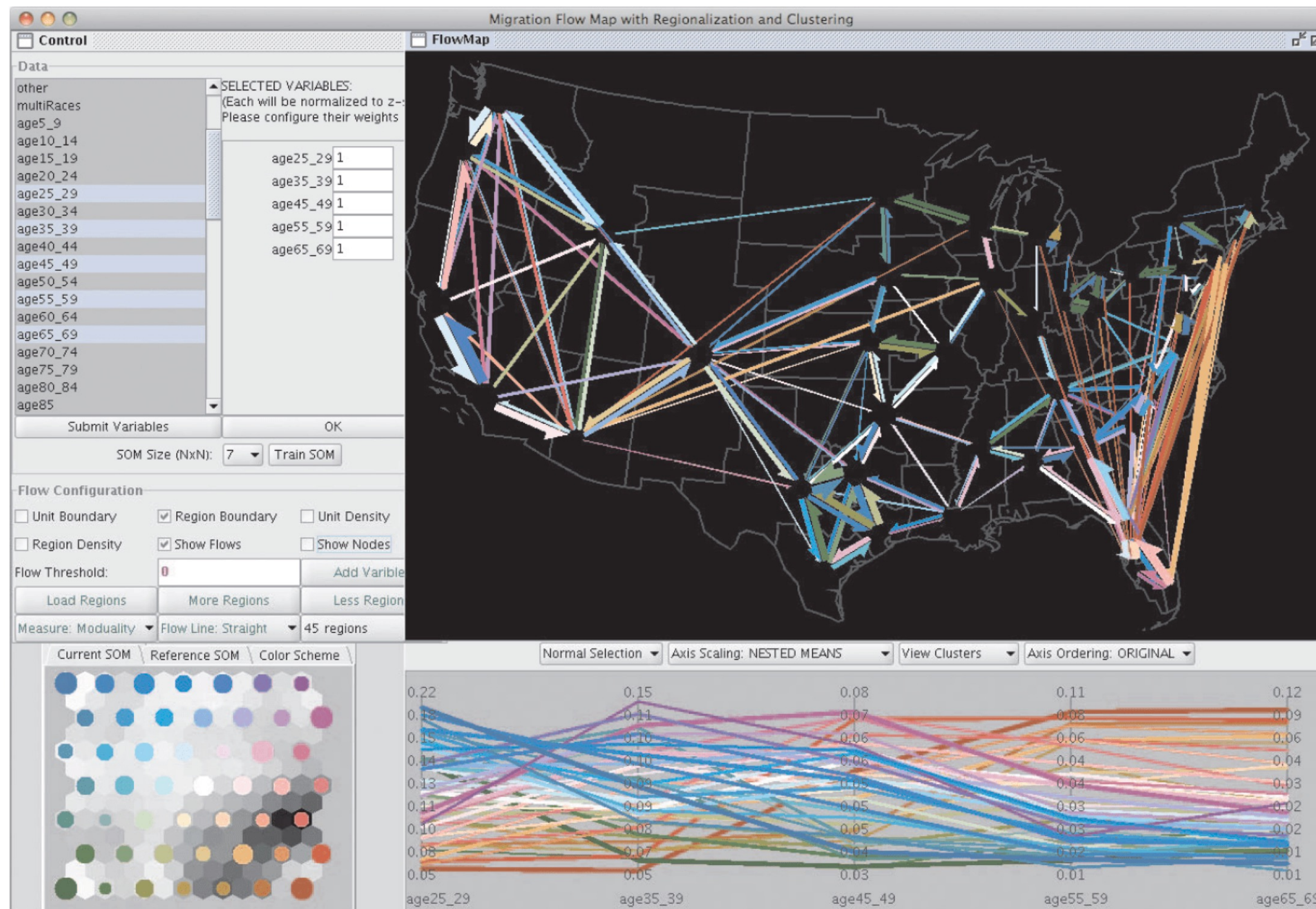
Deriving New Attributes



**Graph Dice** *Bezerianos et al. 2010*

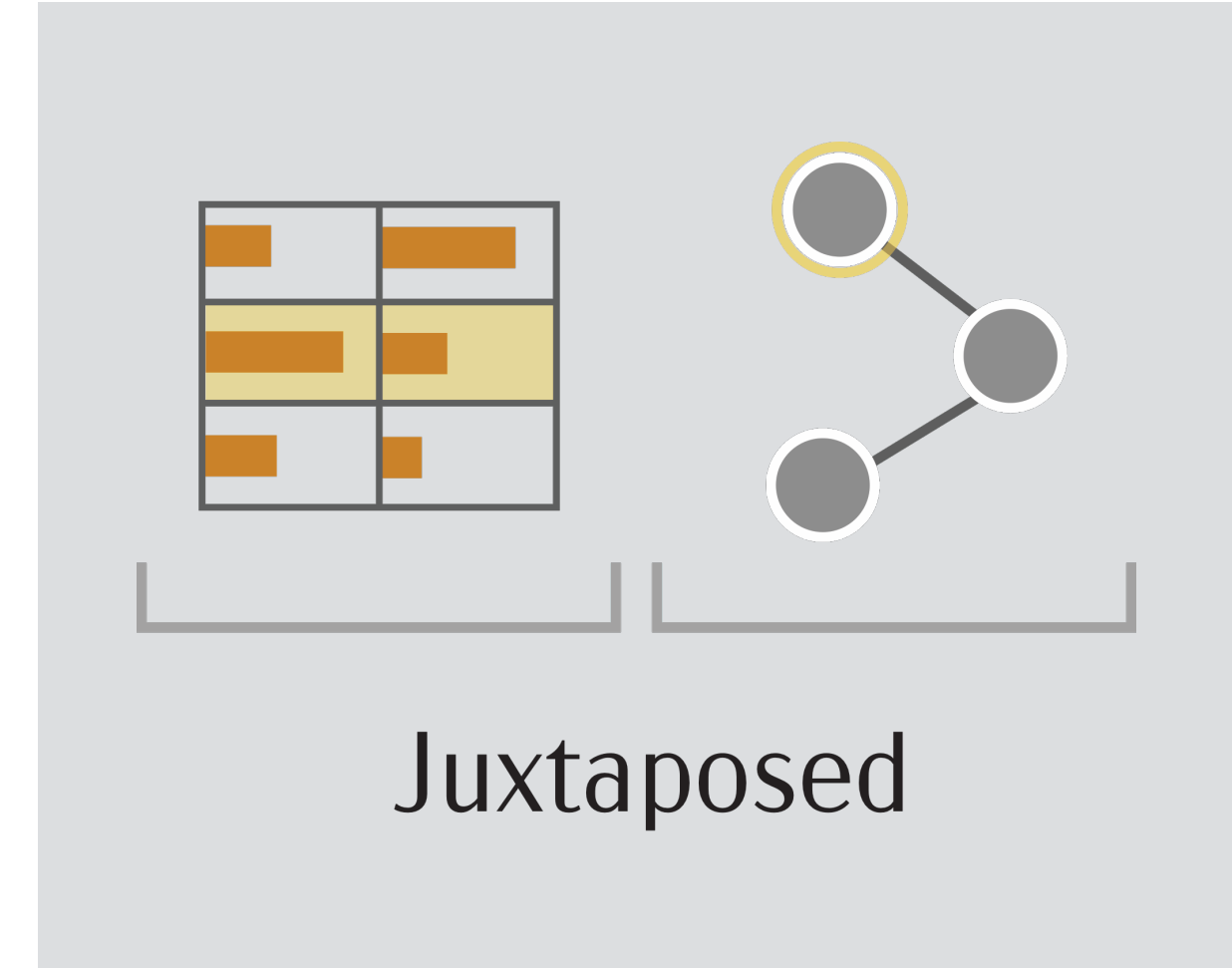


Guo, 2009



Juxtaposed

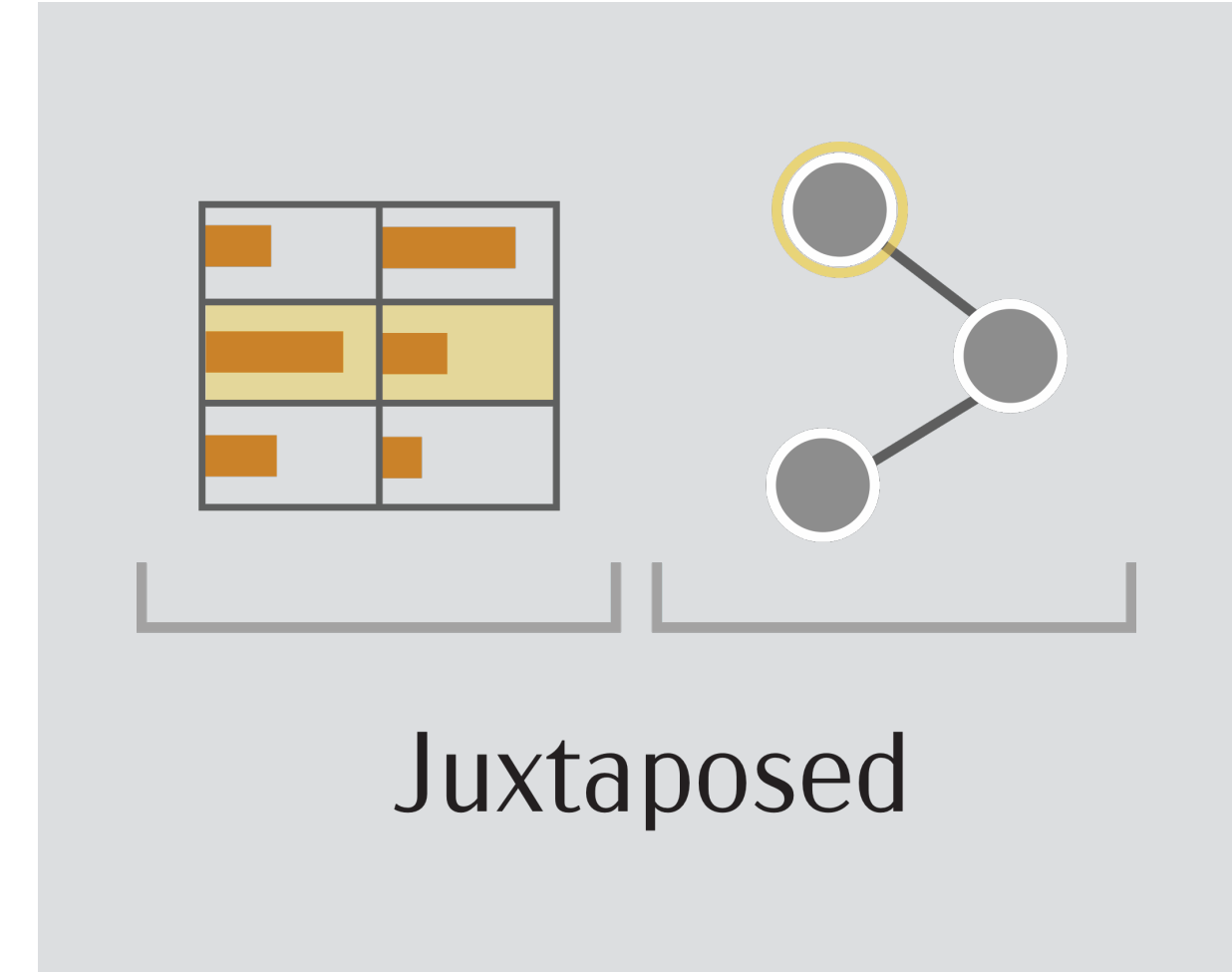




Independent views can optimize for topology and attribute independently.

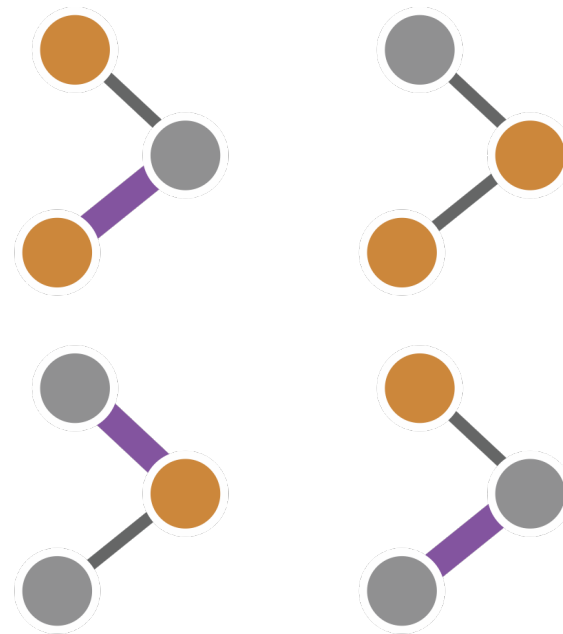


Not great for tasks on topological structures beyond a single node or edge.

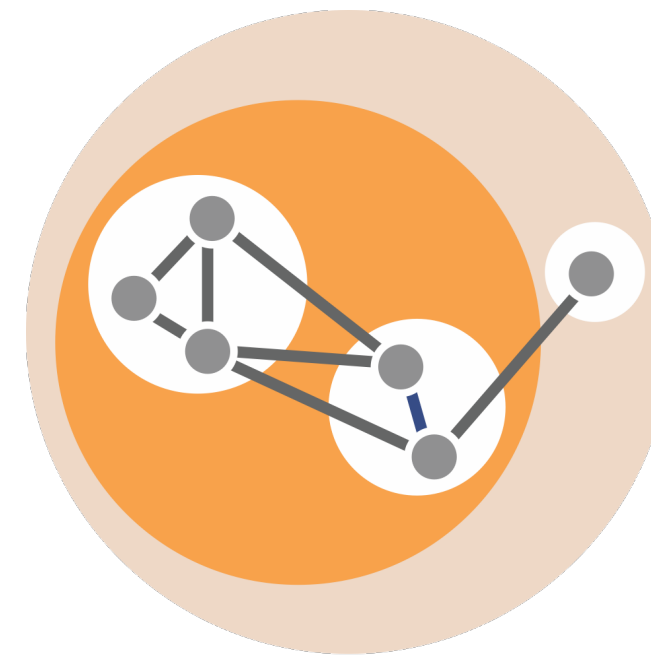


*Recommended for large networks and/or very large numbers or heterogeneous types of node and link attributes*

# Layout Operations



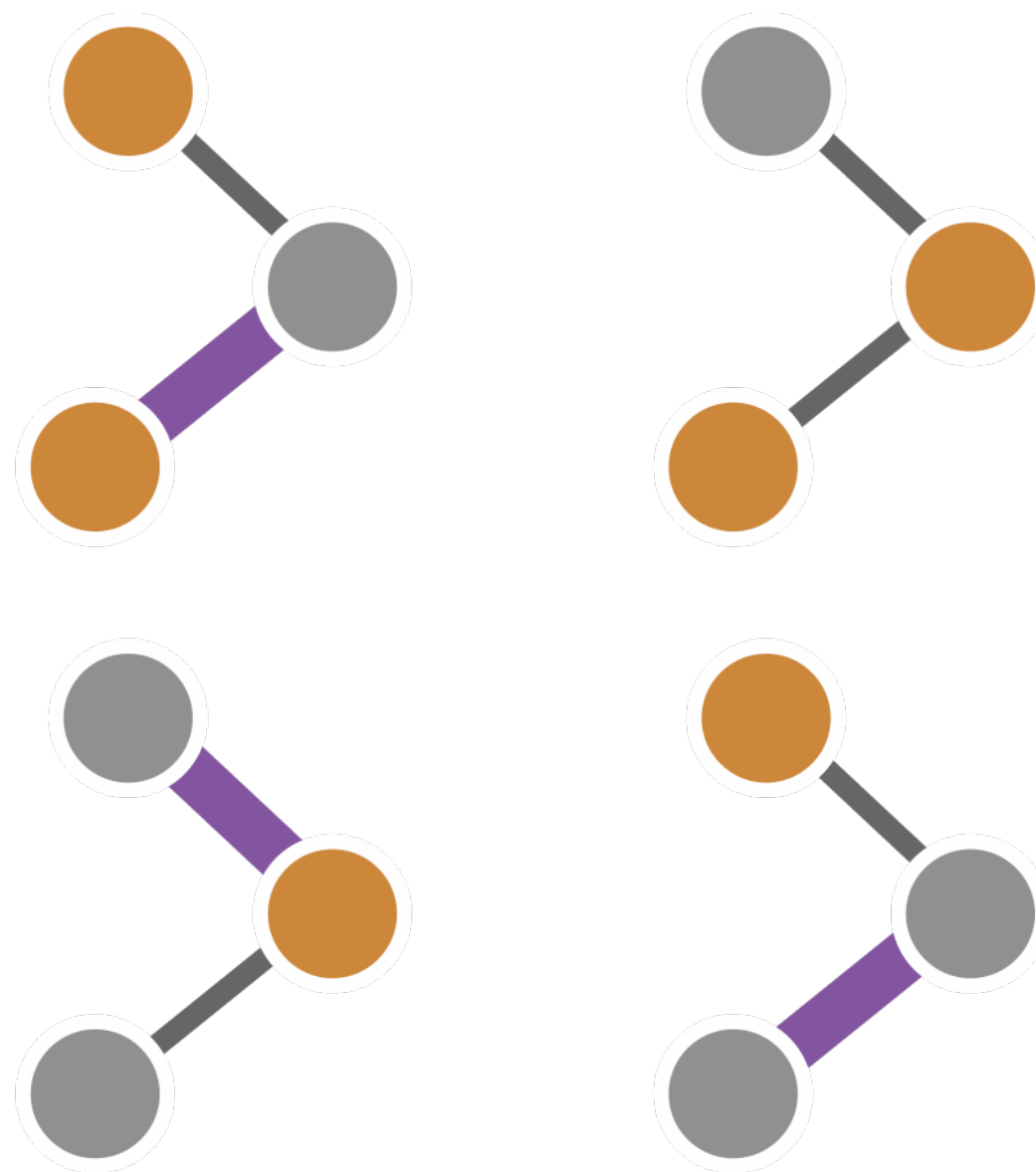
Small Multiples

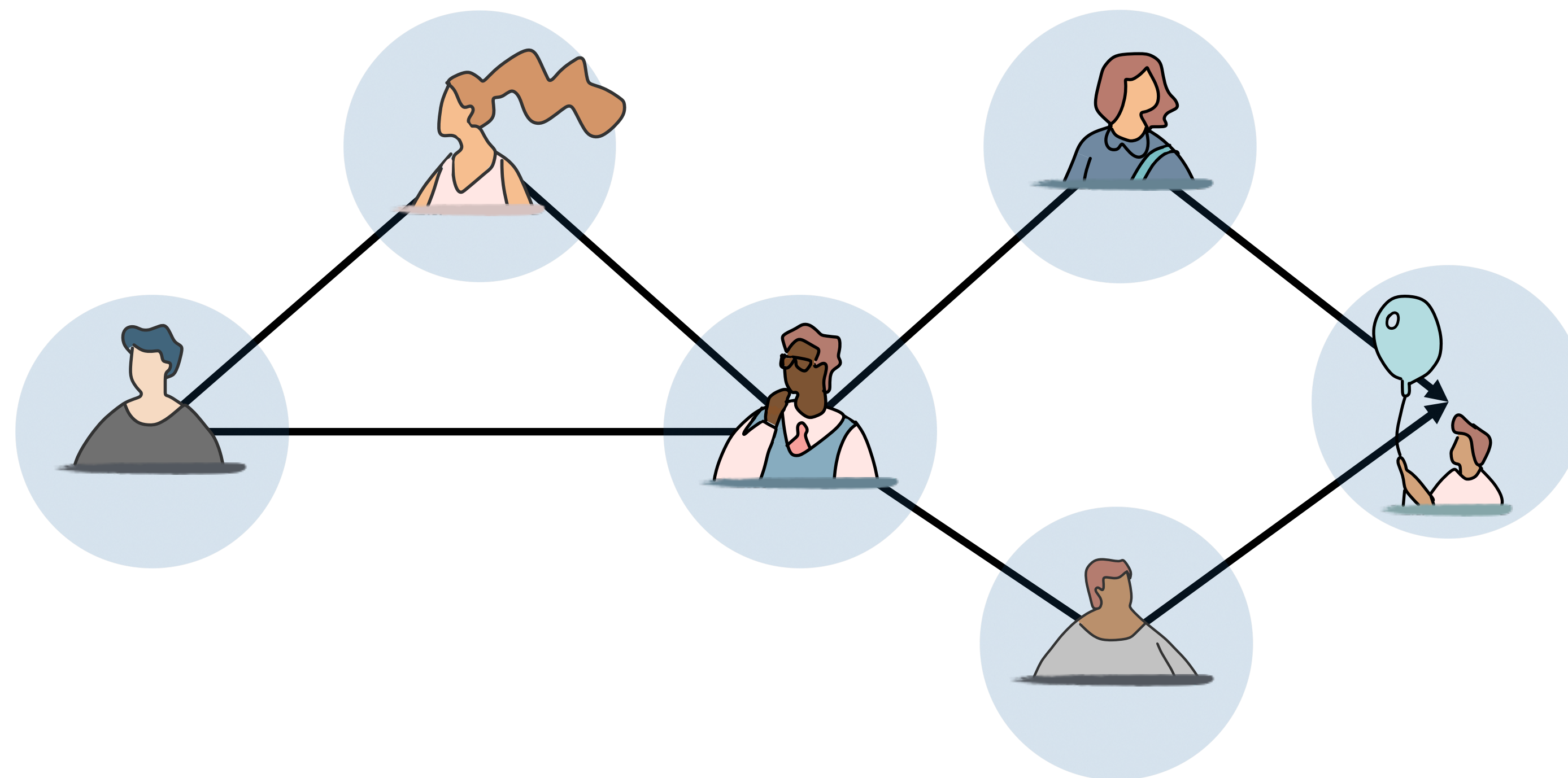


Hybrids

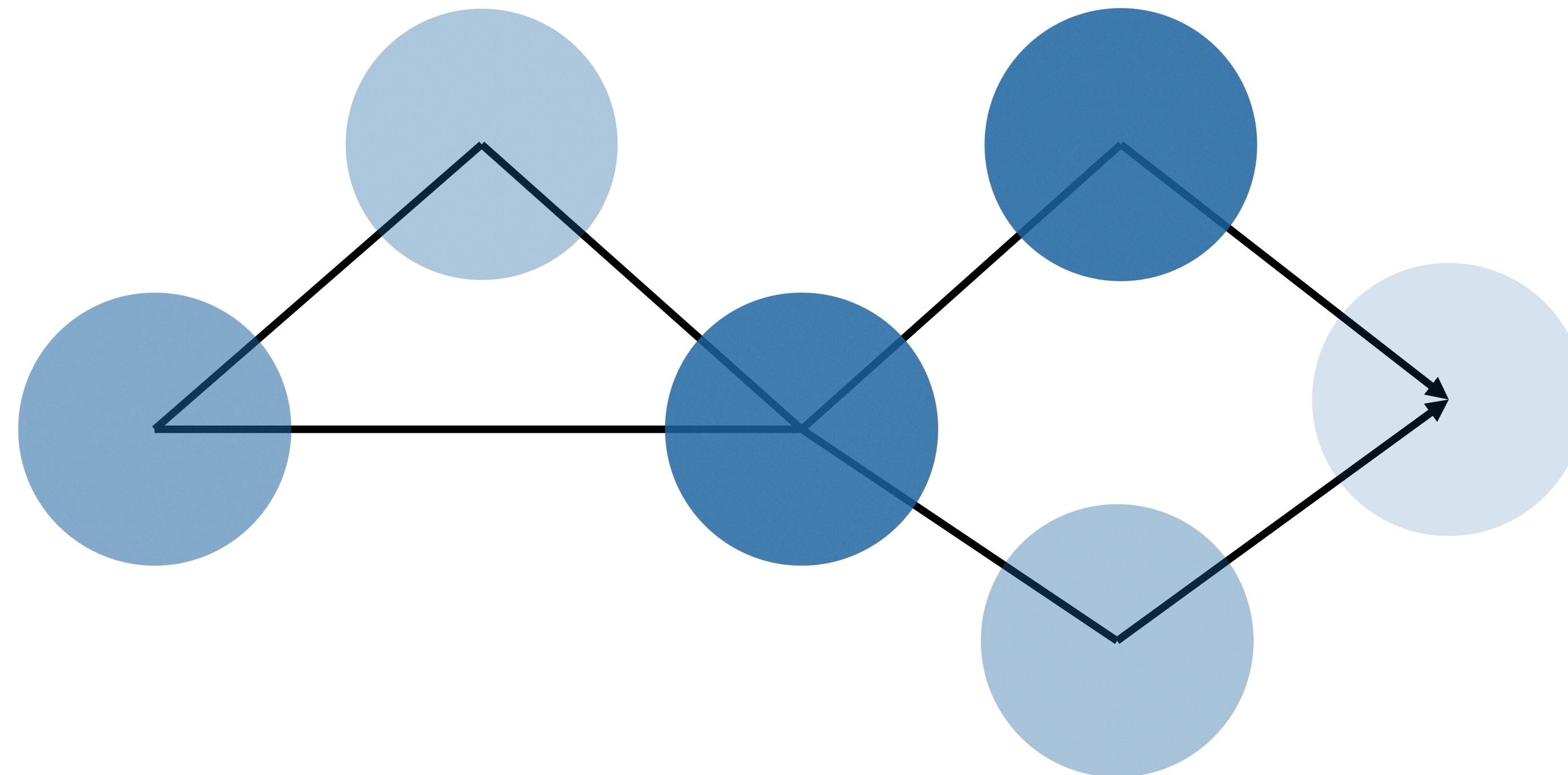


# Small Multiples



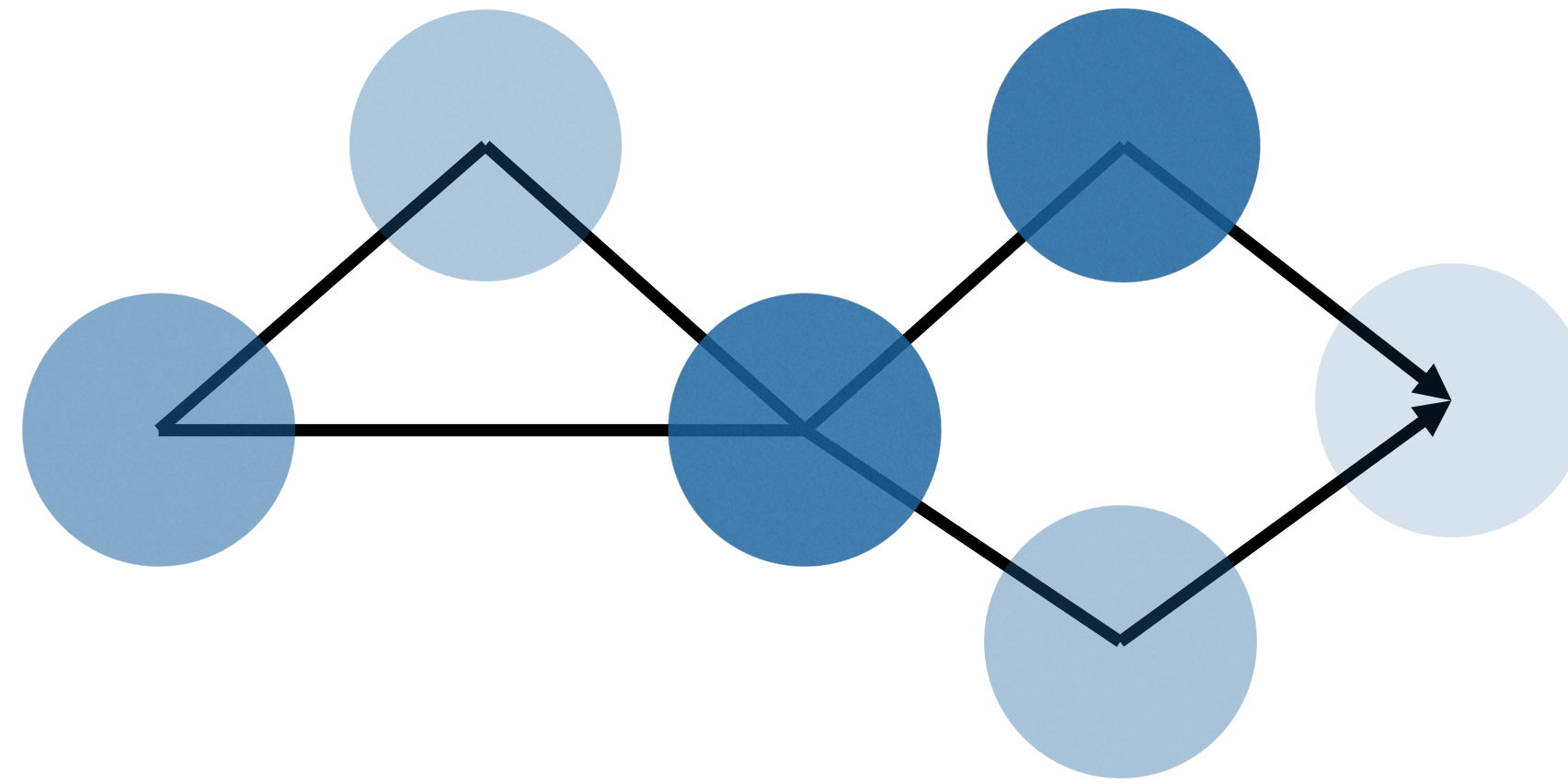


Day 1

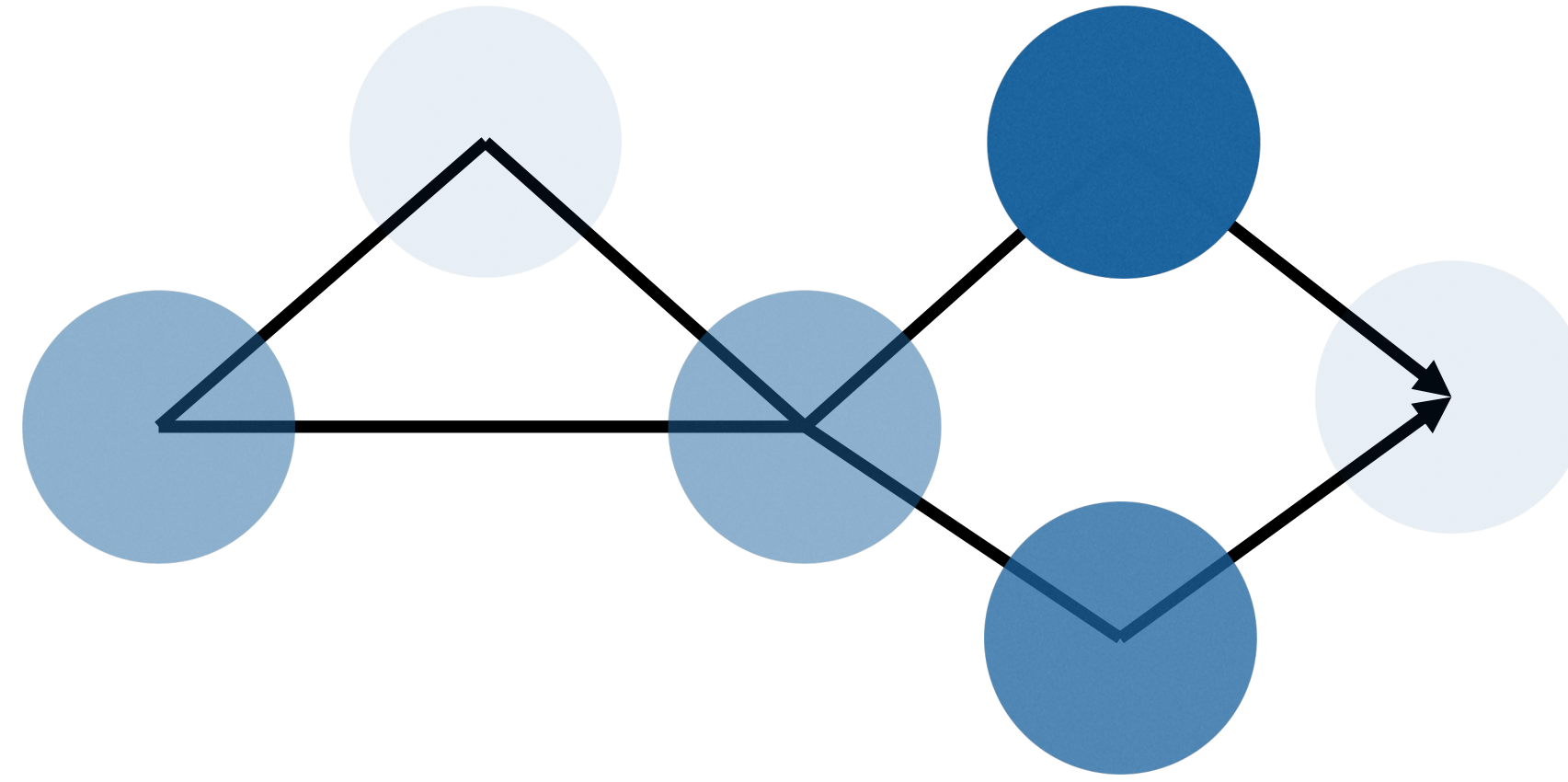




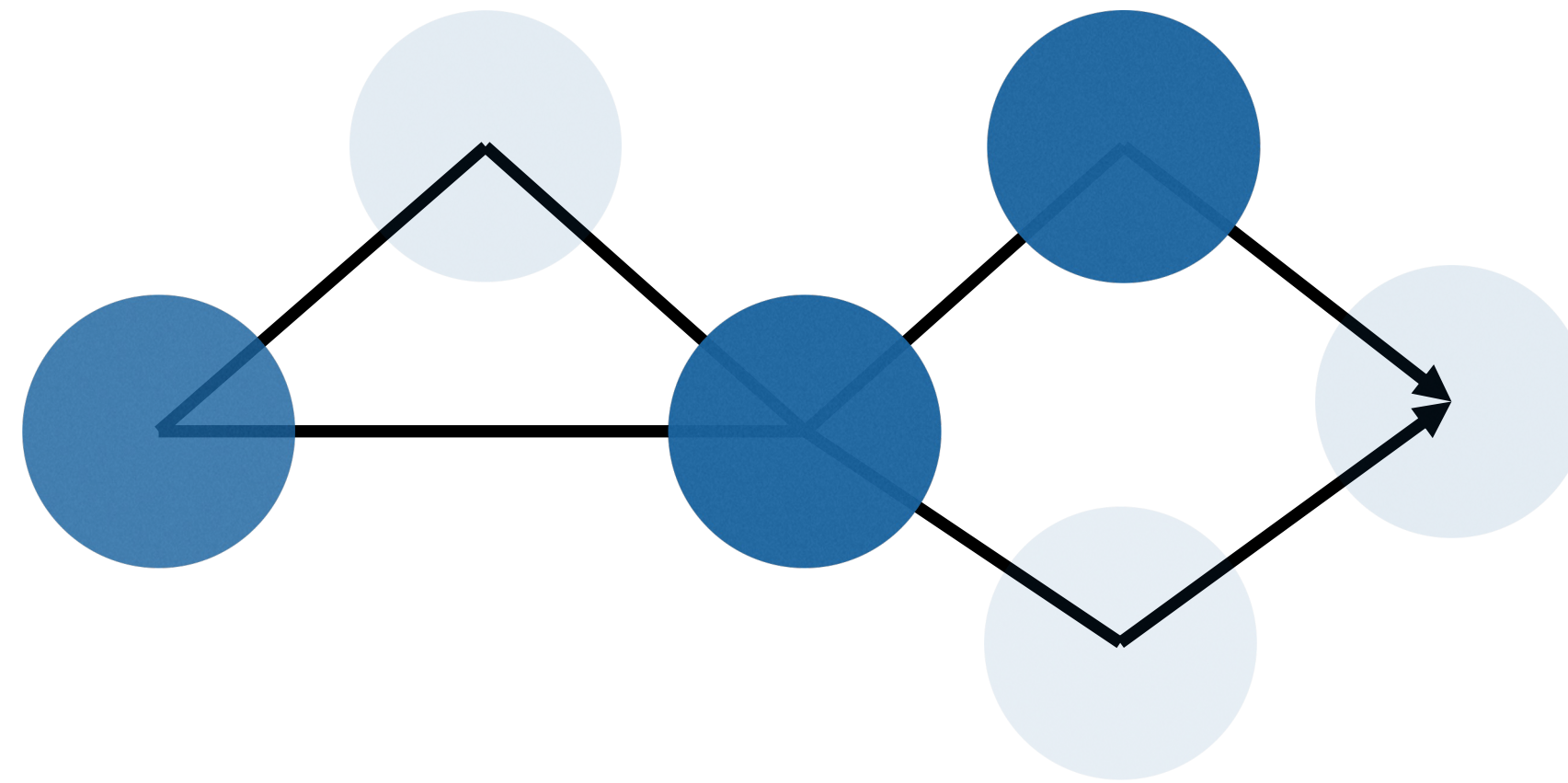
Day 1

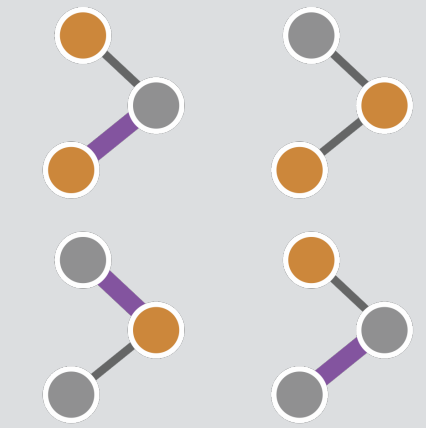
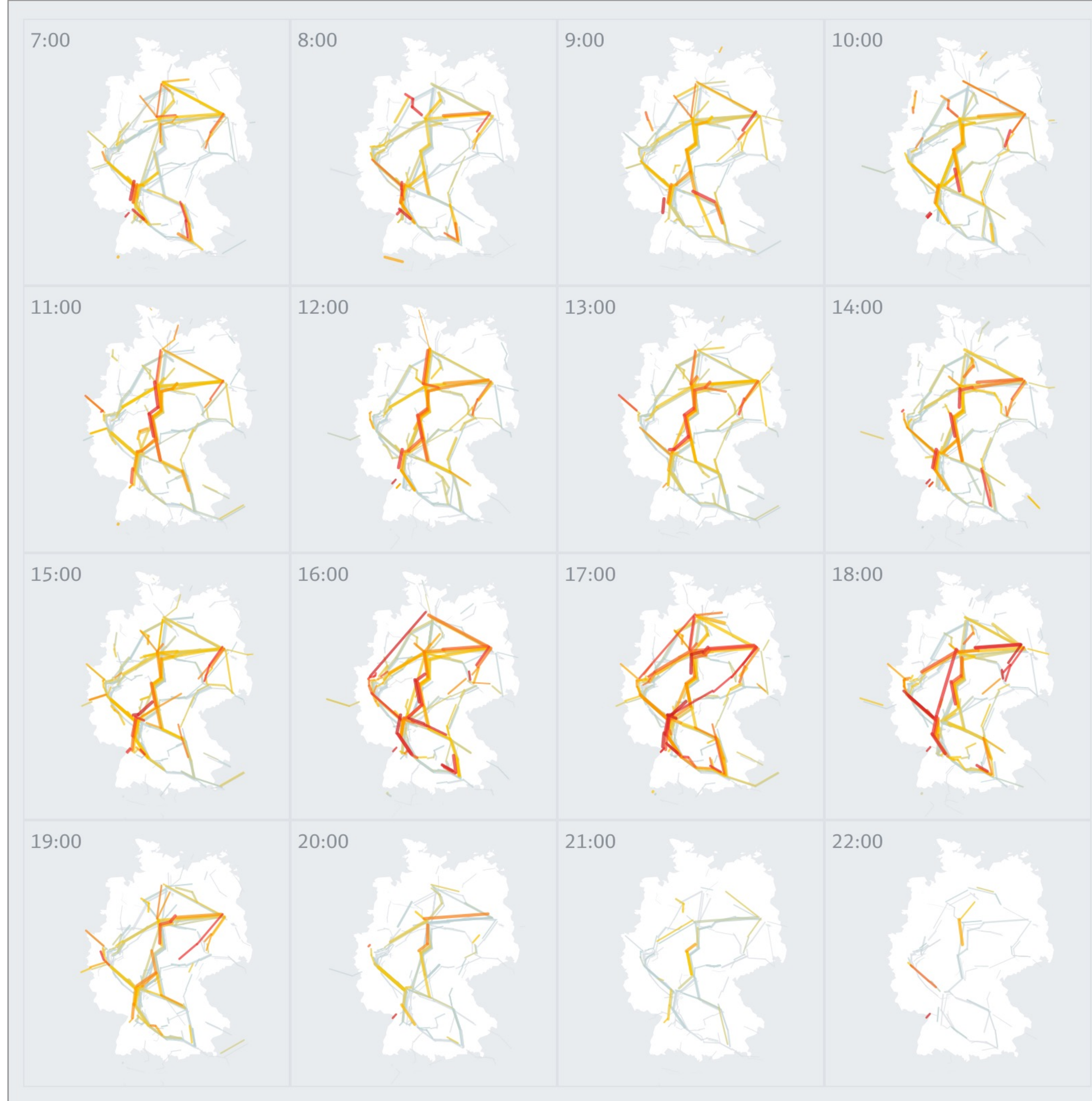


Day 2

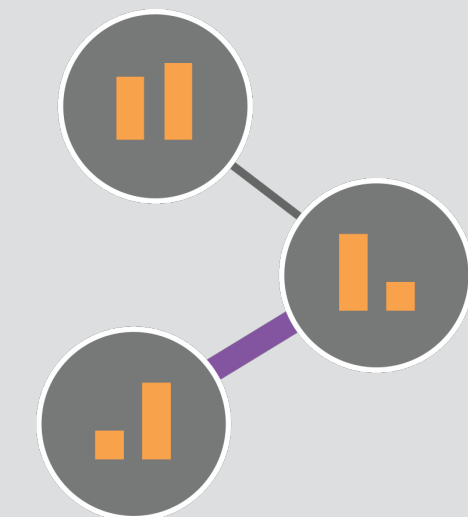


Day 3





Small Multiples



On-Node / On-Edge  
Encoding





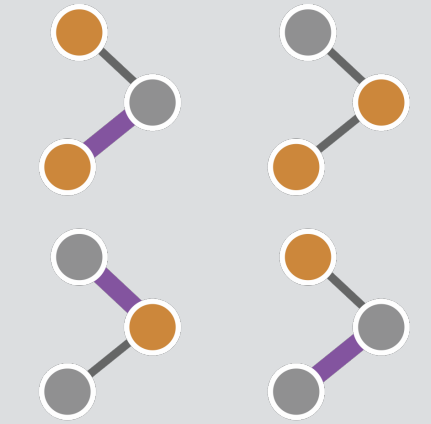
Small Multiples



Common layout facilitates attribute comparisons in specific topological features



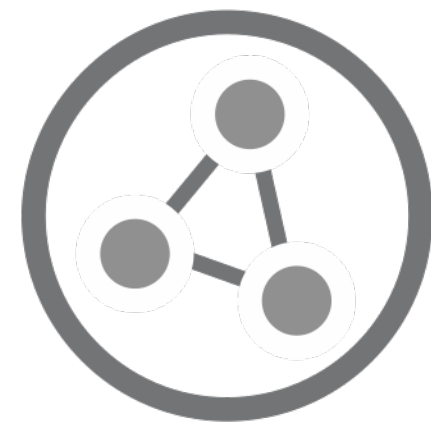
Not ideal for large networks, or tasks on clusters



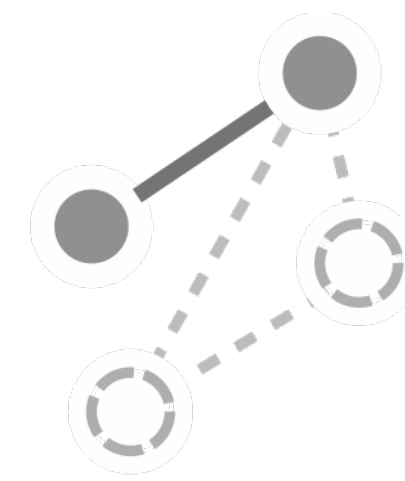
Small Multiples

*Recommended for small networks where the tasks are focused on attribute comparison*

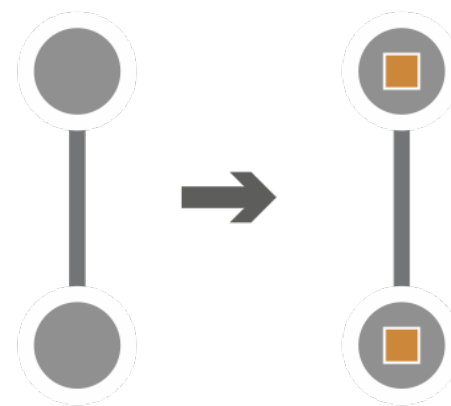
# Data Operations



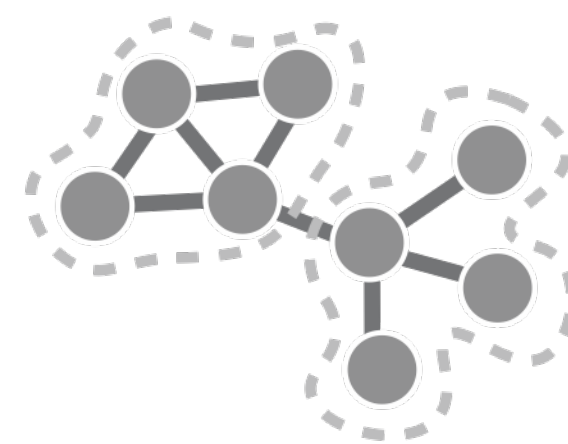
Aggregating Nodes/Edges



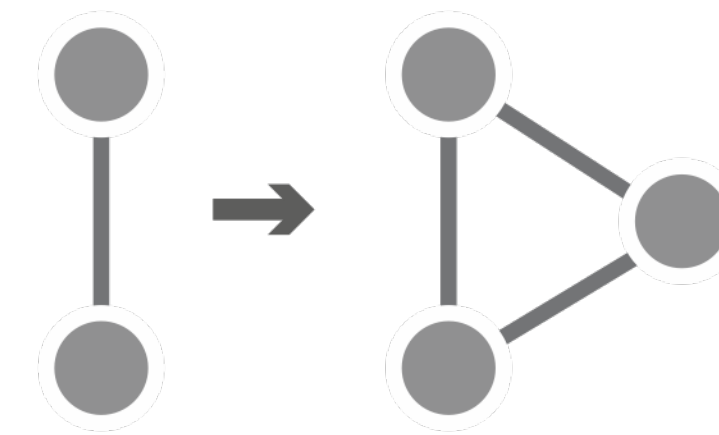
Querying and Filtering



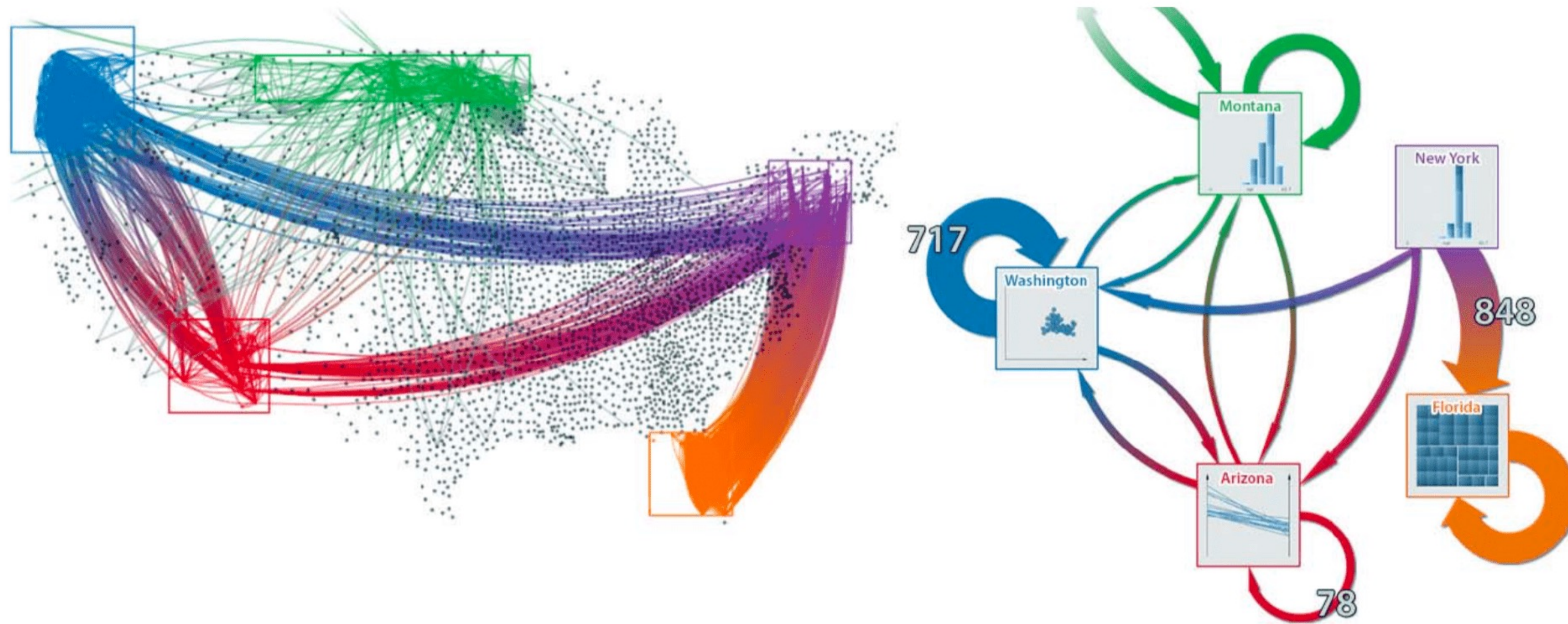
Deriving New Attributes



Clustering



Converting Attributes/Edge to Nodes



*Elzen and Wijk, 2014*



Aggregating Nodes/Edges



# Multivariate Network Visualization Techniques

A companion website for the STAR Report on Multivariate Network Visualization Techniques.

---

[HOME](#)

[TECHNIQUES](#)

[WIZARD](#)

## About

This is a companion website for a review article on multivariate network visualization techniques.

Multivariate networks are networks where both the structure of the network and the attributes of the nodes and edges matter. It turns out, these are very common. Every person in a social network, for example, has both, relationships and lots of other characteristics, such as their age, the school they went to, or the city they live in. Multivariate network visualization techniques are designed to be able to show both, these attributes and the structure. Using these visualization techniques, we can analyze, for example, if a network of friends predominantly went to the same high school.

The visualization research community has developed many techniques to visualize these kinds of networks, and our review article – and this website – are designed to help you sort through these options.

Browse through the techniques illustrated below, or use our wizard to find the right multivariate network visualization technique for your datasets and tasks!

[Get in touch](#) if you have questions or comments.

## Use the Wizard

Technique recommendations to fit your needs!

Navigate to the [wizard tab](#) and select your specific network characteristics, such as the size of the network and its type, and what tasks are relevant for your analysis and receive technique recommendations that are best suited to your selection.

## Read the Review Article

**The State of the Art in Visualizing Multivariate Networks**

Carolina Nobre, Miriah Meyer, Marc Streit, and Alexander Lex  
To appear in Computer Graphics Forum (EuroVis 2019)

vdl.sci.utah.edu/mvnmv/